



Physics 201

Professor P. Q. Hung

311B, Physics Building

Electric Charges, Forces and Fields

Summary of last lecture

- Electrostatic force between 2 point charges:

$$\vec{F}_{21} = k \frac{q_1 q_2}{r^2} \hat{r}$$

Electric Charges, Forces and Fields

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- Electric field of a point charge:

$$\vec{E}(r) = k \frac{q}{r^2} \hat{r}$$

Electric Charges, Forces and Fields

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- Electrostatic force between 2 point charges:

$$\vec{F}_{21} = k \frac{q_1 q_2}{r^2} \hat{r}$$

- Electric field of a point charge:

$$\vec{E}(r) = k \frac{q}{r^2} \hat{r}$$

- Force on a point charge q_0 in the presence of an electric field:

$$\vec{F} = q_0 \vec{E}(r)$$

Electric Charges, Forces and Fields

Question

Determine the electric field at a distance r from a line of charge of total charge Q

- A line of charge is **not** a point charge. How do we calculate the electric field then?

Electric Charges, Forces and Fields

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⇒ **Very complicated!!**

Electric Charges, Forces and Fields

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Determine the electric field at a distance r from a line of charge of total charge Q

- A line of charge is **not** a point charge. How do we calculate the electric field then?
- Try line of charge = collection of “point charges”. Calculate the electric field at a distance r from the line by the superposition of the electric fields of all the “point charges”
⇒ **Very complicated!!**
- More powerful concept using **symmetry** to solve this. Later...

Electric Charges, Forces and Fields

Electric Field Lines

The electric field is a **vector field**:

$$\vec{E}(r) = k \frac{q}{r^2} \hat{r}$$

- It points radially **outward** (from the point charge) if $q > 0$ and **inward** if $q < 0$.

Electric Charges, Forces and Fields

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- It becomes **stronger** as one gets **closer** to the point charge

Electric Charges, Forces and Fields

Electric Field Lines

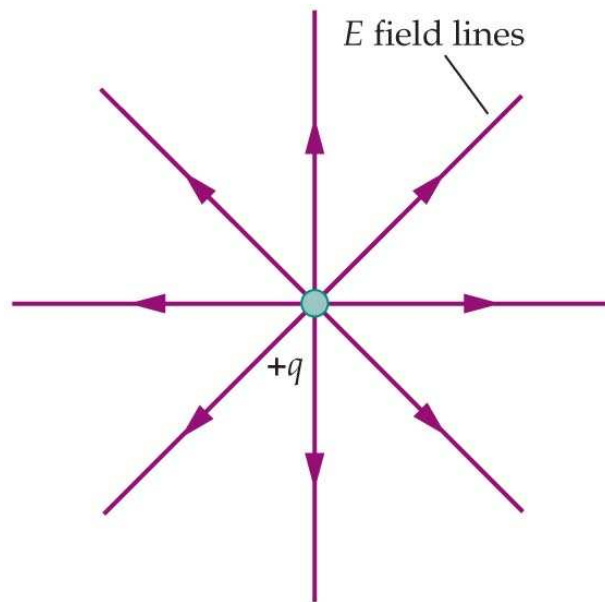
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- It becomes **stronger** as one gets **closer** to the point charge
- It depends directly on the magnitude of the point charge

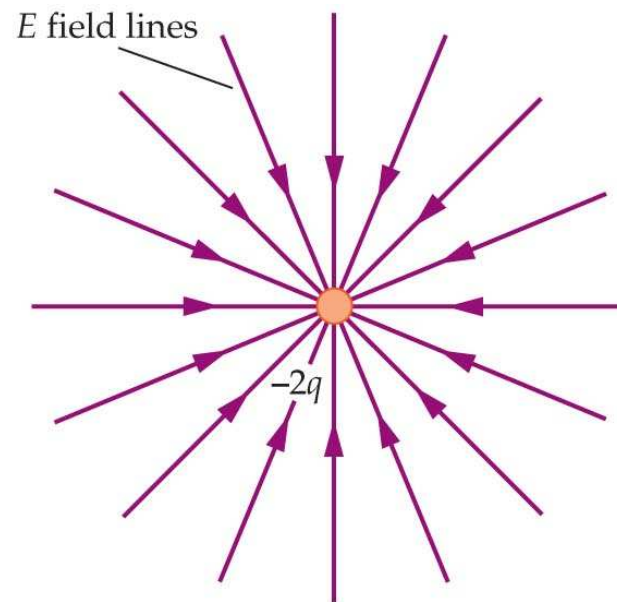
Electric Charges, Forces and Fields

Electric field of point charge: $\vec{E}(r) = k \frac{q}{r^2} \hat{r}$



(a) *E* field lines point away from positive charges

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(b) *E* field lines point toward negative charges

