

1) A car traveling  $60.0 \text{ km/h}$  is  $25.0 \text{ m}$  from a barrier when the driver slams on the brakes. The car hits the barrier  $2.00 \text{ s}$  later. (a) What is the car's constant deceleration before impact? (5 pts) (b) How fast is the car traveling at impact? (5 pts)

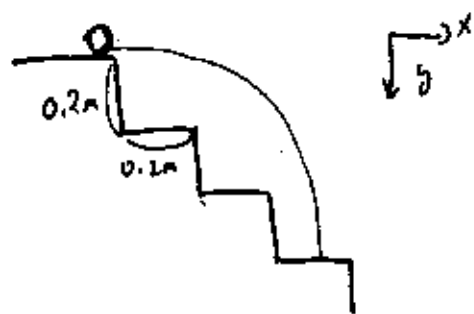
$$a) \quad \Delta x = v_0 t + \frac{1}{2} a t^2 \quad v_0 = 60 \frac{\text{km}}{\text{h}} = 16.67 \text{ m/s}$$

$$\Rightarrow a = 2 \times \frac{(\Delta x - v_0 t)}{t^2} = -4.17 \text{ m/s}^2$$

$$b) \quad v = v_0 + a t = 16.67 \text{ m/s} - 4.17 \text{ m/s}^2 \times 2 \text{ s} \\ = 8.33 \text{ m/s}$$

You can also use  $v^2 = v_0^2 + 2a \Delta x$ .  
Numerically, the above formula is simpler.

2) A ball rolls horizontally off the top of a stairway with a speed of  $1.6 \text{ m/s}$ . The steps are  $20 \text{ cm}$  high and  $20 \text{ cm}$  wide. If one defines the first step to be the first one down, which step does the ball hit first? Show a picture in addition to the calculations.



$$x = v_0 t$$

$$y = \frac{1}{2} g t^2 = \frac{1}{2} g \left( \frac{x}{v_0} \right)^2$$

let  $y_1 = 0.2 \text{ m}$       $x_1 = 0.2 \text{ m} \leftarrow 1^{\text{st}} \text{ step}$

Number of steps:  $n$      an integer

$$n y_1 = \frac{1}{2} g \left( \frac{n x_1}{v_0} \right)^2$$

e.g.  $1 < n < 2$   
 $\Rightarrow n = 2$   
 $2 < n < 3$   
 $n = 3$

Discarding  $n = 0$

$$\Rightarrow n = \frac{2 y_1 v_0^2}{g x_1^2} = 2.6 \Rightarrow n = 3$$

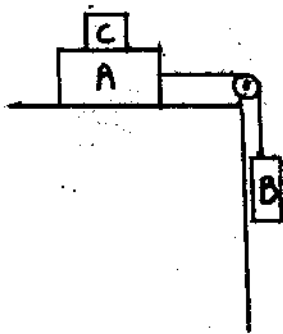
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 $3^{\text{rd}} \text{ step}$

Another way is to work in increments of height. For example at

$$y = 0.6 \text{ m} \quad t = 0.35 \text{ s} \quad \Rightarrow x = 0.56 \text{ m} < 0.6 \text{ m}$$

$\Rightarrow 3^{\text{rd}} \text{ step}$ .

3) In the Figure shown below, blocks A and B have weights of  $44\text{ N}$  and  $22\text{ N}$ , respectively. (a) Determine the minimum weight of block C to keep A from sliding if  $\mu_s$  between A and the table is  $0.20$ . (5 pts) (b) Block C suddenly is lifted off A. What is the acceleration of block A if  $\mu_k$  between A and the table is  $0.15$ . (5 pts)



$$a) \text{ For B: } T - m_B g = 0 \Rightarrow T = m_B g = 22\text{ N}$$

$$\text{For A+C: } \mu_s (m_A g + m_C g) = T = 22\text{ N}$$

$$0.2 (44\text{ N} + m_C g) = 22\text{ N} \Rightarrow m_C g = 110\text{ N} - 44\text{ N} = 66\text{ N}$$

b) If C is lifted, we get:

$$\text{for A: } T - \mu_k \times 44\text{ N} = m_A a$$

$$\text{for B: } 22\text{ N} - T = m_B a$$

$$\Rightarrow 22\text{ N} - \mu_k \times 44\text{ N} = (m_A + m_B) a$$

$$\Rightarrow a = 2.3\text{ m/s}^2$$