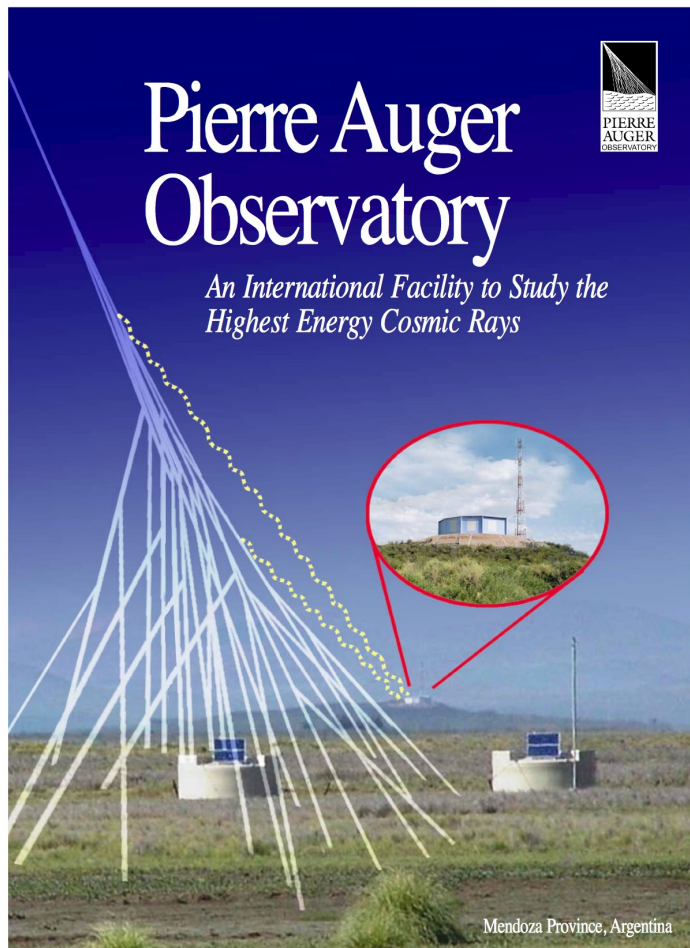




Ultra High Energy Cosmic Rays

and_

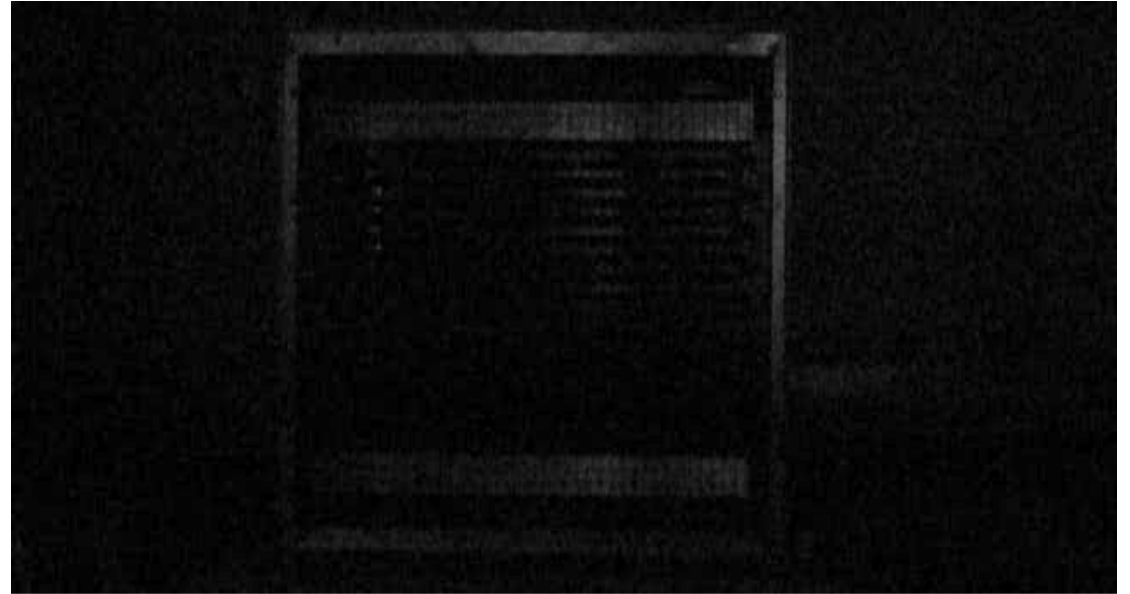
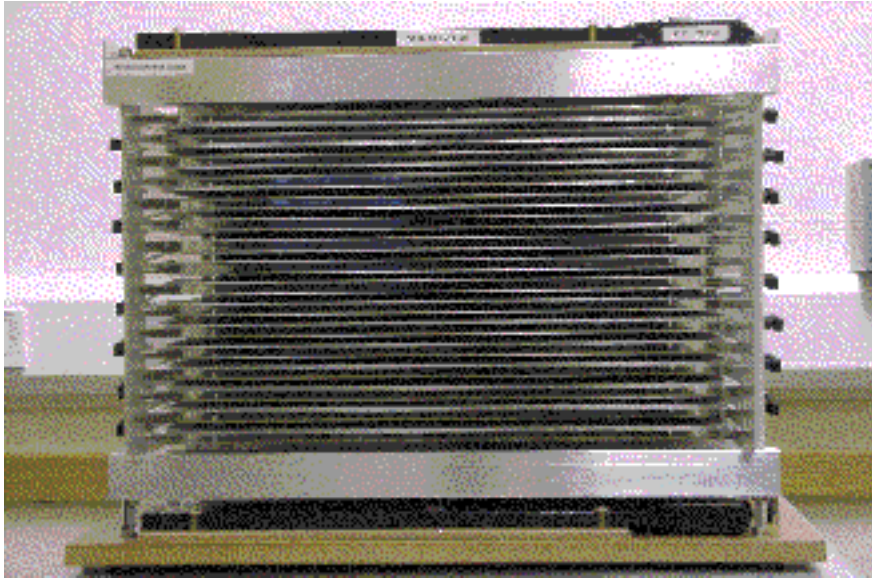
The Pierre Auger Observatory



Paolo Privitera



Cosmic Rays are always with us

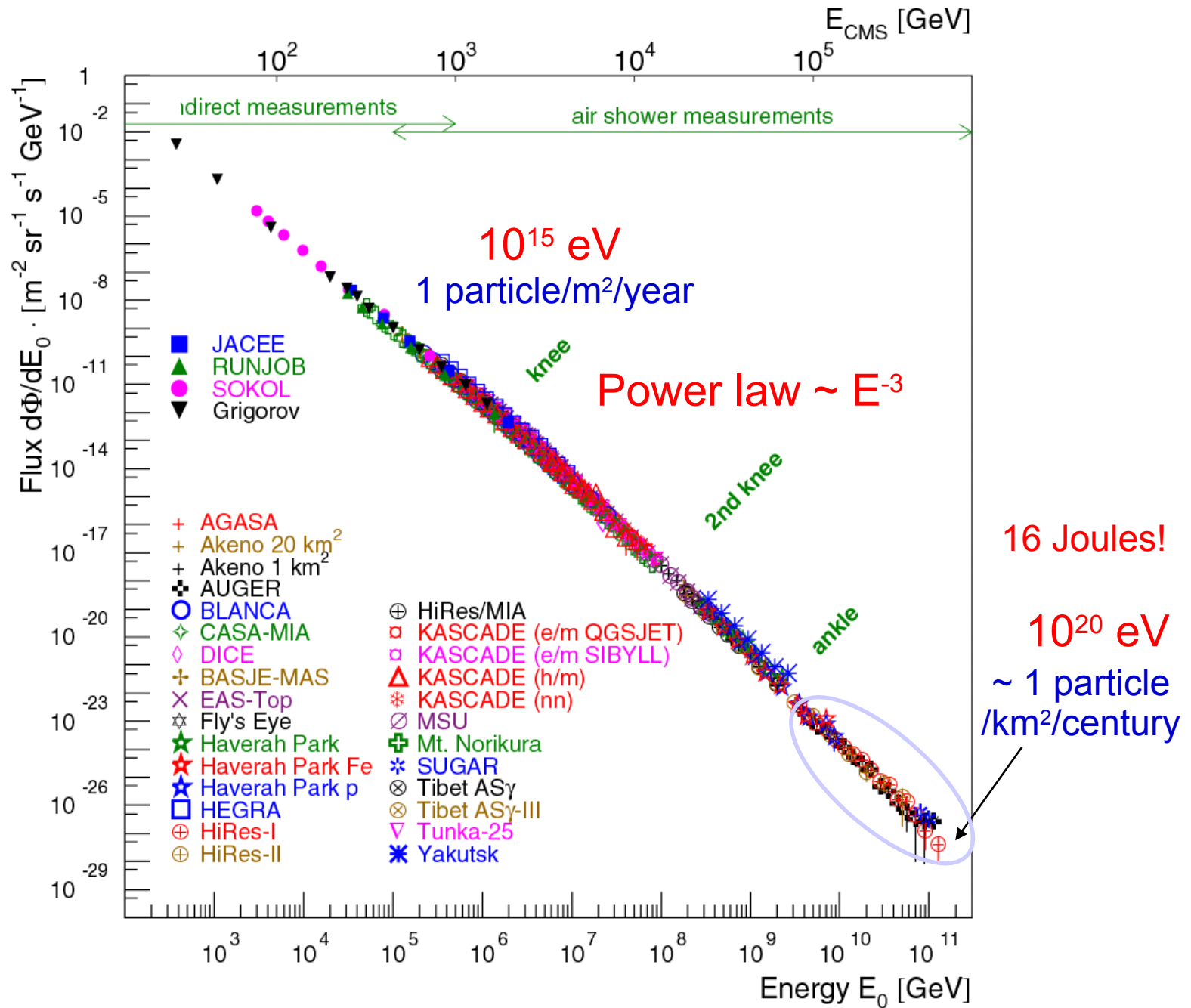


A particle detector: the Spark Chamber
(courtesy University of Birmingham)

Rate of cosmic rays at ground $\approx 1 / \text{cm}^2 / \text{minute}$

Typical cosmic ray energy 1 GeV

Ultra High Energy Cosmic Rays



Amazing energies?



Ultra High Energy Cosmic Ray

$$10^{20} \text{ eV} = 16 \text{ Joule !!!}$$

$$\text{Energy/mass} = 10^{28} \text{ J/kg}$$

$$\text{Energy/size} = 10^{31} \text{ J/cm}^2$$

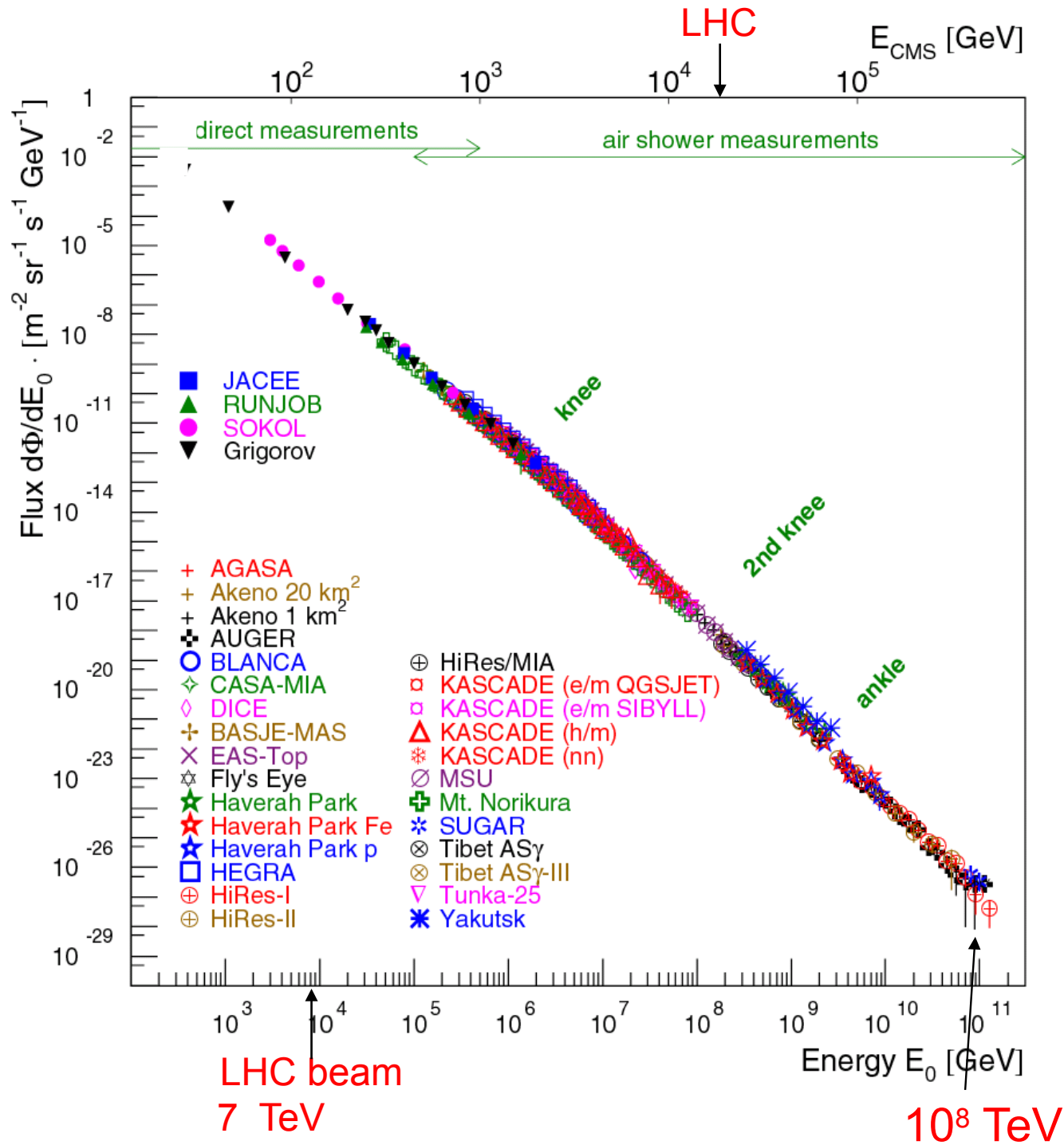
Sicilian cannolo:

$$300 \text{ Cal} = 1.2 \text{ MJoule !!!}$$

$$\text{Energy/mass} = 10^7 \text{ J/kg}$$

$$\text{Energy/size} = 10^4 \text{ J/cm}^2$$

UHECR VS LHC



$$E_{CMS}(UHECR) \approx \sqrt{2 m_p E_p}$$

$$= \sqrt{2 \cdot 10^9 \cdot 10^{20}} \approx 4.4 \cdot 10^{14} \text{ eV}$$

$$= 440 \text{ TeV}$$

$$E_{CMS}(LHC) = 14 \text{ TeV}$$

UHECR vs LHC



Proton pizza



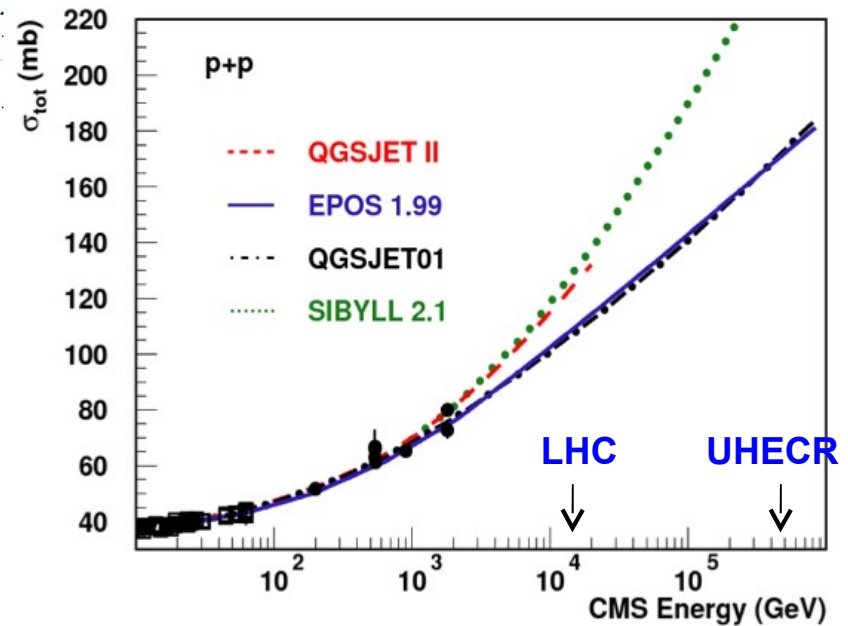
Air pizza

(Courtesy of F. Le Diberder)

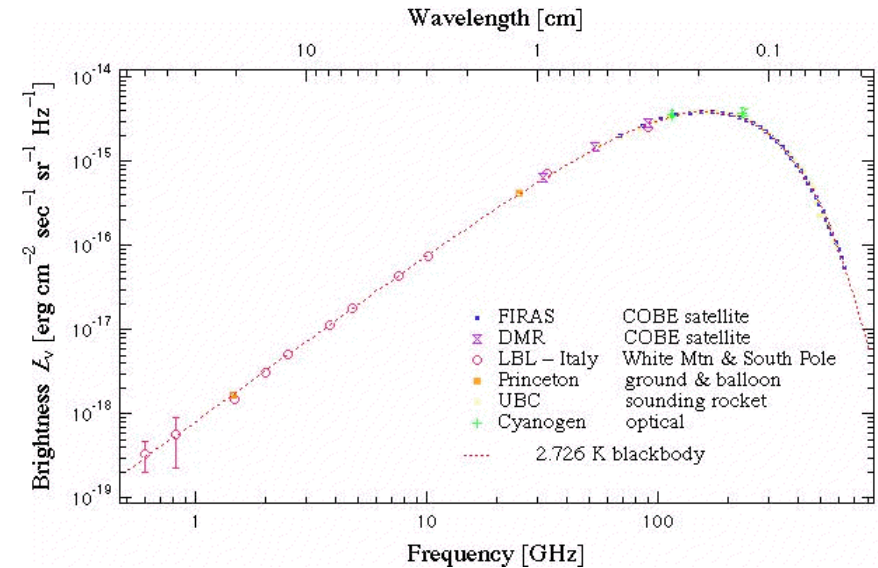
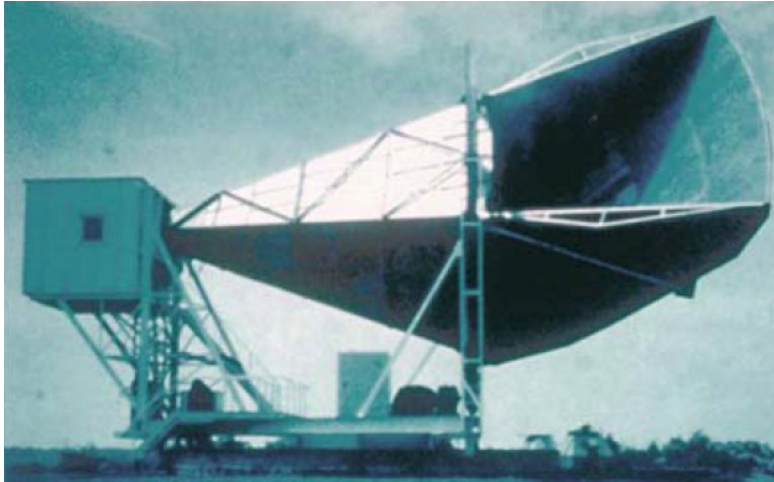
Measurement of the p-p cross section, a fundamental quantity in particle physics

UHECR allow to explore “pizza-pizza” interactions (underlying events, minimum bias events) way above LHC energy.