Electric Charges, Forces and Fields

Electric Field Lines

- Electric field lines point **away** from **positive** charges and point **into negative** charges,

Electric Charges, Forces and Fields

Electric Field Lines

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- The **density of lines** (number of lines per unit area) is **higher** at places where the electric field is **stronger**.

Electric Charges, Forces and Fields

Electric Field Lines

- Electric field lines point **away** from **positive** charges and point **into negative** charges,
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- The higher the charge is, the higher the number of lines

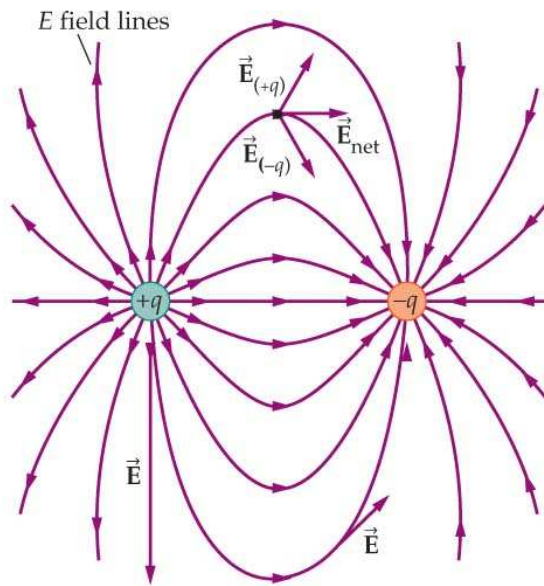
Electric Charges, Forces and Fields

Electric Field Lines

- Electric field lines point **away** from **positive** charges and point **into negative** charges,
- The **density of lines** (number of lines per unit area) is **higher** at places where the electric field is **stronger**.
- The higher the charge is, the higher the number of lines
- **No two field lines can cross each other**

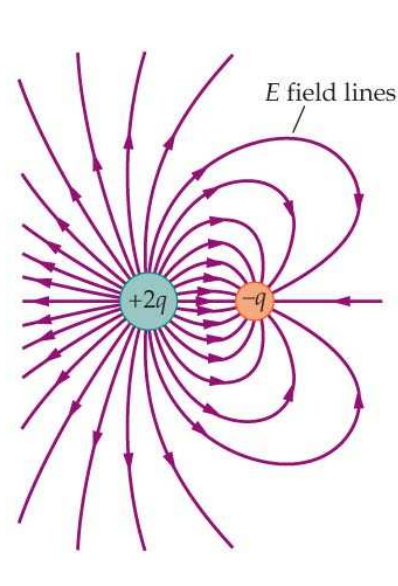
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Electric Field Lines for a system of charges

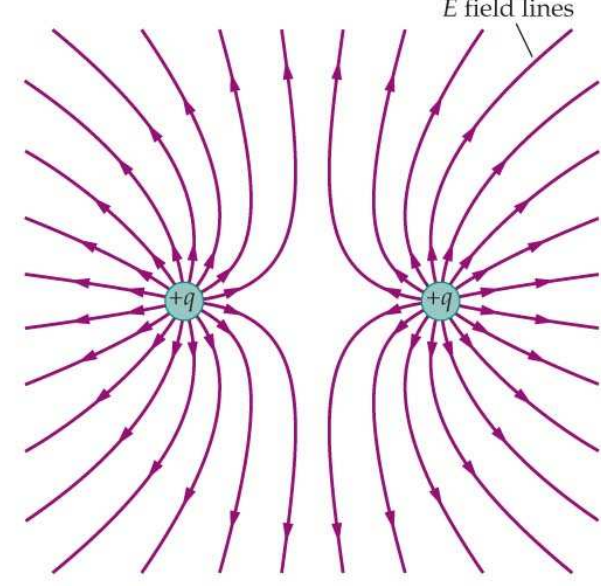


(a)

