## Faraday's law

 An emf is induced in a circuit when the magnetic flux through that circuit is changing:

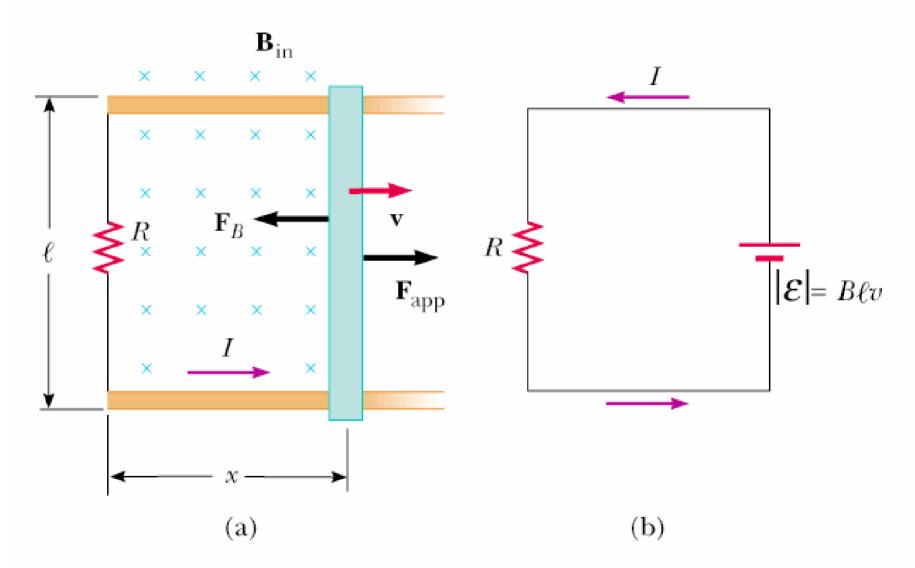
$$\varepsilon = -\frac{d\Phi_B}{dt}$$

$$\varepsilon = -\frac{d}{dt} (BA\cos\theta)$$
(1)

## Lenz's law

The polarity of the induced *emf* is such that if tends to produce a magnetic flux to oppose the change in magnetic flux through the area enclosed by the current loop

Serway, Physics for Scientists and Engineers, 5/e Figure 31.9



## Motional EMF

The magnetic flux through the circuit:

$$\Phi_B = Blx$$

• The induced motional emf

$$\varepsilon = -\frac{d\Phi_B}{dt}$$

$$= -\frac{d}{dt}(Blx) = -Bl\frac{dx}{dt}$$

$$= -Blv$$
(2)

The current in the circuit:

$$I = \frac{|\varepsilon|}{R}$$

$$= \frac{BLV}{R}$$
(3)

• Due to this current in the moving bar, it experiences a magnetic force  $(F_B)$  that opposes the motion; need to apply an equal and opposite force  $(F_{app})$  to maintain the velocity:

$$F = IlB$$

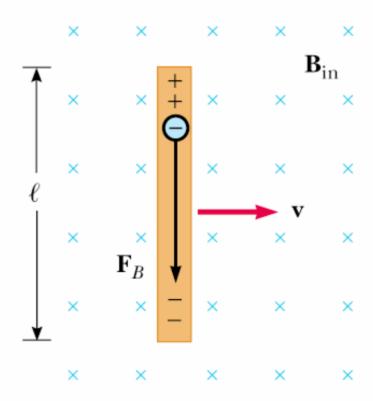
Work required to move the bar (and the associated power)

$$W = (F_{app})x = (IlB)x$$

$$P = \frac{d}{dt}W = (F_{app})v = (IlB)v = \frac{B^2l^2v^2}{R} = \frac{\varepsilon^2}{R}$$

$$(4)$$

Serway, Physics for Scientists and Engineers, 5/e Figure 31.8



Harcourt, Inc.

Serway, Physics for Scientists and Engineers, 5/e Figure 31.19