NOTE: too few events to study Higgs, supersimmetry, etc.



UHECR and Cosmology



Penzias and Wilson discovery of Cosmic Microwave Background (1965)

END TO THE COSMIC-RAY SPECTRUM?

Kenneth Greisen

Cornell University, Ithaca, New York
(Received 1 April 1966)

This note predicts that above 10^{20} eV the primary spectrum will steepen abruptly, and the experiments in preparation will at last observe it to have a cosmologically meaningful termination.

The Greisen-Zatsepin-Kusmin "cutoff"

A definite prediction:
strong suppression of the flux

The Greisen-Zatsepin-Kusmin “cut-off”



$$s = m_p^2 + 2 E_p \epsilon_\gamma (1 - \beta \cos \vartheta) \sim m_p^2 + 4 E_p \epsilon_\gamma$$

$$\geq (m_p + m_\pi)^2 \quad \text{AT THRESHOLD}$$

$$\Rightarrow E_p \geq \frac{m_\pi (m_\pi + 2m_p)}{4 \epsilon_\gamma} \approx 7 \cdot 10^{19} \text{ eV}$$

$\epsilon_\gamma \sim 10^{-3} \text{ eV}$

INTERACTION
LENGTH

$$L = \left(\sigma \rho_\gamma \right)^{-1} \approx 6 \text{ Mpc}$$

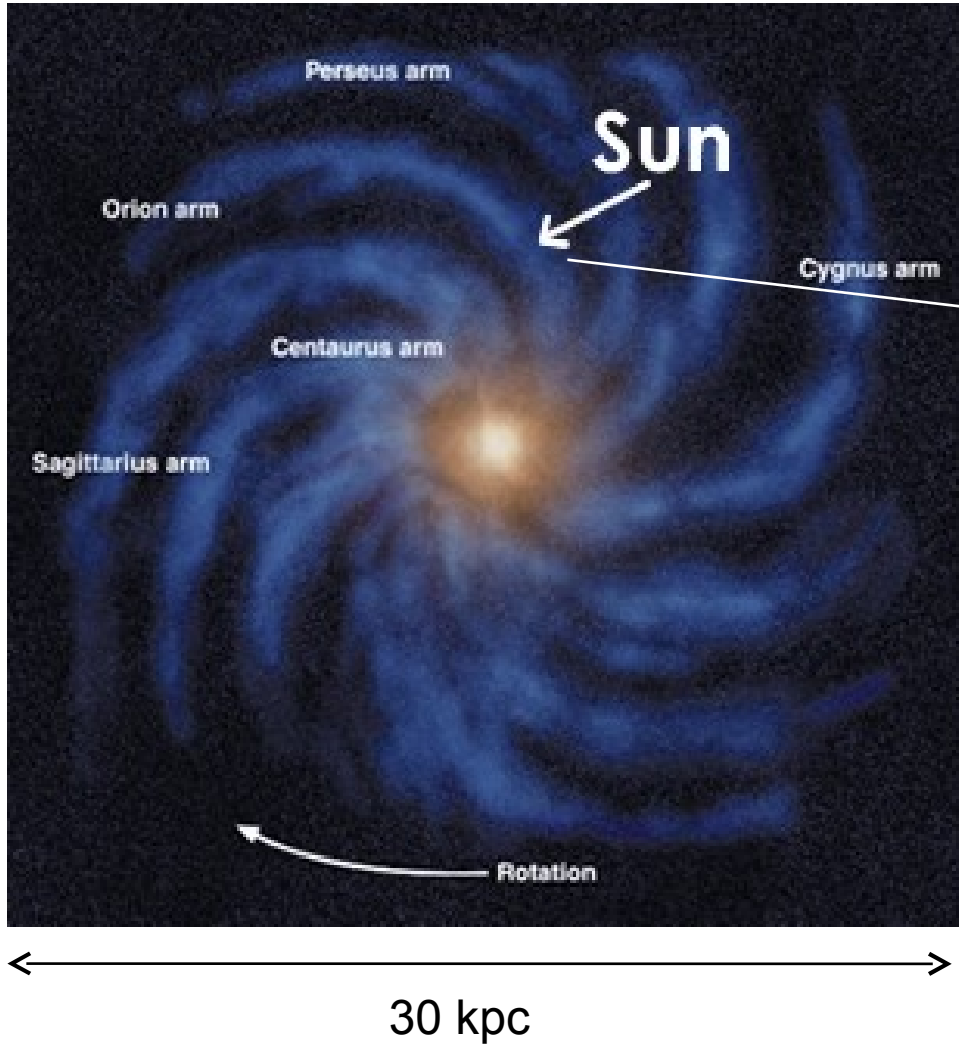
$\sigma \rightarrow 130 \mu\text{b}$ $\rho_\gamma \rightarrow \frac{400}{\text{cm}^3}$

$$1 \text{ b} = 10^{-24} \text{ cm}^2$$

$$1 \text{ pc} = 3.26 \text{ light years} \approx 10^{18} \text{ cm}$$

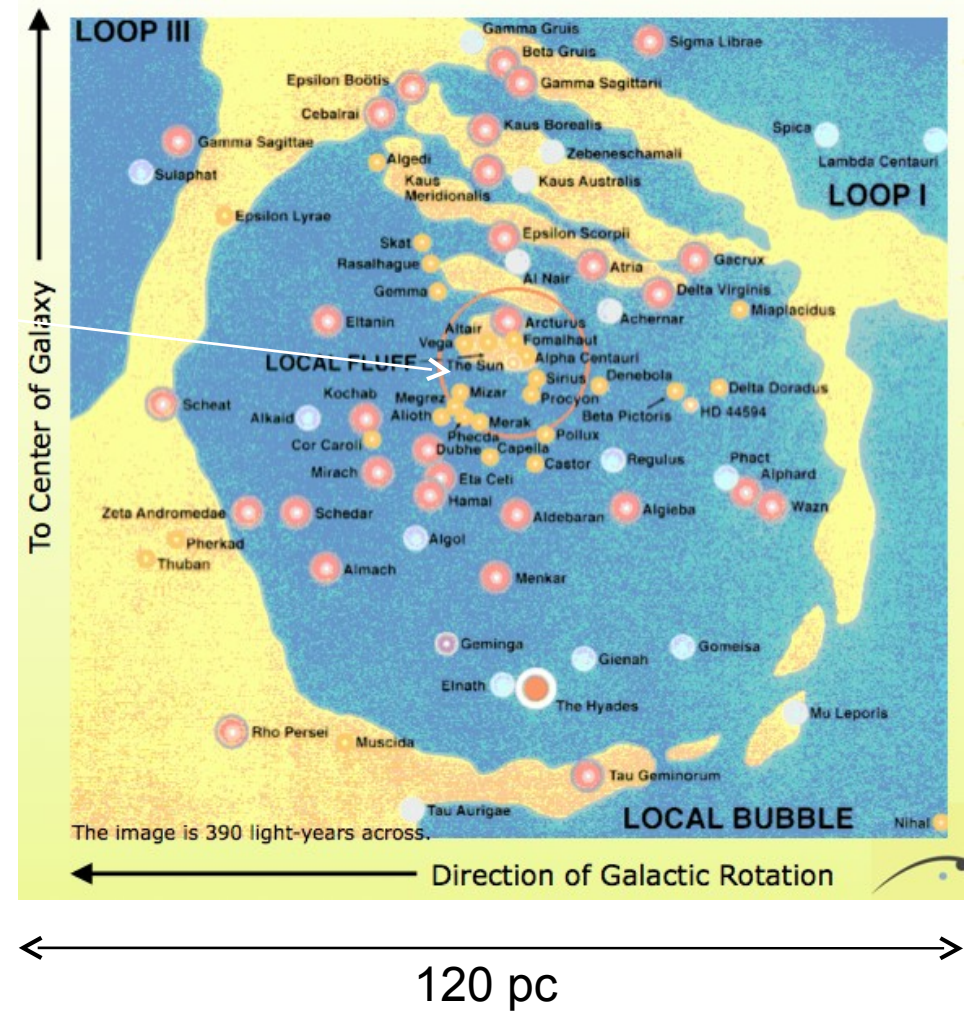
Astronomical distances

The Milky Way



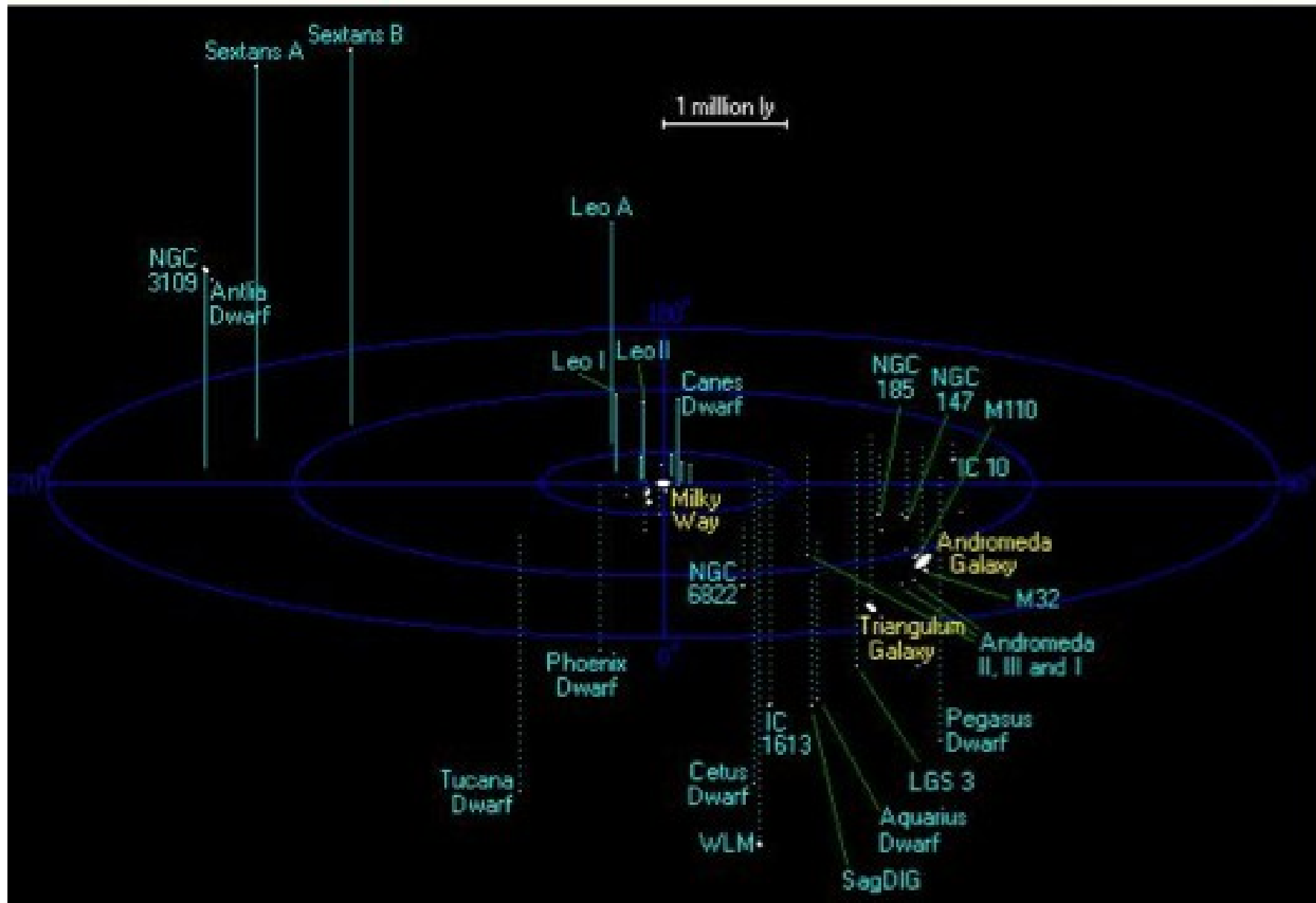
Distance Sun to center of Milky way 8 kpc

The Solar neighborhood



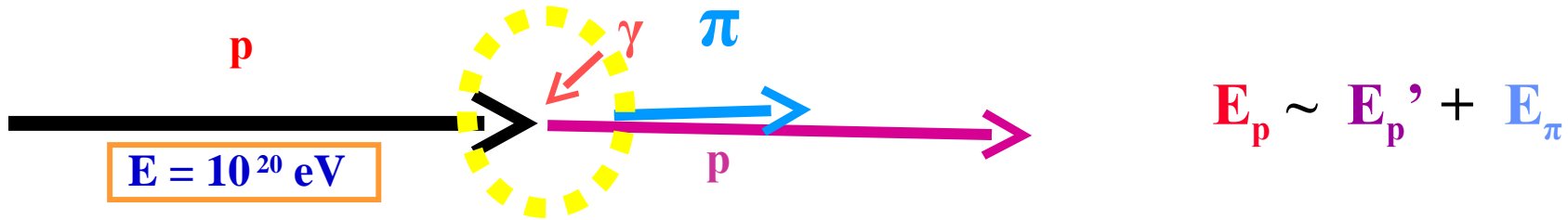
Distance earth to Alpha Centauri 1.3 pc

Local group of galaxies



← 2 Mpc →

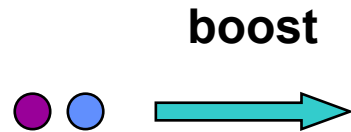
The Greisen-Zatsepin-Kusmin “cut-off”



$$E_p - E_p' = \Delta E_p = E_\pi$$

$$\frac{\Delta E_p}{E_p} = \frac{E_\pi}{E_p}$$

at threshold



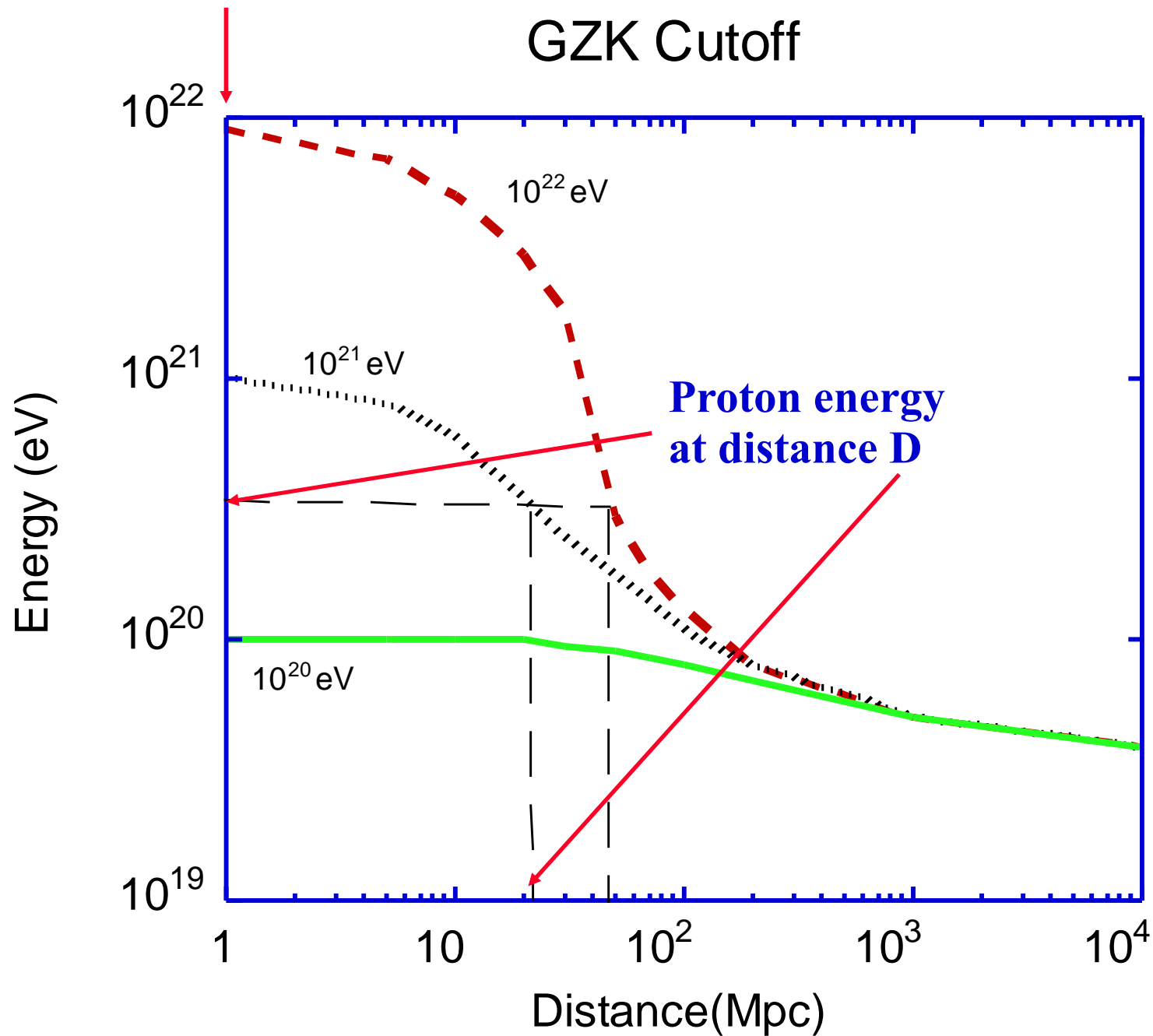
$$\gamma_{\text{Lab}} = \frac{E_p}{(m_p + m_\pi)}$$