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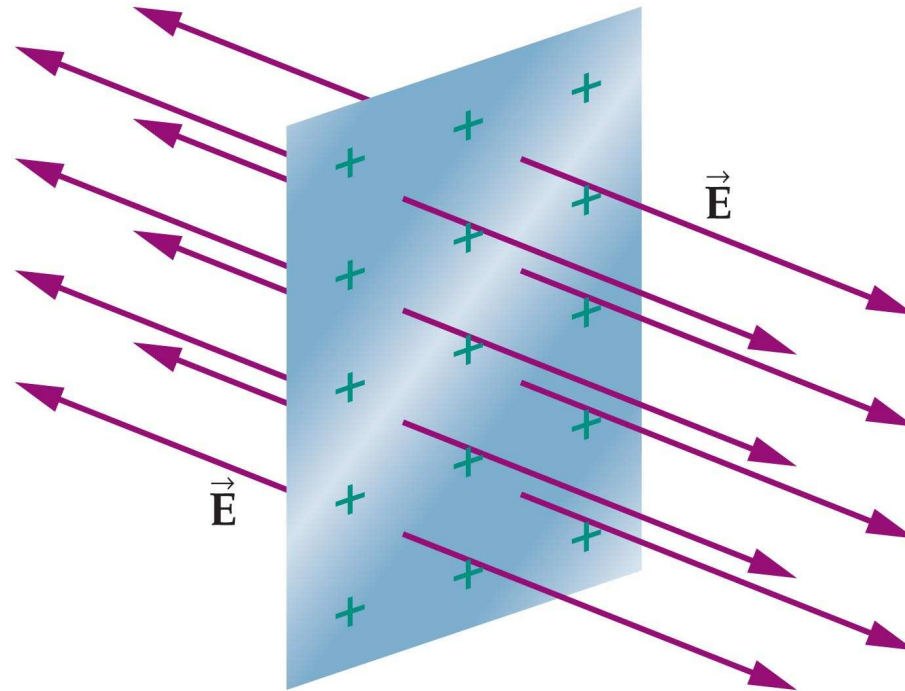
(b)



(c)

Electric Charges, Forces and Fields

Electric Field Lines for a charged plate

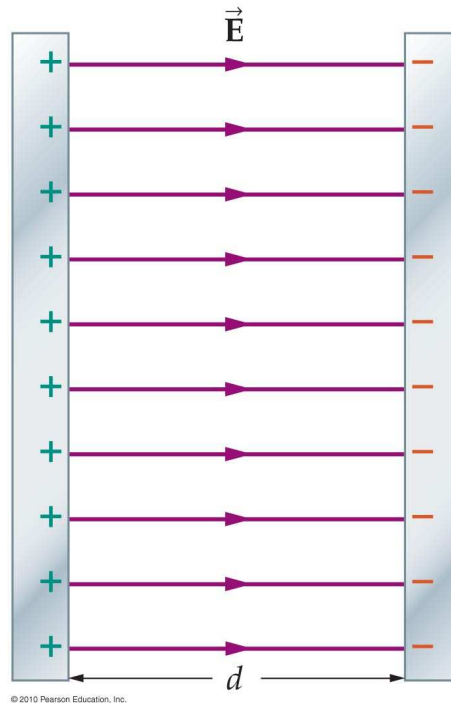


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Why is the electric field uniform?

Electric Charges, Forces and Fields

Electric Field Lines for a parallel-plate capacitor



Why is the electric field uniform between the plates and zero outside?

Electric Charges, Forces and Fields

Electric Field inside a Conductor: Concepts

- A conductor contains a number of conducting electrons which are free to move about.

