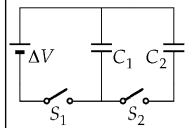
## PHYS 232 Lecture supplement 10



26.23: C1= 6  $\mu$ F, C2= 3  $\mu$ F, and  $\Delta$ V= 20 V. Capacitor C1 is charged by closing S1. S1 is then opened and S2 is closed. Calculate the initial charge on C1 and the final charge on each capacitor.

26.40: Two identical parallel-plate capacitors, each with capacitance C, are charged to  $\Delta V$  and connected in parallel. Then the plate separation in one is doubled. Find:

- 1. the total energy of the two capacitors before the change
- 2. the potential difference across each after the change
- 3. total energy of the system after the change

## 27.9

The electron beam from a particle accelerator has a circular cross section of radius 1.00 mm.

- If the current is 8  $\mu$ A, what is the current density in the beam assuming that it is uniform throughout?
- Find the electron density of the beam.

27.9 (a) 
$$J = \frac{I}{A} = \frac{8.00 \times 10^{-6} \text{ A}}{\pi (1.00 \times 10^{-3} \text{ m})^2} = [2.55 \text{ A/m}^2]$$

(b) From 
$$J = nev_d$$
, we have 
$$n = \frac{J}{ev_d} = \frac{2.55 \text{ A/m}^2}{\left(1.60 \times 10^{-19} \text{ C}\right) \left(3.00 \times 10^8 \text{ m/s}\right)} = \frac{5.31 \times 10^{10} \text{ m}^{-3}}{5.31 \times 10^{10} \text{ m}^{-3}}$$

(c) From 
$$I = \Delta Q / \Delta t$$
, we have 
$$\Delta t = \frac{\Delta Q}{I} = \frac{N_{\rm A}e}{I} = \frac{\left(6.02 \times 10^{23}\right)\left(1.60 \times 10^{-19}~{\rm C}\right)}{8.00 \times 10^{-6}~{\rm A}} = \boxed{1.20 \times 10^{10}~{\rm s}}$$
(This is about 381 years!)

$$C = \frac{Q}{\Delta V}$$

so 
$$6.00 \propto 10^{-6} = \frac{Q}{20.0}$$

and

$$Q = \boxed{120 \,\mu\text{C}}$$

$$Q_1 = 120 \,\mu\text{C} - Q_2$$
 and  $\Delta V = \frac{Q}{C}$ 

$$\Delta V = \frac{Q}{C}$$

$$\frac{120 - Q_2}{C_1} = \frac{Q_2}{C_2}$$
 or  $\frac{120 - Q_2}{6.00} = \frac{Q_2}{3.00}$ 

$$\frac{120 - Q_2}{6.00} = \frac{Q_2}{3.00}$$

$$\begin{array}{c|c}
 & \downarrow \\
 & \downarrow \\
 & \downarrow \\
 & S_1
\end{array}$$

$$\begin{array}{c|c}
 & \downarrow \\
 & C_1 & C_2
\end{array}$$

$$(3.00)(120 - Q_2) = (6.00)Q_2$$

$$Q_2 = \frac{360}{9.00} = \boxed{40.0\,\mu\text{C}}$$

$$Q_1 = 120 \,\mu\text{C} - 40.0 \,\mu\text{C} = \boxed{80.0 \,\mu\text{C}}$$