$$E_\pi = \gamma_{\text{Lab}} m_\pi = \frac{E_p m_\pi}{(m_p + m_\pi)}$$

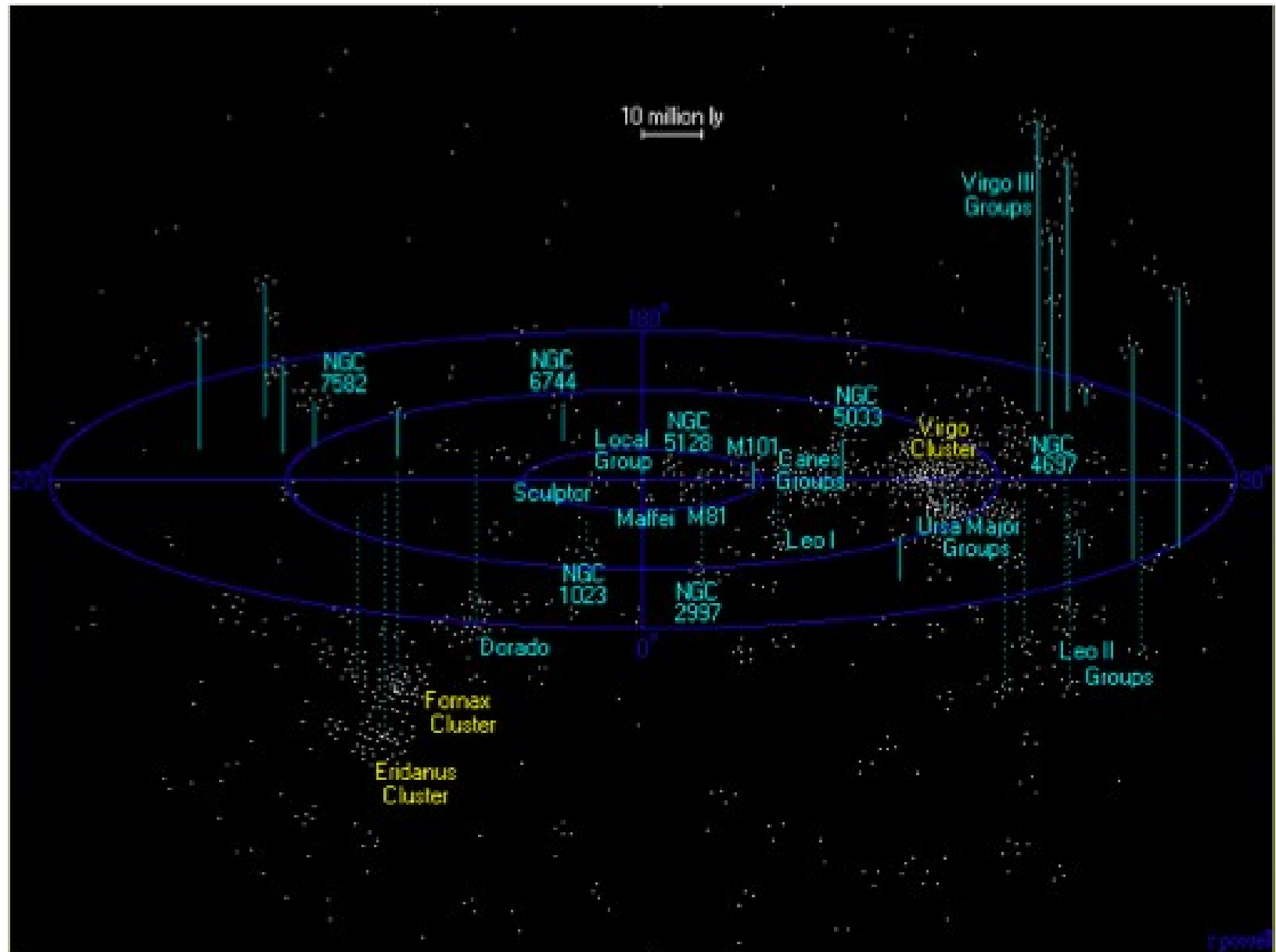
$$\frac{\Delta E_p}{E_p} \sim \frac{m_\pi}{m_p + m_\pi} \sim 15\%$$

**Proton energy
at the source**

**UHECR source must be closer than 50-
100 Mpc!**



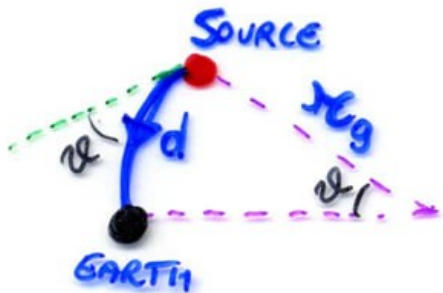
Local supercluster



← 40 Mpc →

Can we find their origin?

* ARRIVAL DIRECTION



$$\psi \sim \frac{d}{r_g}$$

$$r_g \sim \frac{E}{ZeB}$$

$$\Rightarrow \psi_d \approx 0,5^\circ \cdot Z \cdot \left(\frac{E}{10^{20} \text{ eV}} \right)^{-1} \cdot \left(\frac{d}{1 \text{ Mpc}} \right) \cdot \left(\frac{B}{10^{-9} \text{ G}} \right)$$

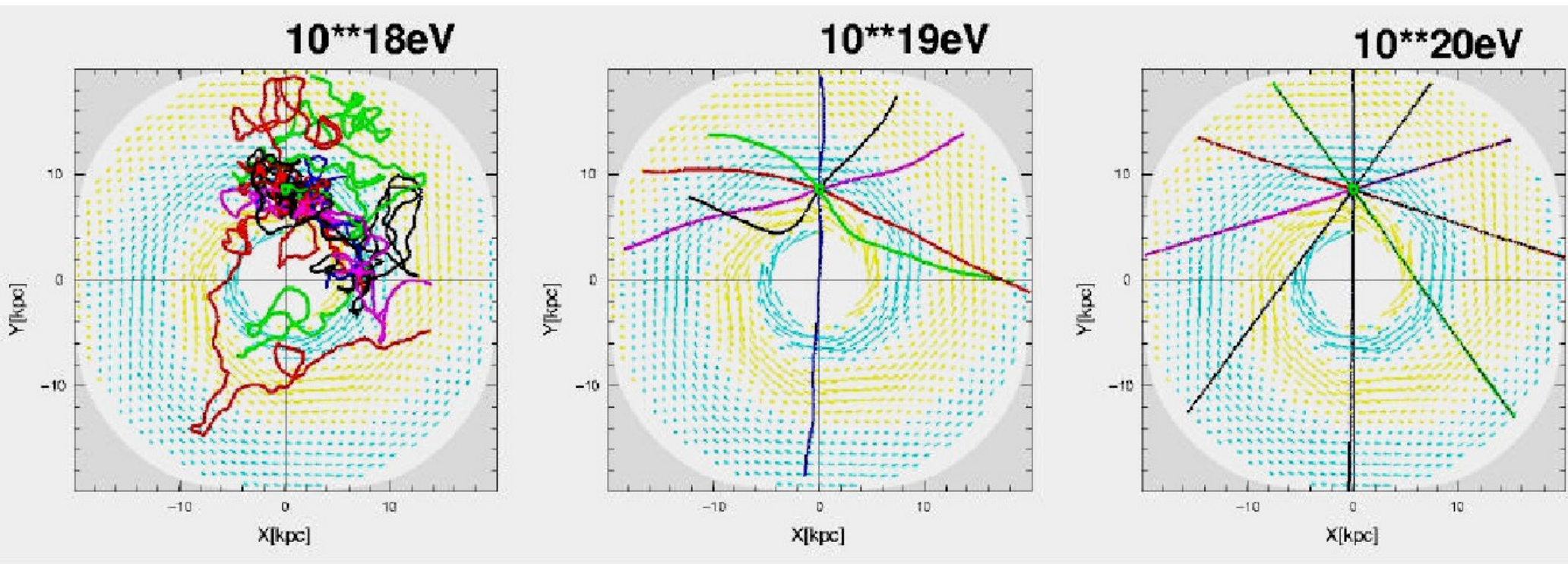
Ex: PROTON FROM THE GALACTIC CENTER

$$E = 3 \cdot 10^{20} \text{ eV}, \quad d = 8,5 \text{ Kpc}, \quad B = 2 \mu\text{G}$$

$$\Rightarrow \psi \sim 3^\circ$$

- **Galactic magnetic fields:**

A 10^{20} eV proton is almost not deflected in the galactic magnetic field (μG)



Can we find their origin?



$$\sigma_{\varphi}(d) \approx \sqrt{N} \varphi_{\lambda} \approx \sqrt{\frac{d}{\lambda}} \cdot \frac{\lambda}{r_g} = \sqrt{d} \sqrt{\lambda} \frac{1}{r_g}$$

$$\approx 0,8^{\circ} \cdot Z \cdot \left(\frac{E}{10^{20} \text{eV}}\right)^{-1} \cdot \left(\frac{d}{10 \text{Mpc}}\right)^{\frac{1}{2}} \cdot \left(\frac{\lambda}{1 \text{Mpc}}\right)^{\frac{1}{2}} \cdot \left(\frac{B}{10^{-9} \text{G}}\right)$$

Ex: $\rho, d = 50 \text{ Mpc}$

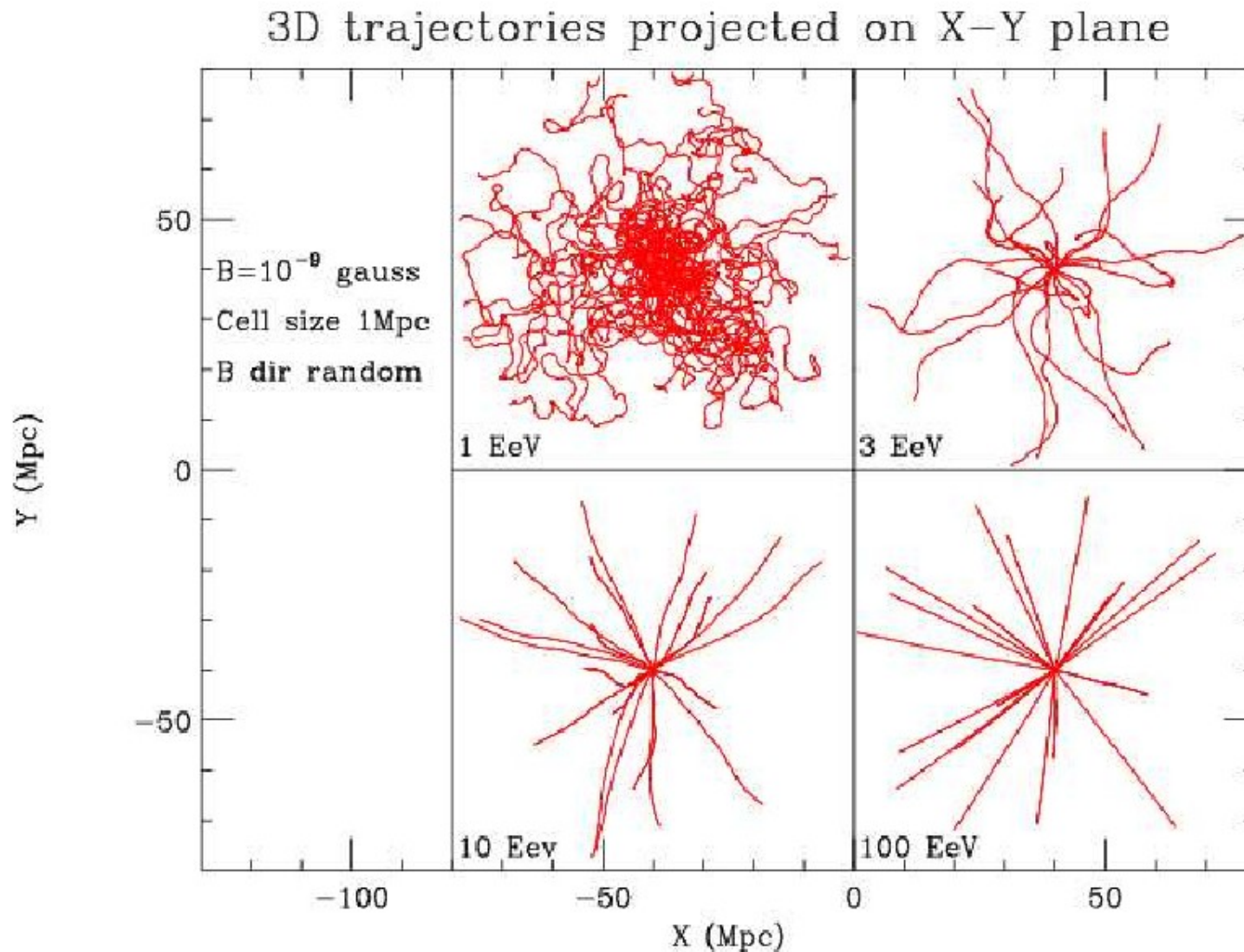
$\lambda = 1 \text{ Mpc}, B = 1 \text{ mG}$



$\sigma_{\varphi} \sim 0,6^{\circ}$

- **Inter-Galactic magnetic fields:**

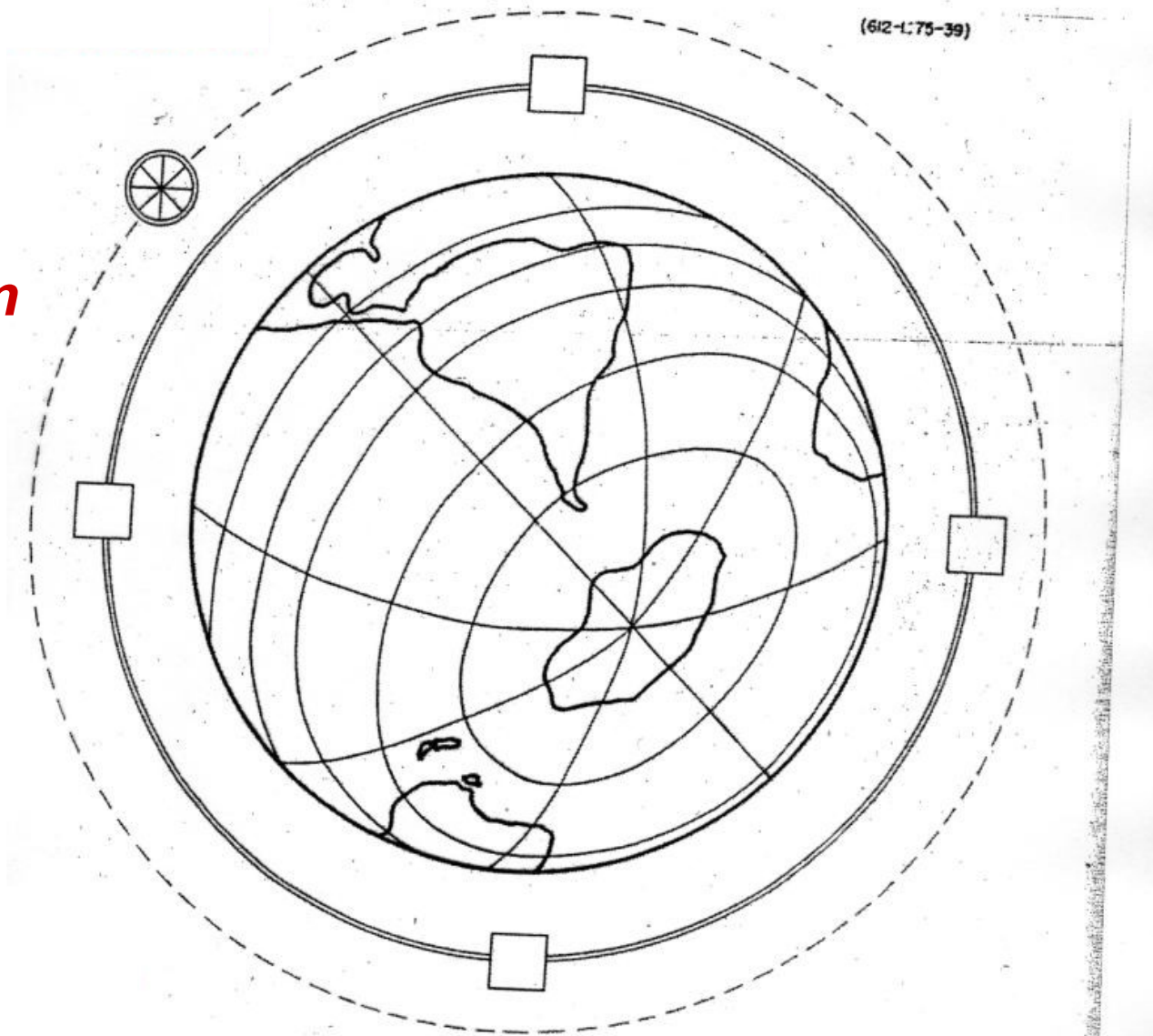
A 10^{20} eV proton is almost not deflected in the inter-galactic magnetic field (nG)



1 EeV = 10^{18} eV

10²⁰ eV accelerator?