Electric Charges, Forces and Fields

Electric Field inside a Conductor: Concepts

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- A conductor in **electrostatic equilibrium** has **zero electric field inside it** otherwise the conducting electrons will be free to move which brings it **out of electrostatic equilibrium**

Electric Charges, Forces and Fields

Electric Field inside a Conductor: Concepts

- A conductor contains a number of conducting electrons which are free to move about.
- A conductor in **electrostatic equilibrium** has **zero electric field inside it** otherwise the conducting electrons will be free to move which brings it **out of electrostatic equilibrium**
- In **electrostatic equilibrium**, any **excess charge** on a conductor will have to reside on its surface because the electric field is **zero** inside. We will prove this after discussing Gauss's law

Electric Charges, Forces and Fields

Electric Field inside a Conductor: Concepts

- Conductor in **electrostatic equilibrium** with an excess charge \Rightarrow the electric field is **always perpendicular** to the surface. If not, there will be a component of the electric field which is parallel to the surface \Rightarrow loss of **electrostatic equilibrium**

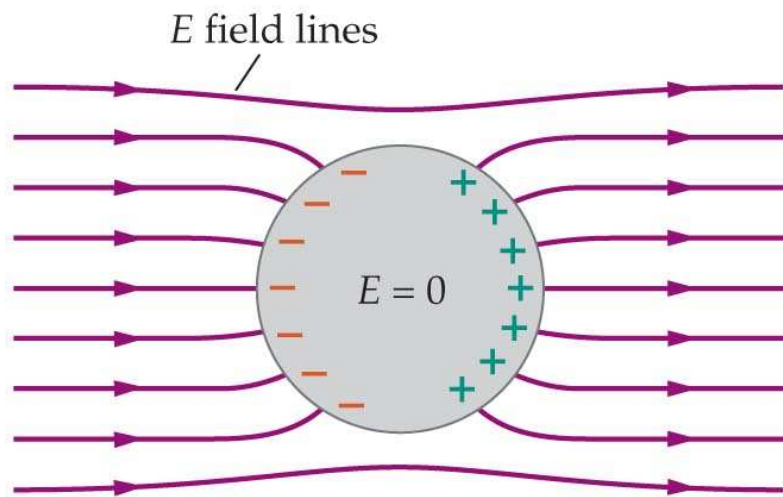
Electric Charges, Forces and Fields

Electric Field inside a Conductor: Concepts

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- An external electric field incident upon a conductor **cannot** penetrate it $\Rightarrow \vec{E} = 0$ inside. Example: Inside a **hollow** conductor \Rightarrow **Shielding**. A car is one of such example during a thunderstorm.

