

24. (a) We assume the flux is entirely due to the field generated by the long straight wire (which is given by Eq. 29-17). We integrate according to Eq. 30-1, not worrying about the possibility of an overall minus sign since we are asked to find the absolute value of the flux.

$$|\Phi_B| = \int_{r=b/2}^{r+b/2} \left(\frac{\mu_0 i}{2\pi r} \right) (a dr) = \frac{\mu_0 i a}{2\pi} \ln \left(\frac{r + \frac{b}{2}}{r - \frac{b}{2}} \right).$$

When $r = 1.5b$, we have

$$|\Phi_B| = \frac{(4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(4.7\text{A})(0.022\text{m})}{2\pi} \ln(2.0) = 1.4 \times 10^{-8} \text{ Wb}.$$

(b) Implementing Faraday's law involves taking a derivative of the flux in part (a), and recognizing that $\frac{dr}{dt} = v$. The magnitude of the induced emf divided by the loop resistance then gives the induced current:

$$\begin{aligned} i_{\text{loop}} &= \left| \frac{\mathcal{E}}{R} \right| = -\frac{\mu_0 i a}{2\pi R} \left| \frac{d}{dt} \ln \left(\frac{r + \frac{b}{2}}{r - \frac{b}{2}} \right) \right| = \frac{\mu_0 i a b v}{2\pi R [r^2 - (b/2)^2]} \\ &= \frac{(4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(4.7\text{A})(0.022\text{m})(0.0080\text{m})(3.2 \times 10^{-3} \text{ m/s})}{2\pi(4.0 \times 10^{-4} \Omega)[2(0.0080\text{m})^2]} \\ &= 1.0 \times 10^{-5} \text{ A}. \end{aligned}$$