Fermi's
Globalatron



American Physical
Society 1954

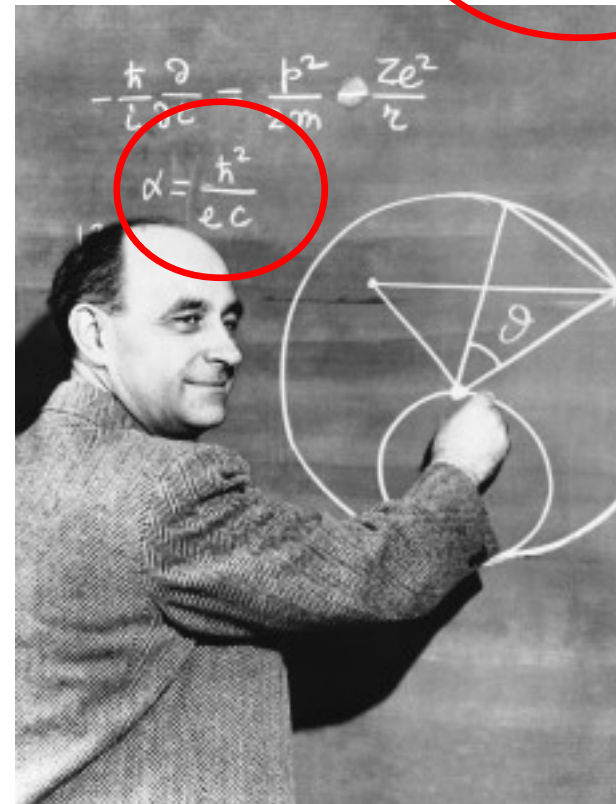
5 10¹⁵ eV

Enrico Fermi

(1901 Rome – 1954 Chicago)



$$\alpha = \frac{e^2}{\hbar c} !$$



Chain reaction, the first atomic pile, theory of beta decay, Fermions, Fermilab,

On the Origin of the Cosmic Radiation

ENRICO FERMI

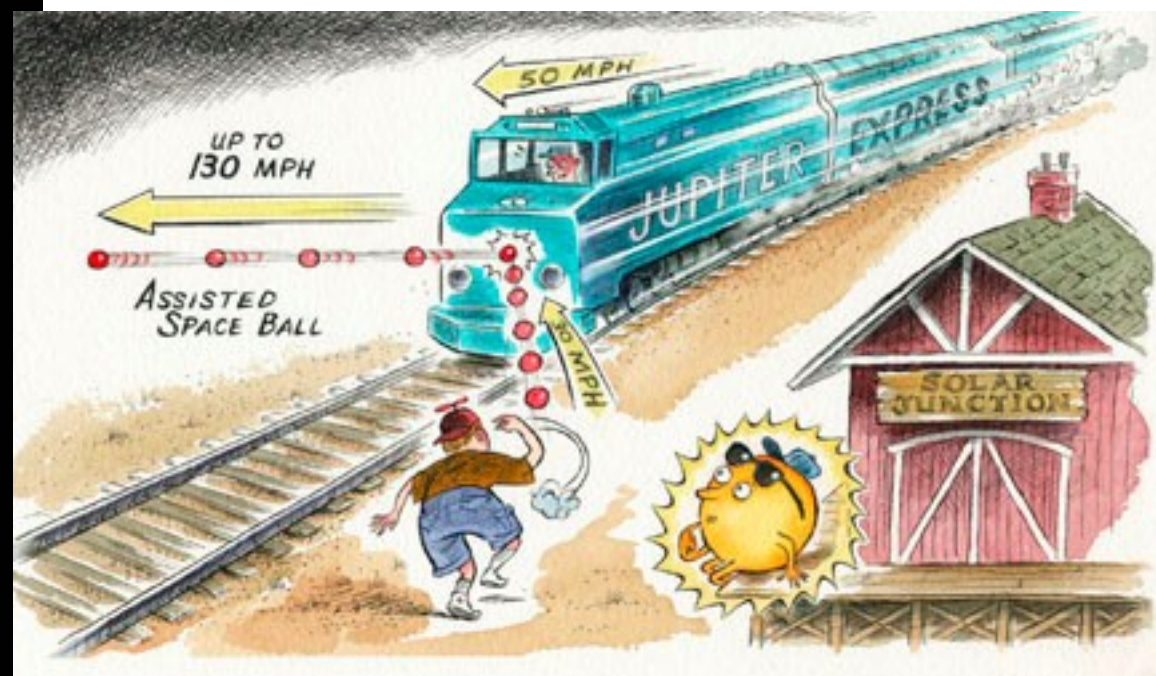
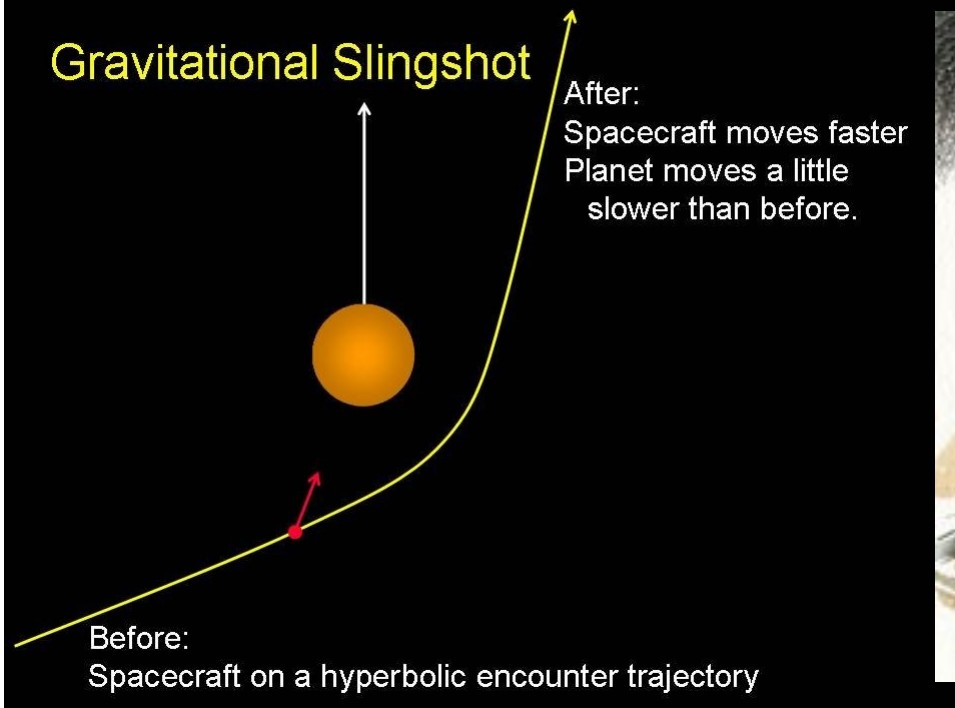
Institute for Nuclear Studies, University of Chicago, Chicago, Illinois

(Received January 3, 1949)

A theory of the origin of cosmic radiation is proposed according to which cosmic rays are originated and accelerated primarily in the interstellar space of the galaxy by collisions against moving magnetic fields. One of the features of the theory is that it yields naturally an inverse power law for the spectral distribution of the cosmic rays. The chief difficulty is that it fails to explain in a straightforward way the heavy nuclei observed in the primary radiation.

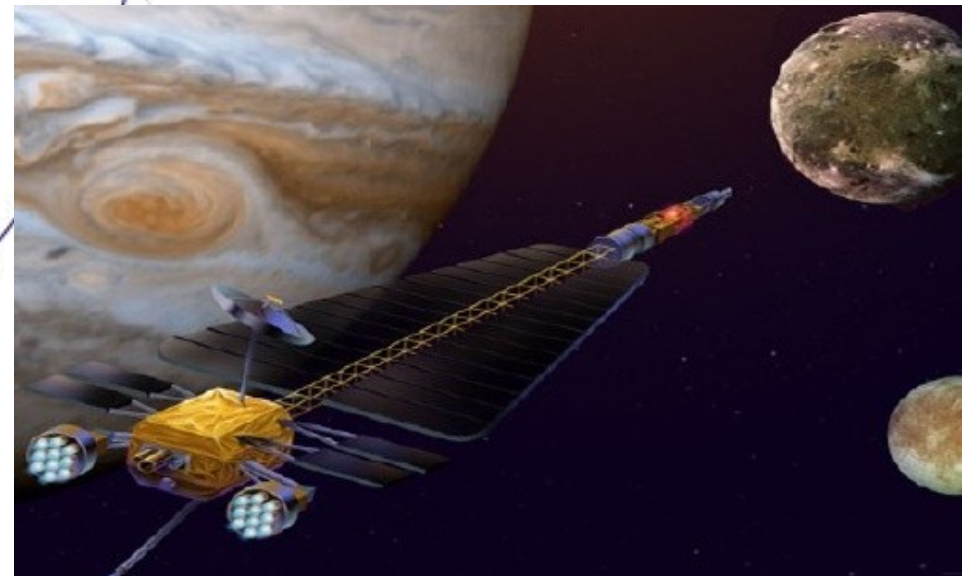
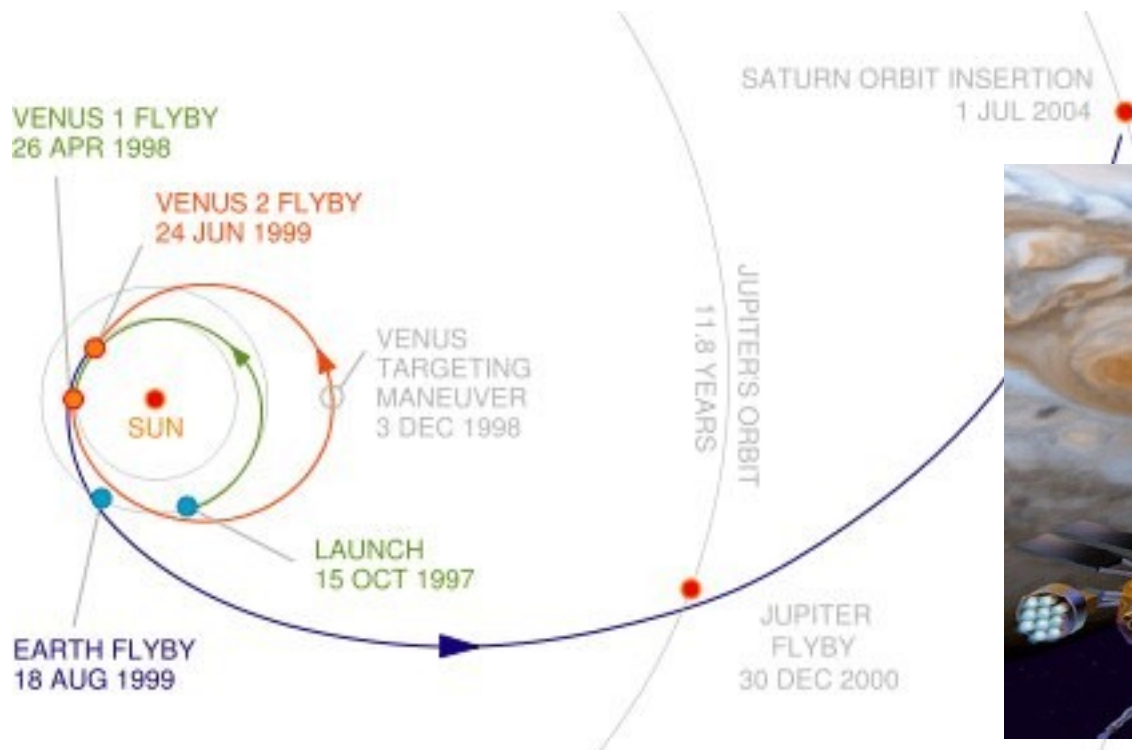


Gravitational Slingshot



Gravity assist

Cassini



Dec 4 1948

Saturday!

137

Theory of cosmic rays

a) Energy acquired in collisions against cosmic magnetic fields



Non relativistic case

$$M V^2$$

(M = mass of particle V = velocity of moving field)

Proof: Head on collision gives energy gain

$$\frac{M}{2} (v + 2V)^2 - \frac{M v^2}{2} = \frac{M}{2} (4vV + 4V^2) =$$

$$= M(2vV + 2V^2) \quad \text{Prob} = \frac{v+V}{2v}$$

Running after collision (prob = $\frac{v-V}{2v}$) gives energy gain $M(-2vV + 2V^2)$

Average gain order

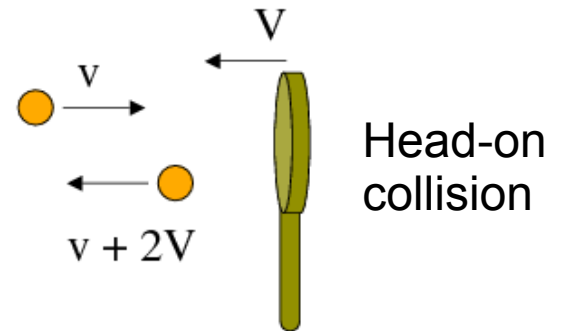
$$M V^2$$

Relativistic: order

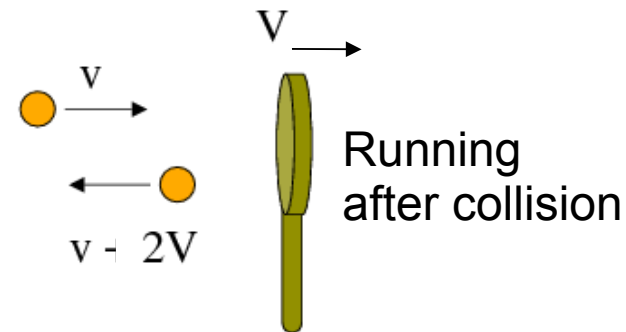
$$\omega \beta^2$$

Fermi's notebook

University of Chicago Library
Special Collections



Frequency of collisions
≈ relative velocity



$$\beta = \frac{\text{Velocity of B field cloud}}{c}$$

Notations

Absorption mean free path $\Lambda = 10^{26}$ cm

Absorption time $T = 3 \times 10^{15}$ years

Scattering mean free path λ

Scattering " " time τ

Time-energy relationship

$$w = Mc^2 e^{\frac{t}{T}\beta^2}$$

$$\beta = \frac{v}{c} \approx 10^{-4}$$

$$t = \frac{\tau}{\beta^2} \log \frac{w}{Mc^2}$$

Prob. distribution in ~~time~~ age

$$e^{-\frac{t}{T}} \frac{dt}{T} = \text{prob of age } t$$

$$= -d e^{-\frac{t}{T}}$$

$$e^{-\frac{t}{T}} = \left(\frac{Mc^2}{w}\right)^{\frac{\tau}{T\beta^2}}$$

$$\text{prob} = \frac{\tau (Mc^2)^{\tau/T\beta^2}}{T\beta^2} \frac{dw}{w^{1+\frac{\tau}{T\beta^2}}}$$

Power law!

Follows

$$1 + \frac{\tau}{T\beta^2} = 2.9$$

$$\frac{\tau}{T\beta^2} = 1.9$$

Fermi's notebook

University of Chicago Library
Special Collections

The measured spectral index gives information on absorption and scattering

Hence

$$\tau = 1.9 \beta^3 T = 1.9 \times 10^{-8} \times 3 \times 10^{15} = 6 \times 10^7$$

$$\lambda = 2 \text{ light years!}$$

Why are there no electrons?