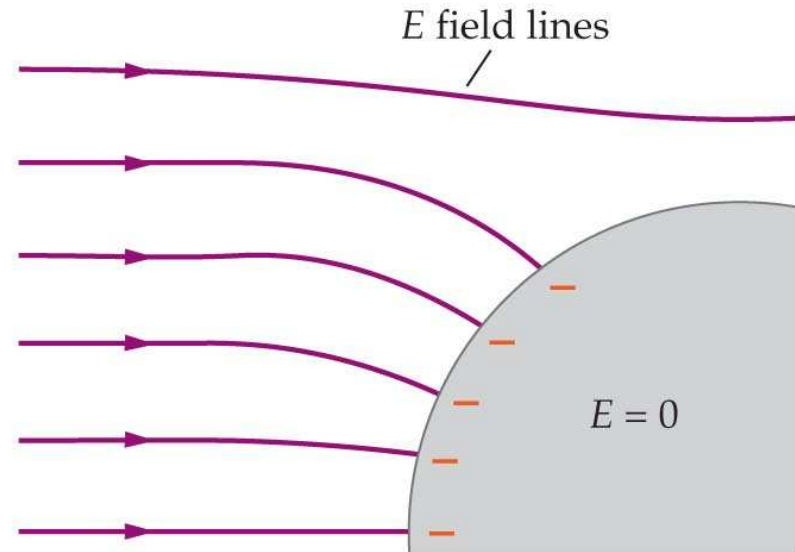
Electric Charges, Forces and Fields

Electric Field inside a Conductor: Concepts



(a) The electric field E vanishes inside a conductor

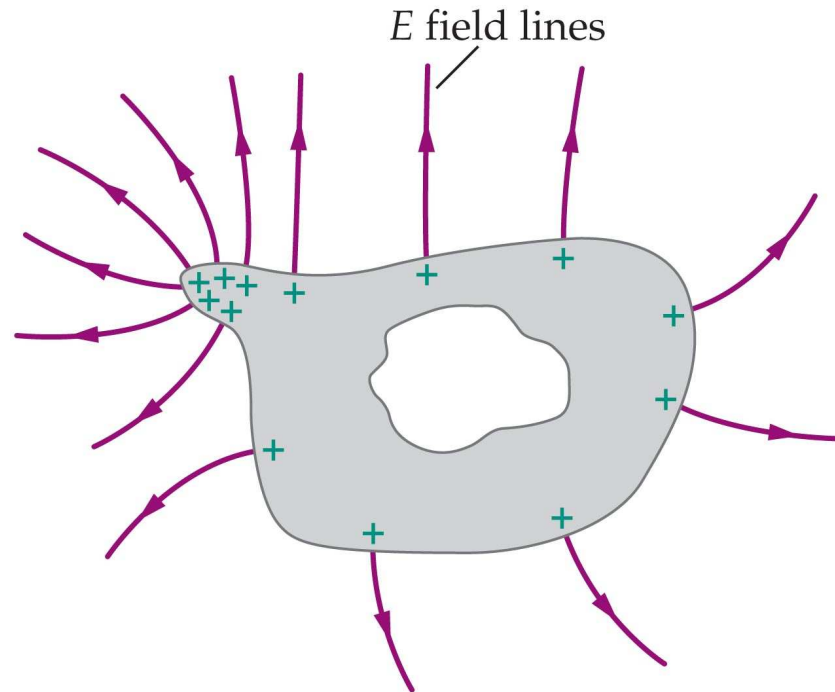
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(b) E field lines meet a conducting surface at right angles

Electric Charges, Forces and Fields

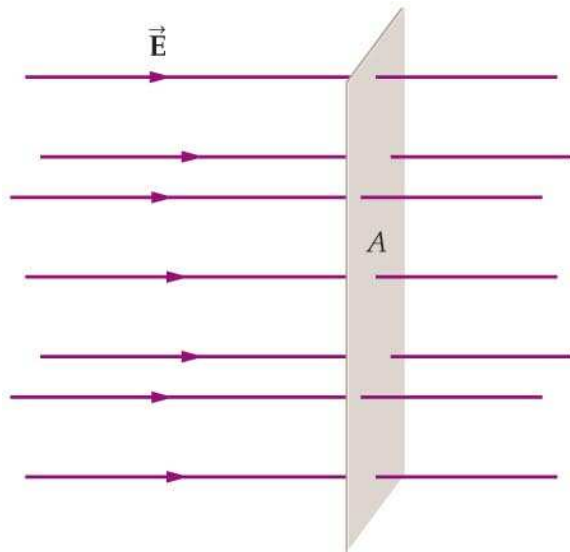
Electric Field inside a Conductor: Concepts



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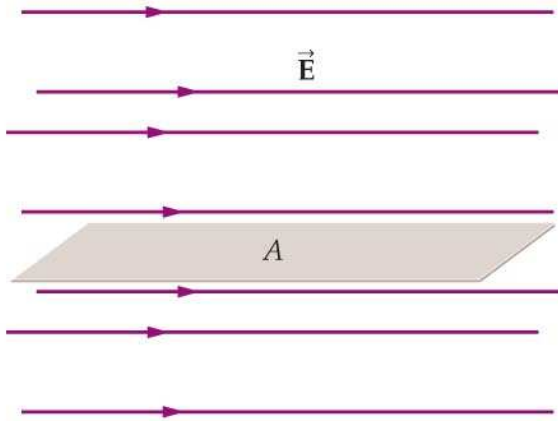
Electric Charges, Forces and Fields

Electric Flux

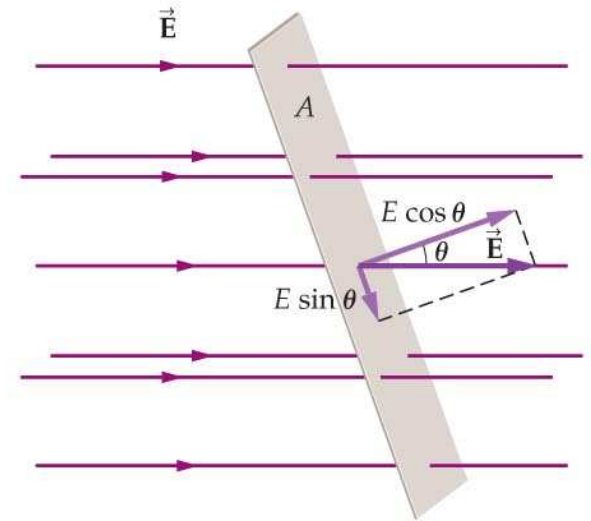


(a) Electric flux = EA

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(b) Electric flux = 0



(c) Electric flux = $(E \cos \theta)A$

Electric Flux for uniform electric field:

$$\Phi = EA \cos \theta$$

Electric Charges, Forces and Fields

Gauss's Law

The total electric flux through a surface enclosing a charge Q is

$\Phi = \frac{Q}{\epsilon_0}$ Gauss's Law for any closed arbitrary surface surrounding the point charge

$\epsilon_0 = \frac{1}{4\pi k} = 8.85 \times 10^{-12} C^2 / N.m^2$ is called the permittivity of free space.

- Under special circumstances, can one use Gauss's Law to calculate the electric field?

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- Under special circumstances, can one use Gauss's Law to calculate the electric field?
- How?

Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a point charge

- Take a point charge. Draw a (imaginary) sphere of radius r (**Gaussian surface**) with the charge at the center.

Electric Charges, Forces and Fields

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- Let the value of the electric field at a point on the surface of the sphere be $E(r)$.

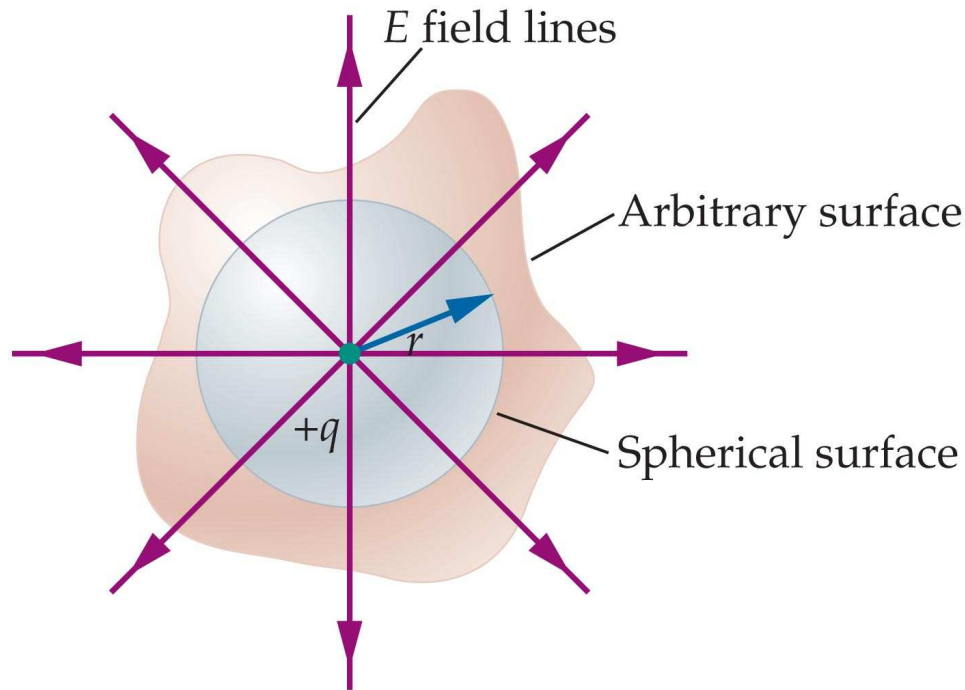
Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a point charge

- Take a point charge. Draw a (imaginary) sphere of radius r (**Gaussian surface**) with the charge at the center.
- Let the value of the electric field at a point on the surface of the sphere be $E(r)$.
- By **spherical symmetry**, the value of the electric field is the **same** at **any** other point on the surface of that sphere.

Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a point charge



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Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a point charge

- Electric flux through the surface $A = 4\pi r^2$ of the sphere of radius r :

$$\Phi = EA = E(r)(4\pi r^2) = \frac{Q}{\epsilon_0} \text{ (Last equality is Gauss's Law)}$$

Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a point charge

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$$\Phi = EA = E(r)(4\pi r^2) = \frac{Q}{\epsilon_0}$$
 (Last equality is Gauss's Law)
- $E(r) = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} = k \frac{Q}{r^2}$ Same as Coulomb's Law.

Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a line of charge with total charge Q

- Find E at a distance r from the line of charge.
Problem 19.70.

Electric Charges, Forces and Fields

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- Calculate the electric flux through a Gaussian surface of radius r .

Electric Charges, Forces and Fields

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- What kind of Gaussian surface?

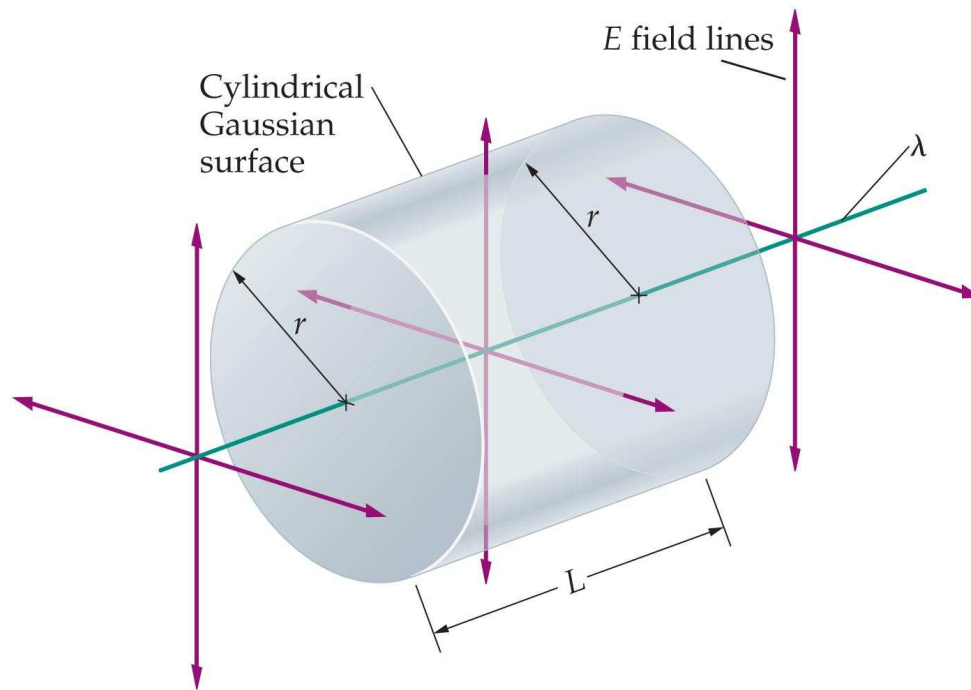
Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a line of charge with total charge Q

- Find E at a distance r from the line of charge.
Problem 19.70.
- Calculate the electric flux through a Gaussian surface of radius r .
- What kind of Gaussian surface?
- What symmetry gives a constant electric field on the Gaussian surface?

Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a line of charge with total charge Q



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Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a line of charge with total charge Q

- The Gaussian surface would be a **cylinder** of radius r and length l . The area of the cylinder (minus the 2 ends) is $A = 2\pi r l$

Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a line of charge with total charge Q

- The Gaussian surface would be a **cylinder** of radius r and length l . The area of the cylinder (minus the 2 ends) is $A = 2\pi r l$
- Why? Because the problem has **cylindrical symmetry**. The value of the electric field would be the **same** at **any point** on the surface of that imaginary cylinder.

Electric Charges, Forces and Fields

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- Why? Because the problem has **cylindrical symmetry**. The value of the electric field would be the **same** at **any point** on the surface of that imaginary cylinder.
- Gauss's Law: $\Phi = EA = E(2\pi r l) = \frac{Q}{\epsilon_0}$

Electric Charges, Forces and Fields

Gauss's Law: How to get the electric field of a line of charge with total charge Q

$$\bullet E = \frac{Q}{2\pi r l \epsilon_0} = \frac{\lambda}{2\pi r \epsilon_0}$$

where

$\lambda = \frac{Q}{l}$ is the **linear charge density**.

Electric Charges, Forces and Fields

What is the most important thing that we learned in this lecture? Gauss's Law

The total electric flux through a surface enclosing a charge Q is

$$\Phi = \frac{Q}{\epsilon_0}$$

Gauss's Law for any closed arbitrary surface surrounding the point charge