Radiation loss is per second

$$\frac{2}{3} \frac{e^2}{c^3} A^2 \frac{1 - \sin^2 \epsilon \frac{v^2}{c^2}}{\left(1 - \frac{v^2}{c^2}\right)^3} = \text{since for magnetic acceleration}$$

$$\sin \epsilon = 1$$

$$= \frac{2}{3} \frac{e^2}{c^3} \frac{c^4}{R^2} \frac{\omega^4}{m^4 c^8} \quad HR = \frac{\omega}{e}$$

$$\Rightarrow = \frac{2}{3} \frac{e^2}{c^3} \frac{\omega^4}{m^4 c^8} \frac{H^2 e^2}{\omega^2} = \frac{2}{3} \frac{e^4 H^2}{m^4 c^7} \omega^{-2}$$

Energy is gained at rate

$$\frac{\beta^2 \omega}{\tau} \approx 10^{-16} \omega$$

Hence limiting energy

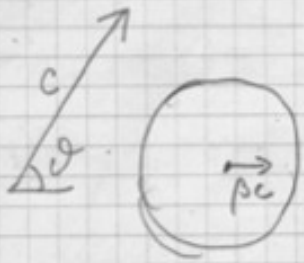
$$\frac{e^4 H^2}{m^4 c^7} \omega \approx 10^{-16}$$

$$\text{assume } H = 10^{-5}$$

$$\omega \approx \frac{m^4 c^7}{e^4 H^2} 10^{-16} \approx \left\{ \frac{.6 \times 10^{-108} \cdot 3 \times 10^{73} \times 10^{-16}}{5 \times 10^{-38} \times 10^{-10}} = 4 \times 10^{-4} \approx 2.5 \text{ MeV} \right. \\ \left. \text{for electrons!} \right.$$

Fermi's notebook

University of Chicago Library
Special Collections



Prob. of collision is

proportional to $(1 - \beta \cos \theta) \times \frac{d\Omega}{4\pi}$

this is exact

$$w' = \frac{w(1 - \beta \cos \theta)}{\sqrt{1 - \beta^2}}$$

If scattering is isotropic in rest-system

Fixed system	Rest system before coll	Rest system after collision	Fixed frame after
$p_x = \frac{w}{c} \cos \theta$	$w' = \frac{w(1 - \beta \cos \theta)}{\sqrt{1 - \beta^2}}$	$w'' = w'$	$w''' = \frac{w'' + \beta p_x''}{\sqrt{1 - \beta^2}}$
$p_y = \frac{w}{c} \sin \theta$	$p_x' = \frac{w}{c} (\cos \theta - \beta)$	$p_x'' = \frac{w'}{c} \cos \varphi$	$= \frac{w'' (1 + \beta \cos \varphi)}{\sqrt{1 - \beta^2}}$
$\theta = 0$	$p_y' = \frac{w}{c} \sin \theta$		$w''' = \frac{w'}{\sqrt{1 - \beta^2}}$
$\varphi = 0$	$p_z' = 0$		

$$\overline{w'''} = \frac{w'}{\sqrt{1 - \beta^2}} = \frac{w(1 - \beta \cos \theta)}{1 - \beta^2}$$

$$w \int \frac{(1 - \beta \cos \theta)}{1 - \beta^2} (1 - \beta \cos \theta) \frac{\sin \theta d\theta}{2} = \frac{1 + \frac{\beta^2}{3}}{1 - \beta^2} w \approx w + \frac{4}{3} \beta^2 w$$

Fermi's notebook

University of Chicago Library
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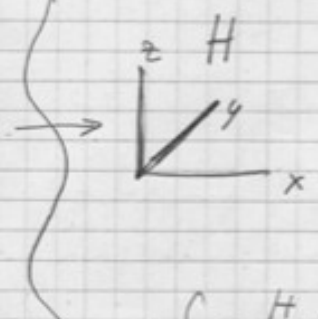
Relativistic calculation

Hence after N collisions

$$w = Mc^2 e$$

December 5 1948 Sunday!

Relaxation time of advection oscillations:



$$H_x = K \quad \vec{v} = (v \hat{x} \otimes 0)$$

$$H_z = H = \text{const} \quad \hat{K} \otimes \hat{H}$$
~~$$E + \frac{1}{c} \vec{v} \times H = 0$$~~

$$\nabla \times E = \begin{cases} -\frac{H}{c} \frac{\partial v}{\partial z} = -\frac{1}{c} \frac{\partial K}{\partial t} \\ 0 \\ 0 \end{cases} \quad E = \begin{pmatrix} 0 & E_y & 0 \end{pmatrix} = \frac{v}{c} H$$

$$\nabla \times H = \begin{cases} 0 \\ \frac{\partial K}{\partial z} = \frac{1}{c} \frac{\partial E}{\partial t} + 4\pi j_y \\ 0 \end{cases}$$

$$F = J \times H = \begin{cases} JH = \frac{H}{4\pi} \left(\frac{\partial K}{\partial z} - \frac{1}{c} \frac{\partial E}{\partial t} \right) = \frac{H}{4\pi} \left(\frac{\partial K}{\partial z} - \frac{Hv}{c^2} \right) \\ 0 \\ JK \text{ (higher order)} \end{cases}$$

$$\frac{\partial K}{\partial t} = H \frac{\partial v}{\partial z} \quad \left(\rho + \frac{H^2}{4\pi c^2} \right) \ddot{v} = \frac{H}{4\pi} \frac{\partial K}{\partial z} \quad J = \frac{1}{4\pi} \left(\frac{\partial K}{\partial z} - \frac{Hv}{c^2} \right)$$

$$\rho \ddot{v} = \frac{H^2}{4\pi} \frac{\partial^2 v}{\partial z^2} \quad \text{velocity of prop} = \frac{H}{\sqrt{4\pi\rho}} \quad \approx \frac{\rho}{H} \ddot{v}$$

K negligible

$k = \text{conductivity } (J = kE)$

$$\text{relax time} = \frac{\rho v^2}{\frac{c\rho^2 \ddot{v}}{2H^2}} = \frac{kH^2}{c\rho v^2} = \frac{4\pi k \lambda^2}{c} \quad \text{Energy loss per cc sec}$$

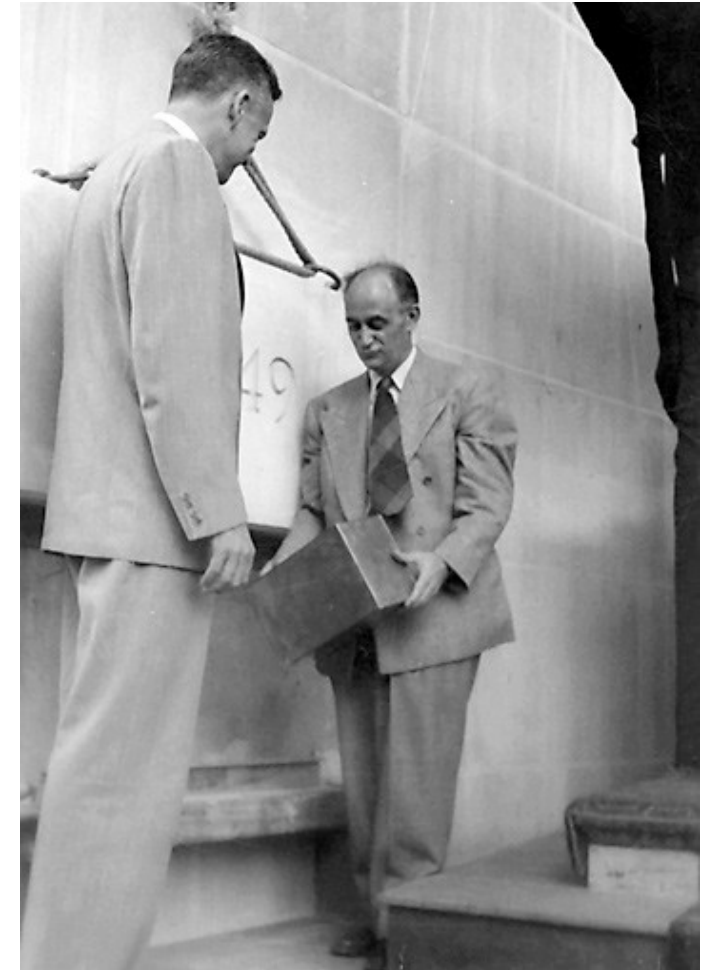
$$\frac{cJ^2}{k} = \frac{c\rho^2}{kH^2} \ddot{v}^2$$

Fermi's notebook

University of Chicago Library
Special Collections



Fermi's time capsule



Opened June 2, 2011



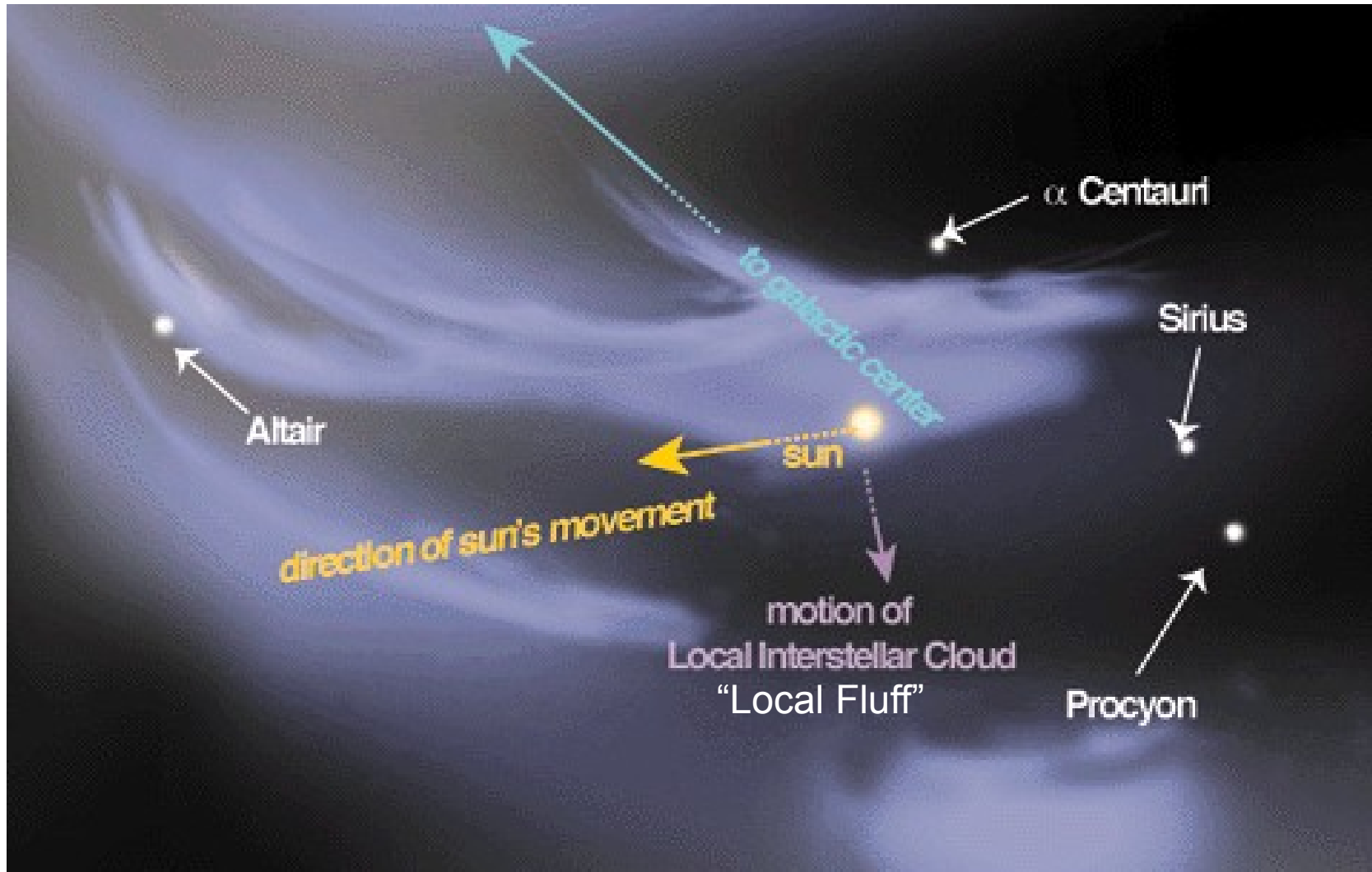
The time capsule contained these items:

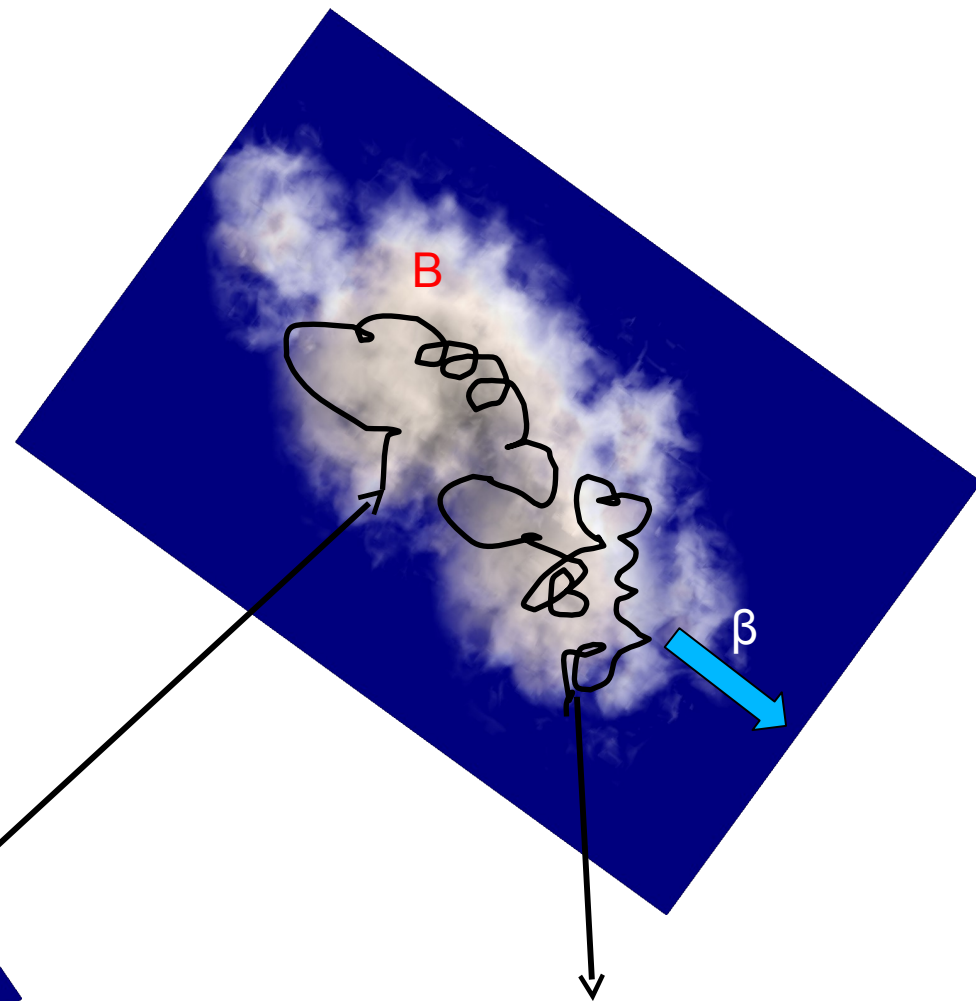
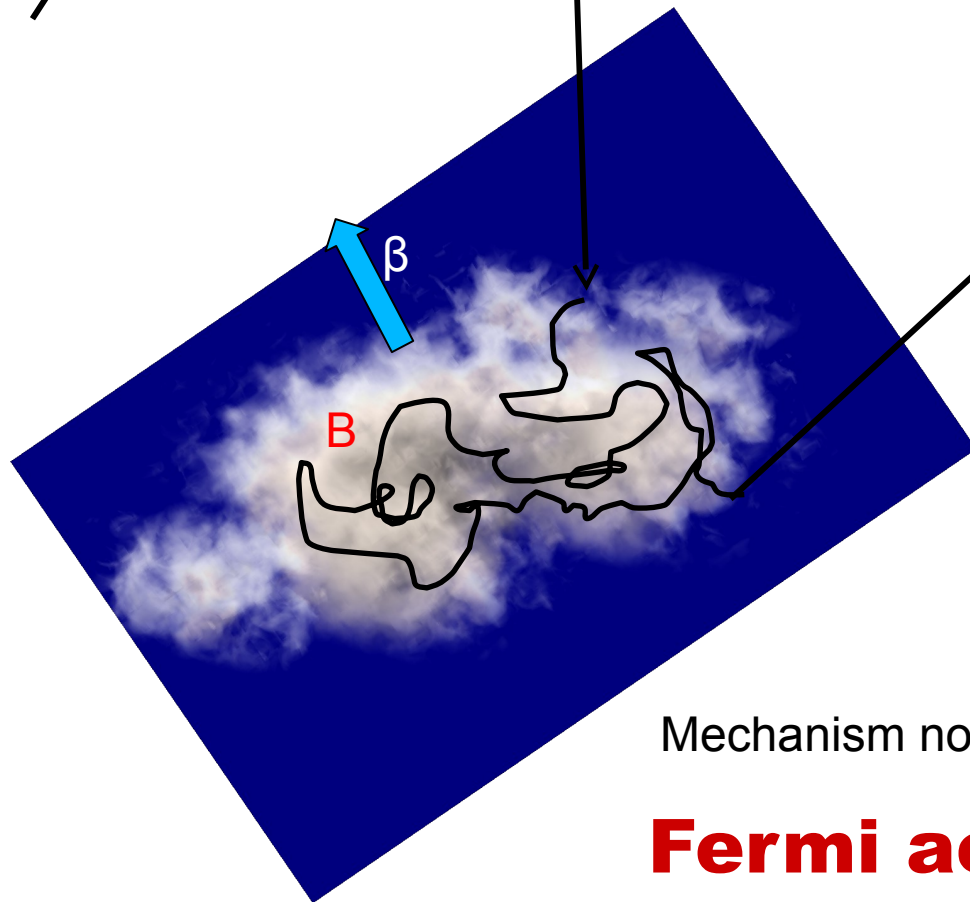
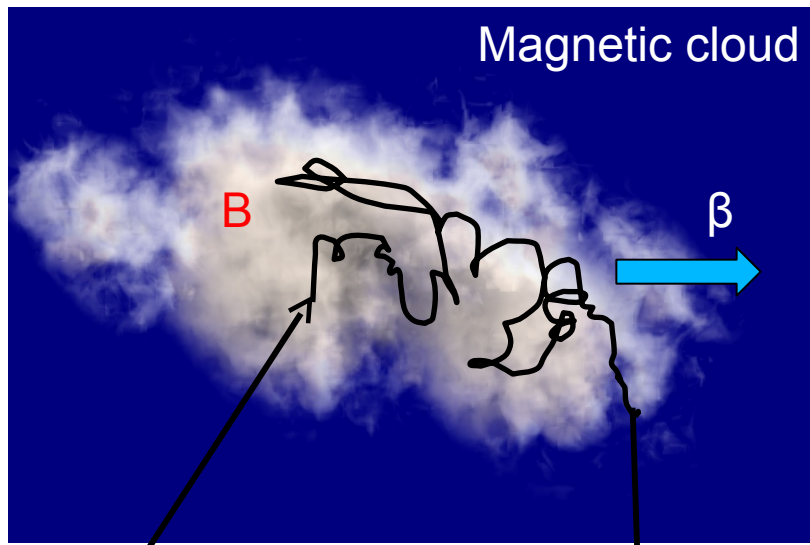
- University of Chicago directory.
- University of Chicago announcements, May 25, 1948.
- Architect's sketch of the Research Institutes building.
- Booklet titled "The New Frontier of Industry — Atomic Research."
- Booklet titled "The Institute for Nuclear Studies, The Institute for the Study of Metals, The Institute of Radiobiology and Biophysics."
- Road map, train and airline timetables.
- List of postdoctoral fellows, Institute of Radiobiology and Biophysics, 1948-1949.

Also found with the time capsule was a 1927 buffalo nickel.



Magnetic Clouds



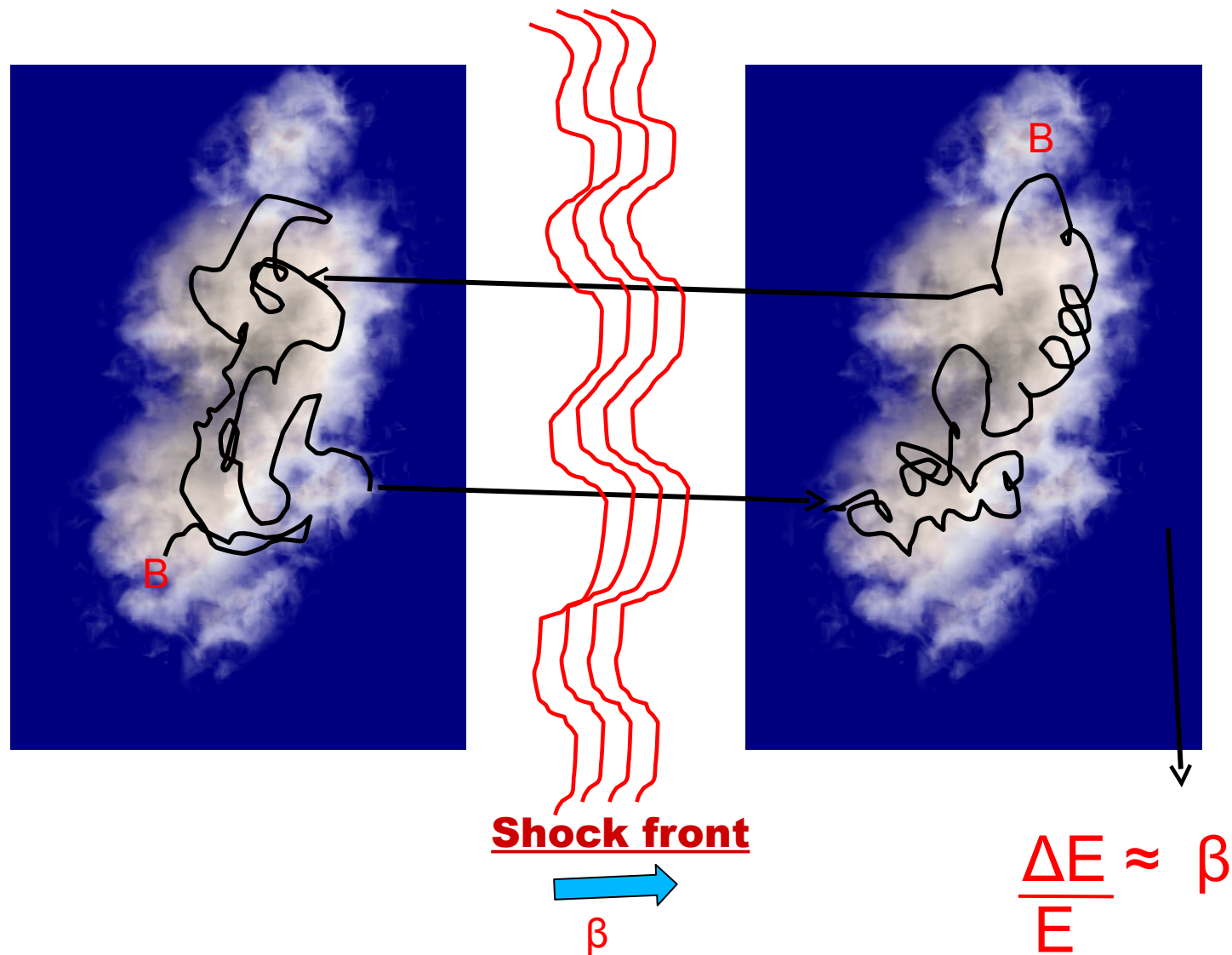


$$\frac{\Delta E}{E} \approx \beta^2$$

Mechanism not efficient enough to accelerate to high energy

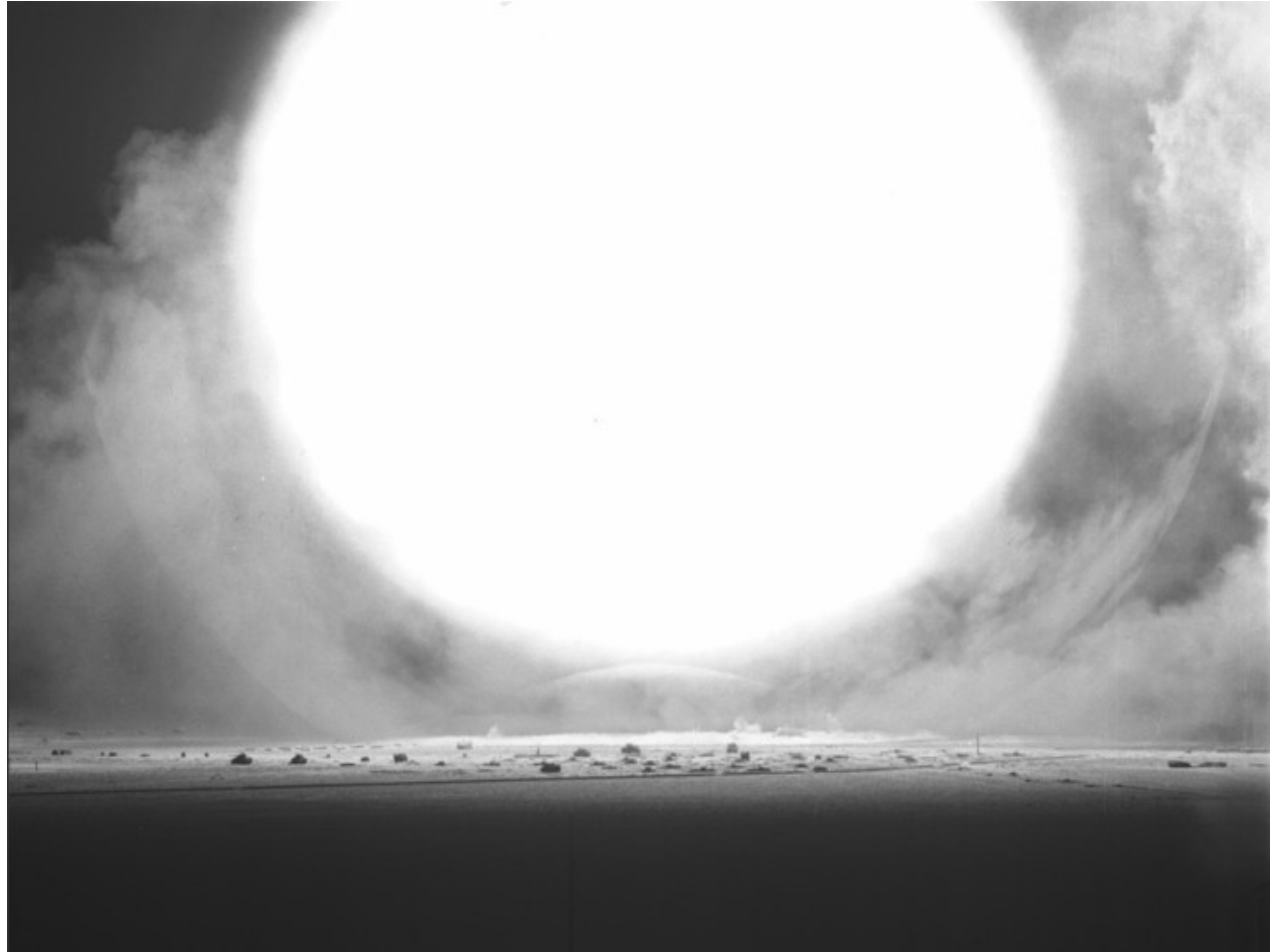
Fermi acceleration (2nd order)

Fermi acceleration (1st order)



The cosmic ray moves back and forth between shocked and unshocked medium

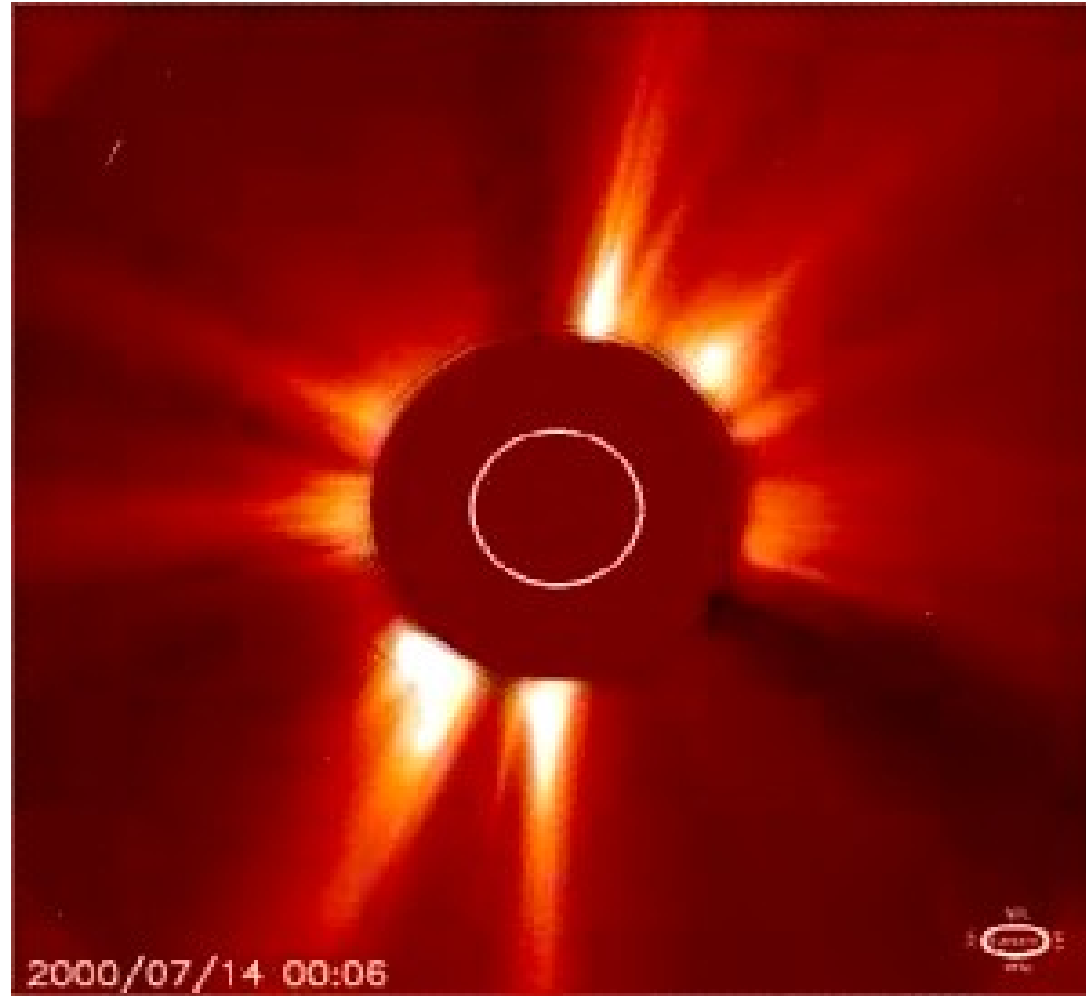
Shocks!



Shock produced by object moving faster than sound in the medium

Shock acceleration of cosmic rays by the sun

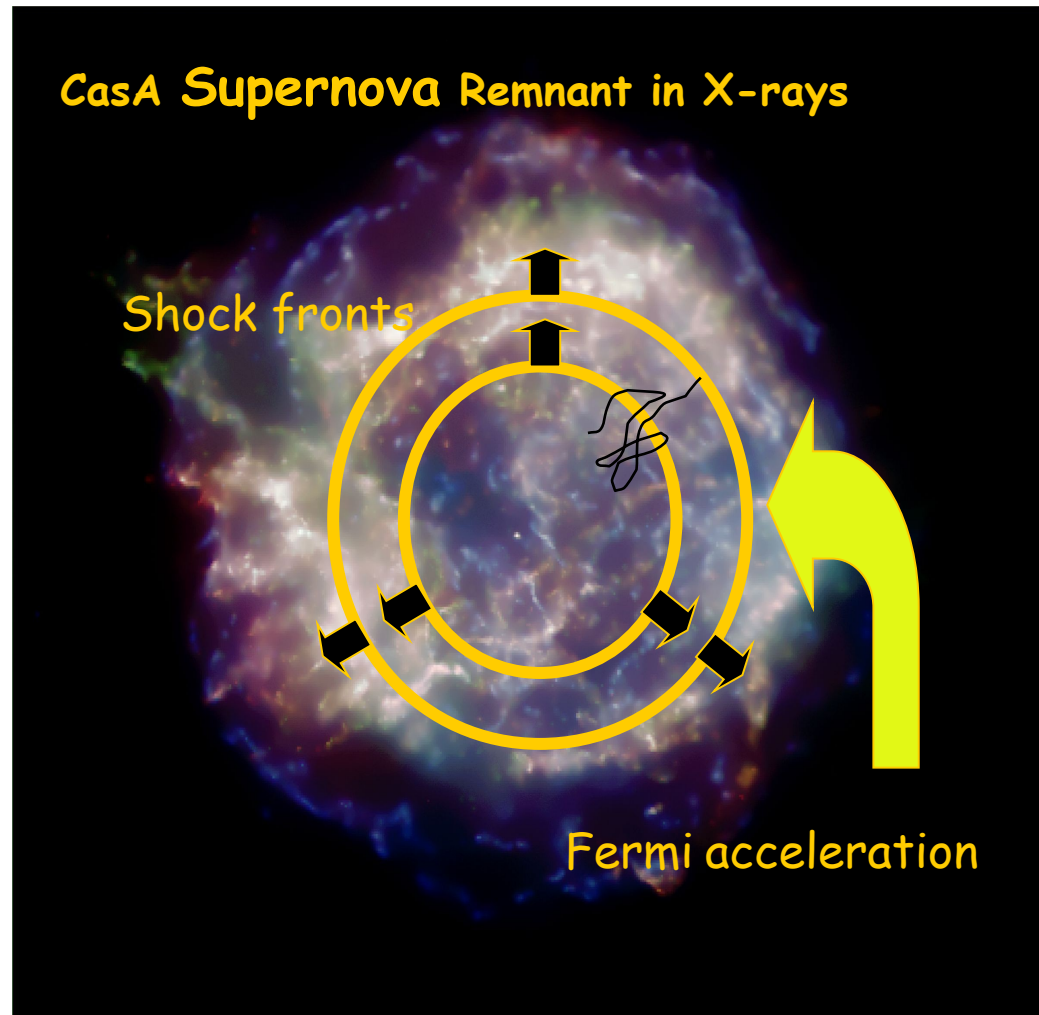
Coronal mass ejection: billions of tons of matter at millions of km / hour



SOHO (SOlar and Heliospheric Observatory) spacecraft

Shock acceleration in SNR

Popular model for high energy cosmic rays (up to 10^{15} eV)



$$\beta \approx 0.01$$

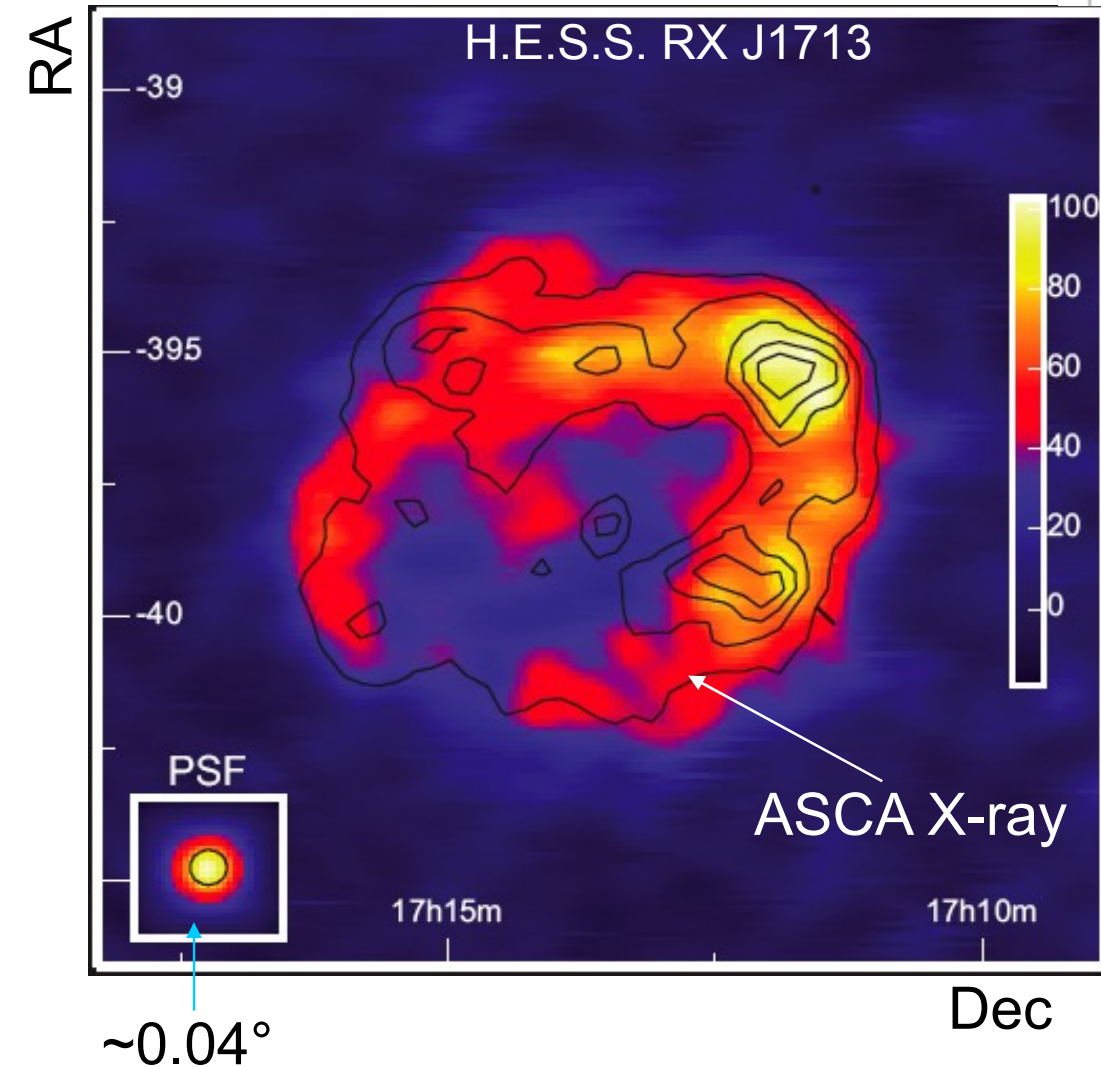
SNR expands for ≈ 1000 years

TeV Gamma Rays from SNR

Distance from earth 1 kpc
Shell radius = 10 pc

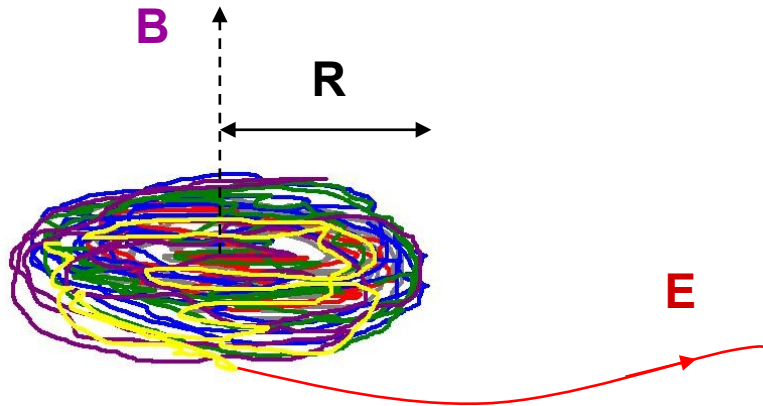
High-energy particle acceleration in
the shell of a supernova remnant

NATURE | VOL 432 | 4 NOVEMBER 2004 | 1



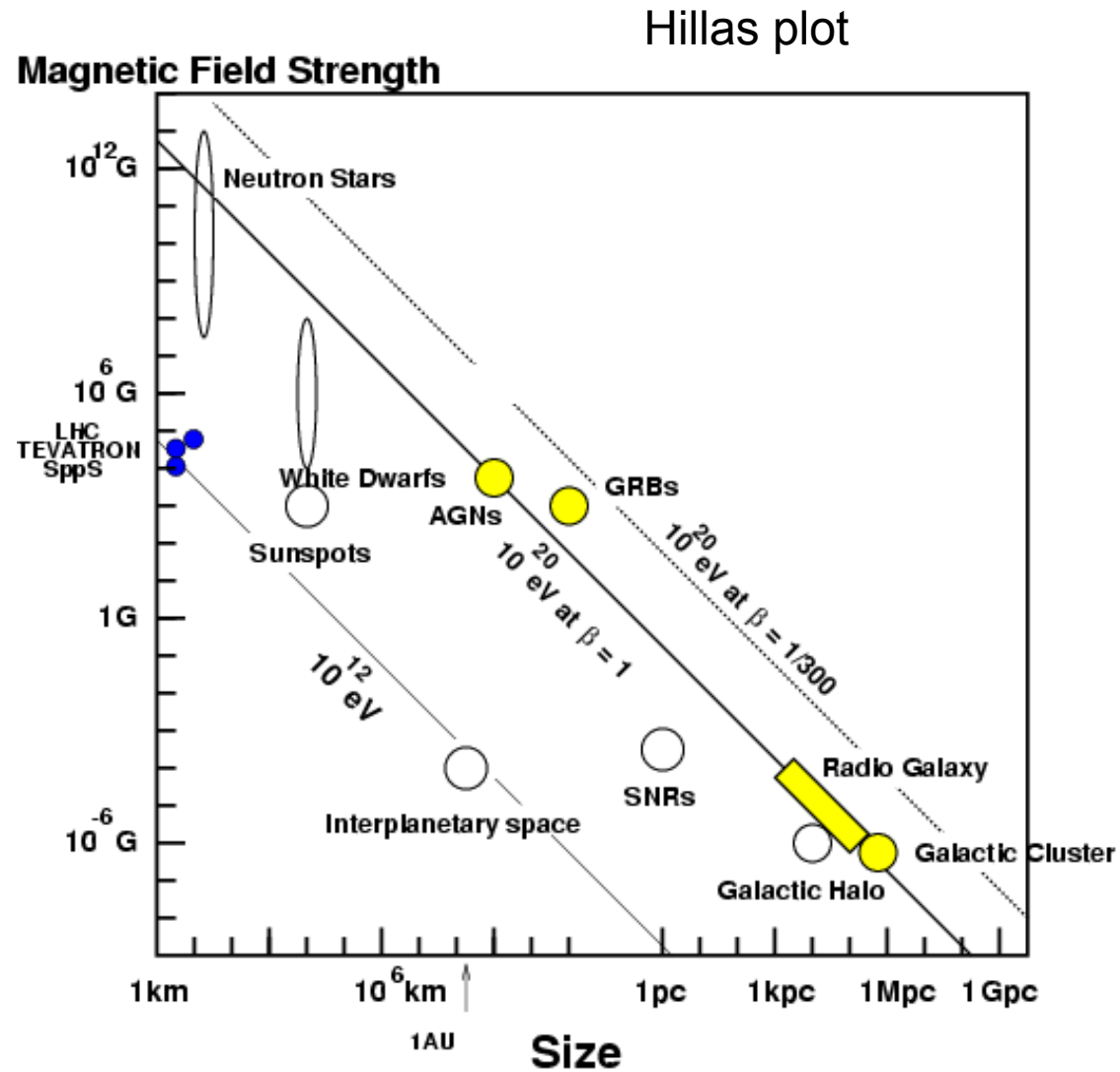
HESS in Namibia
Atmospheric Cherenkov Telescope

10²⁰ eV accelerator?



$$E \sim z \beta B R$$

Particles must be confined by the magnetic field till they escape the accelerating region



Astrophysical shocks

- Active galactic nuclei produce jets with internal shocks and huge shocks at the end (hot spots)

$z = 0.1745$

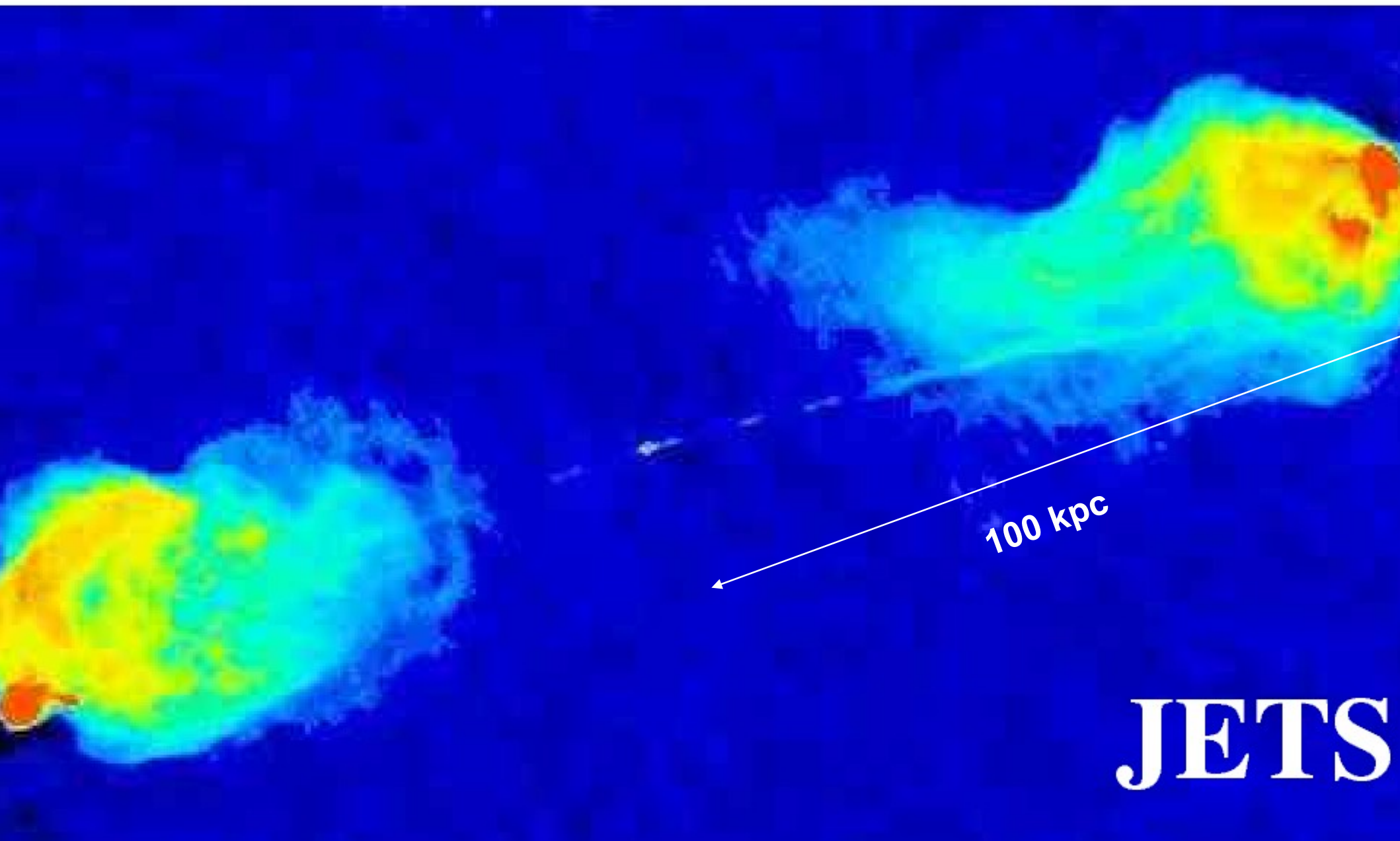
3C 219



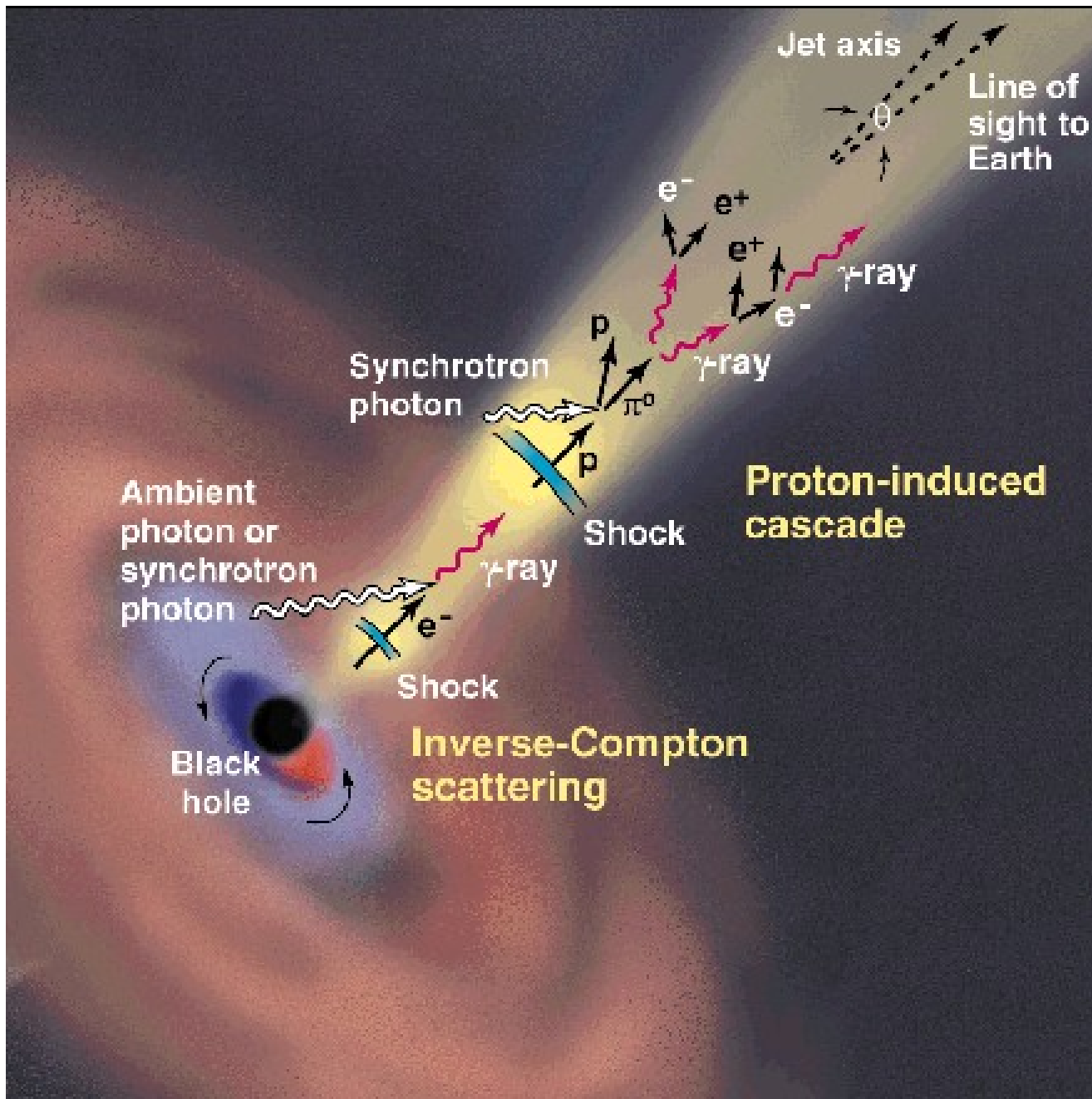
CYGNUS-A

FR-II

$z = 0.0565 \approx 200 \text{ Mpc}$

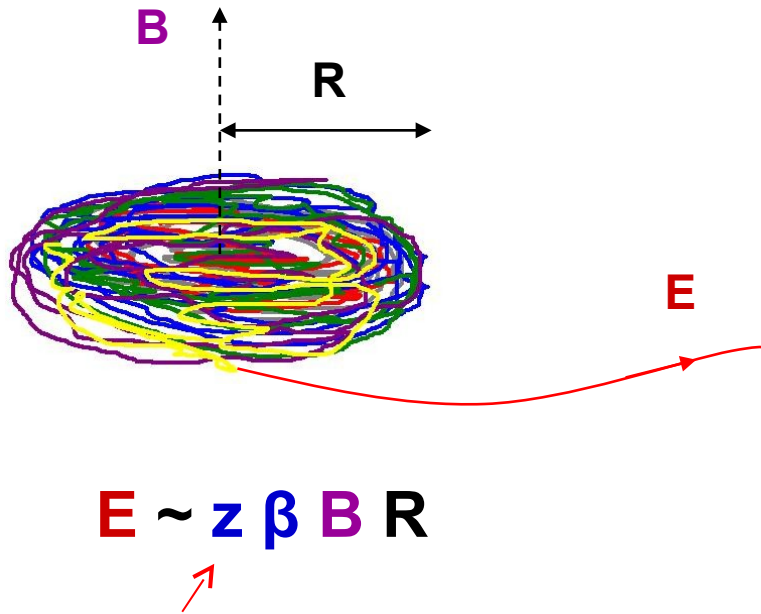


WLA radio image

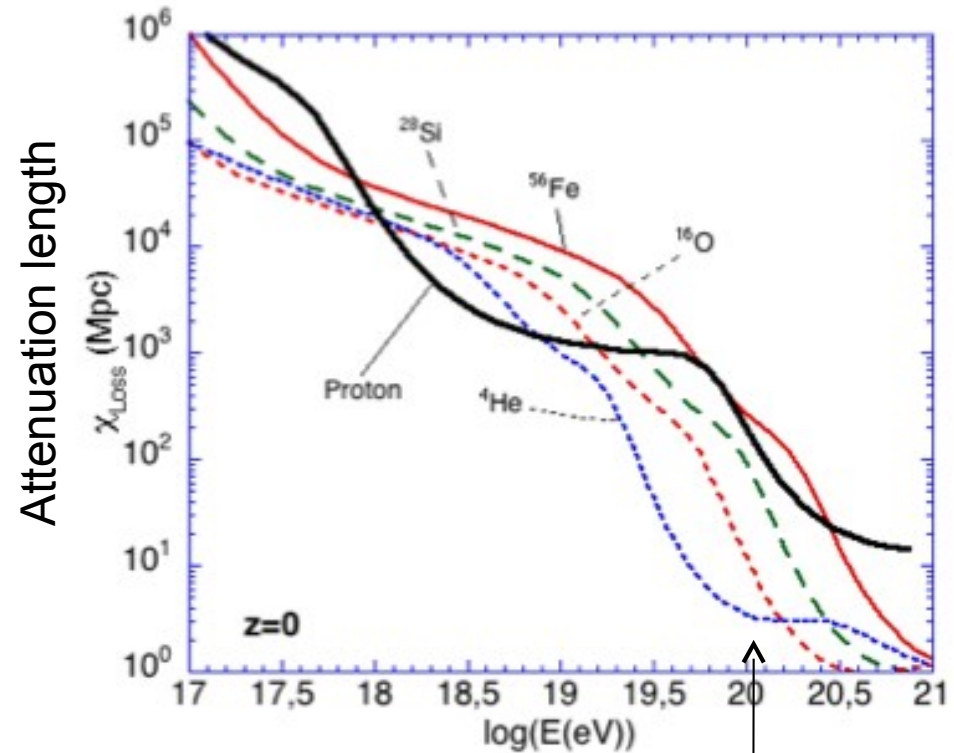


Active Galactic Nuclei

Proton vs heavy nuclei



For the same magnetic field strength and accelerating region size, nuclei can reach energy Z times larger than a proton (example: $Z = 26$ for Iron) but.....



Nuclei lose rapidly their energy through photodisintegration processes. Iron still ok.

$$\vartheta_d \approx 0,5^\circ \cdot Z \cdot \left(\frac{E}{10^{20} \text{eV}} \right)^{-1} \cdot \left(\frac{d}{1 \text{ Mpc}} \right) \cdot \left(\frac{B}{10^{-9} \text{G}} \right)$$

If UHECR are heavy nuclei, their directions will be scrambled and they will not point back to the source!

Physics (well) beyond the SM?

A few articles titles.....

- Microscopic black hole detection in UHECR
- Lorentz invariance violation
- Instant preheating mechanism and UHECR.
- Flipped Cryptons and the UHECRs.
- Super-heavy X particle decay
- Strongly interacting neutrinos
- Electroweak instantons as a solution
- Quantum-gravity phenomenology
- Superheavy dark matter.....
- Long-lived neutralino
- Cosmic Rays and Large Extra Dimensions
- UHECR from relic topological defects.
- Are UHECR a signal for supersymmetry?.

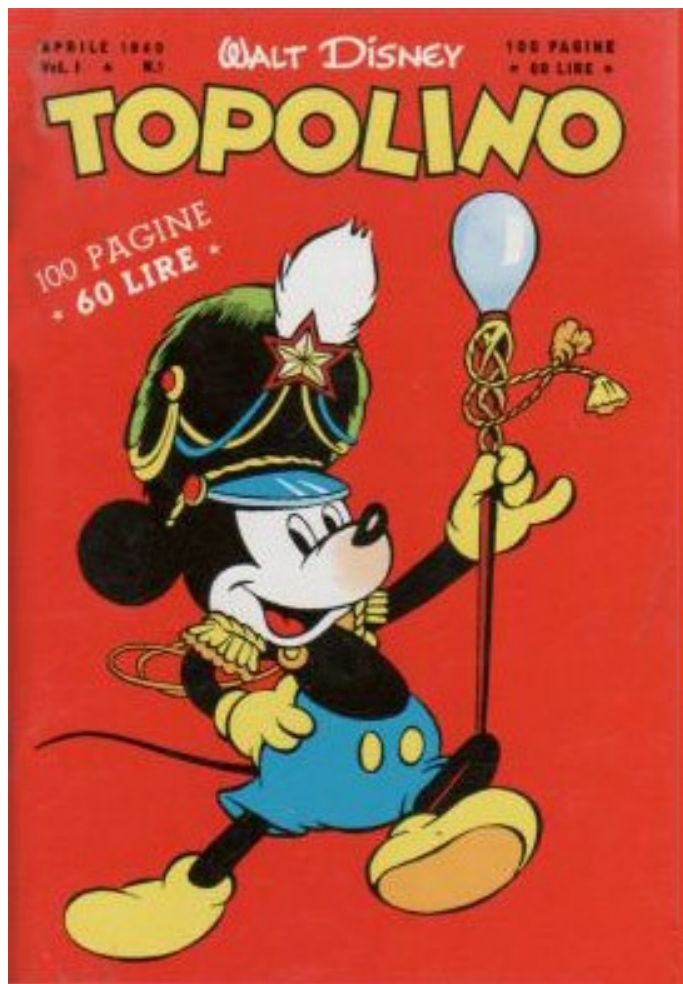
.....

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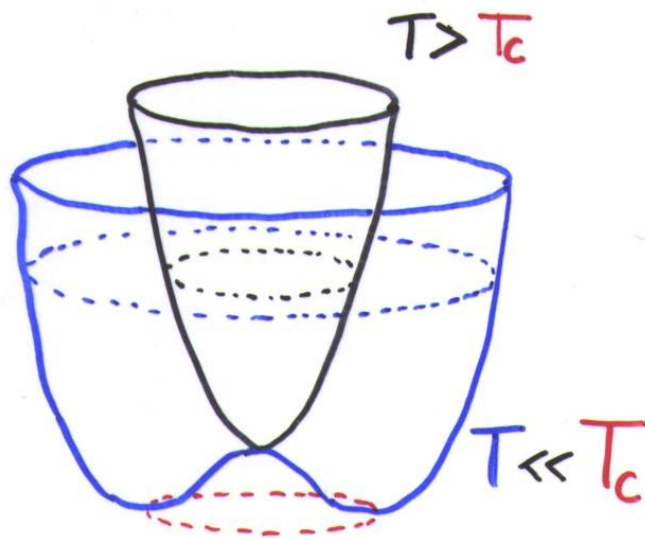
COSMIC



TOPO-LOGICAL
DEFECT



SYMMETRY BREAKING PHASE TRANSITIONS IN EARLY UNIVERSE



$$\text{Ex: } \mathcal{L}(\phi) = \frac{1}{2}(\partial_\mu \phi)^2 - V_T(\phi)$$

$$\bullet T \rightarrow 0 \quad V_0 = \frac{1}{4} \lambda (|\phi|^2 - m^2)^2$$

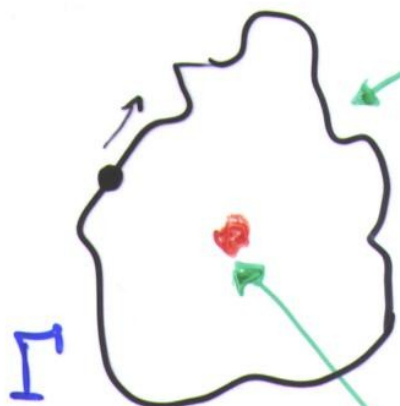
$$\bullet T > T_c \quad V \sim T^2 \phi^2$$

$$T_c \sim m_{\text{GUT}} \sim 10^{25} \text{ eV}$$

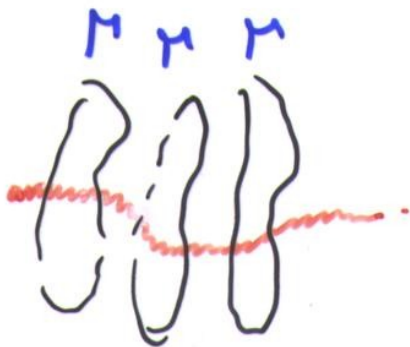
$T > T_c$: VACUUM SYMMETRIC UNDER PHASE ROTATIONS

$T < T_c$: A GIVEN VACUUM STATE NO LONGER INVARIANT UNDER PHASE ROTATIONS \rightarrow "SPONTANEOUS" SYMM. BREAKING
 $\langle \phi \rangle = v(T) e^{i\alpha}$

IN AN EARLY UNIVERSE PHASE TRANSITION, WE EXPECT THAT PHASES IN WIDELY SEPARATED REGIONS WILL BE UNCORRELATED



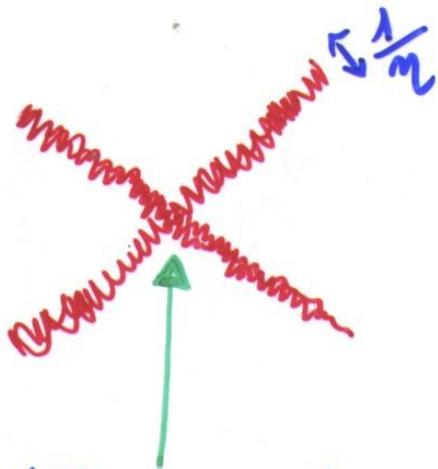
TAKE A CLOSED CURVE IN A PLANE OF PHYSICAL SPACE
 MOVING AROUND Γ THE FIELD ϕ CAN CHANGE
 ITS PHASE. ONCE BACK TO THE STARTING
 POINT $\alpha(1) = \alpha(0) + m2\pi$
 IF $m \neq 0 \Rightarrow$ THERE IS A REGION IN
THE INTERIOR OF Γ WHERE $\langle \phi \rangle = 0$



A COSMIC
 STRING.

$V_{T=0} \neq \emptyset$! THERE IS ENERGY
 (MASS) TRAPPED IN THERE


 $m_x \sim m \sim T_c$



$$\mu \sim \eta^2$$

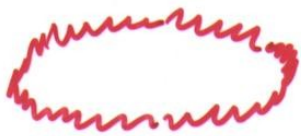
↑
ENERGY
PER UNIT
LENGTH

$$(\mu \sim 10^{22} \text{ gms/cm !!})$$

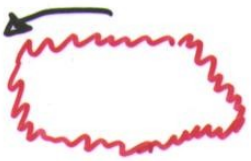
$$\text{ENERGY RELEASE} \sim \mu \cdot \frac{1}{m} \sim \eta \sim m_x$$

↑

INTERSECTION REGION $\sim \frac{1}{m}$, THE PHASE BECOMES UNDEFINED
AND THE ENERGY CONTAINED IN THE OVERLAPPING REGION
IS RELEASED IN THE FORM OF X PARTICLES

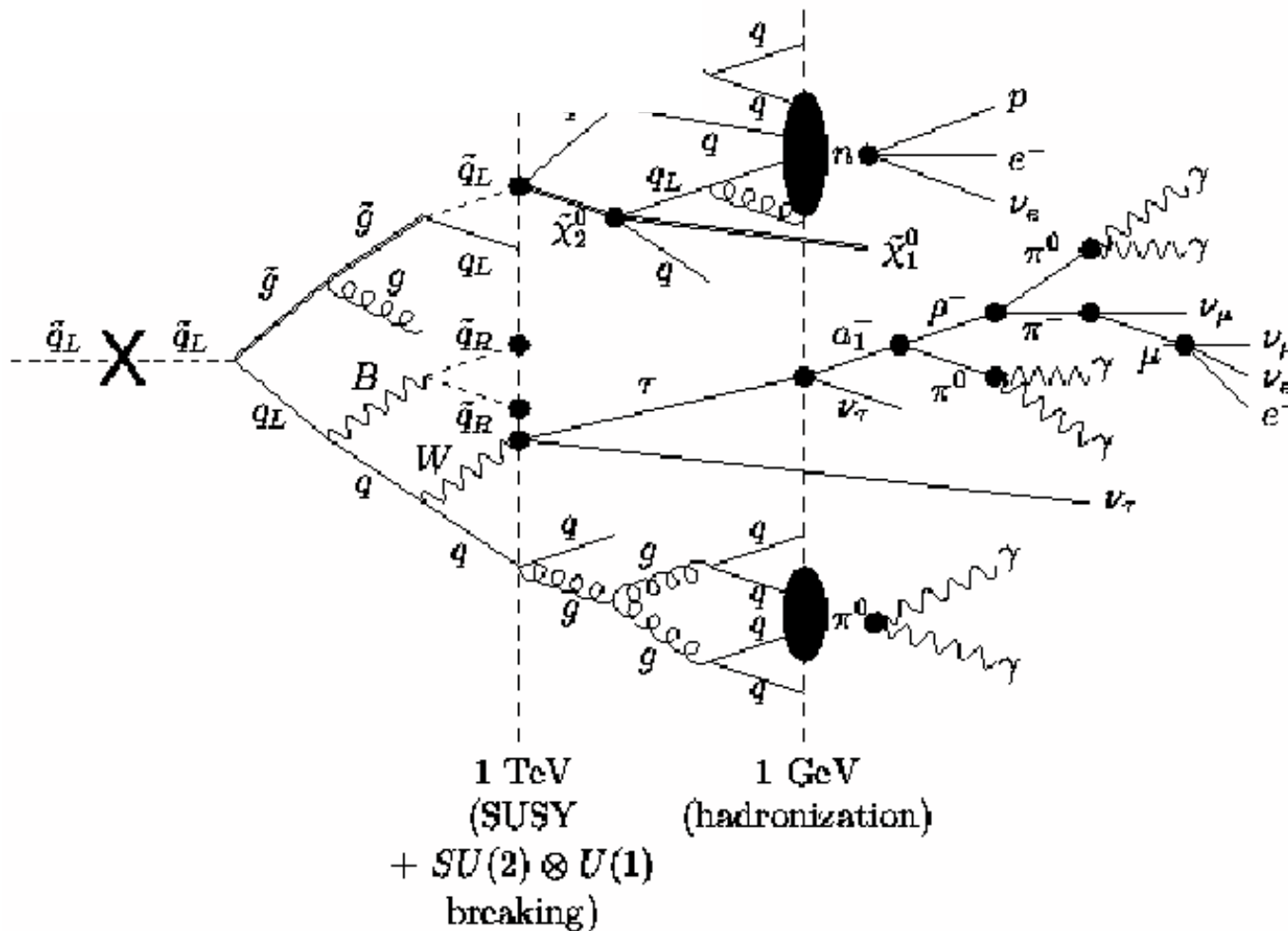


OSCILLATES EMITTING GRAVITATIONAL
RADIATION TILL RADIUS $\sim \frac{1}{m}$
AND THEN COLLAPSES



SUPERCONDUCTING STRING LOOPS. CARRY PERSISTENT
ELECTRIC CURRENTS (CHARGED HIGGS, FERMIONS)
SHRINKING THE CURRENT BECOMES $> I_{crit}$.
AND CHARGED CARRIERS ARE EJECTED

X-particle decay cascade



Particles at the end of the cascade:

predominantly photons

Neutrinos

Few protons

No nuclei

**UHECR photons
signature for New
Physics**

Schematic MSSM “jet” for an initial squark with a virtuality $Q \simeq M_X$. The full circles indicate decays of massive particles, in distinction to fragmentation vertices. The two vertical dashed lines separate different epochs of the evolution of the cascade: at virtuality $Q > m_{\text{SUSY}}$, all MSSM particles can be produced in fragmentation processes. Particles with mass of order m_{SUSY} decay at the first vertical line. For $m_{\text{SUSY}} < Q < 1 \text{ GeV}$ light QCD degrees of freedom still contribute to the perturbative evolution of the cascade. At the second vertical line, all partons hadronize, and unstable hadrons and leptons decay.

(from M. Drees, e-print hep-ph/0210142)

The UHECR 3-piece puzzle

1) The Greisen -Zatsepin-Kusmin cutoff: END TO THE COSMIC-RAY SPECTRUM?

Pion photoproduction (on CMB radiation)



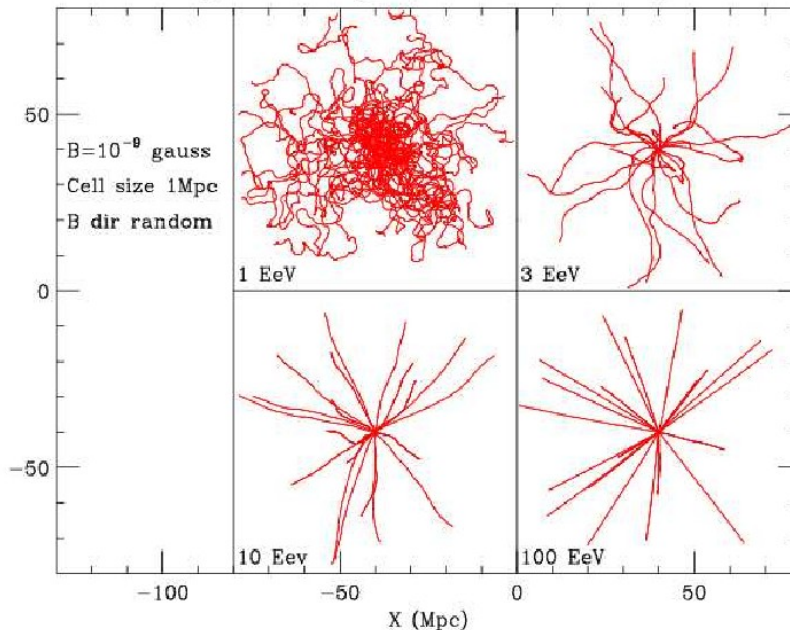
Kenneth Greisen

Cornell University, Ithaca, New York

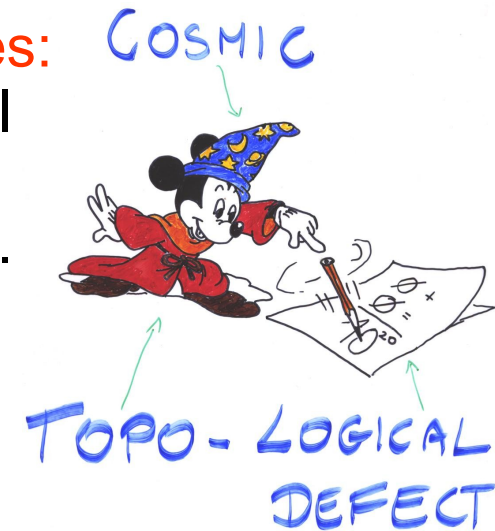
(Received 1 April 1966)

This note predicts that above 10^{20} eV the primary spectrum will steepen abruptly, and the experiments in preparation will at last observe it to have a cosmologically meaningful termination.

3D trajectories projected on X-Y plane

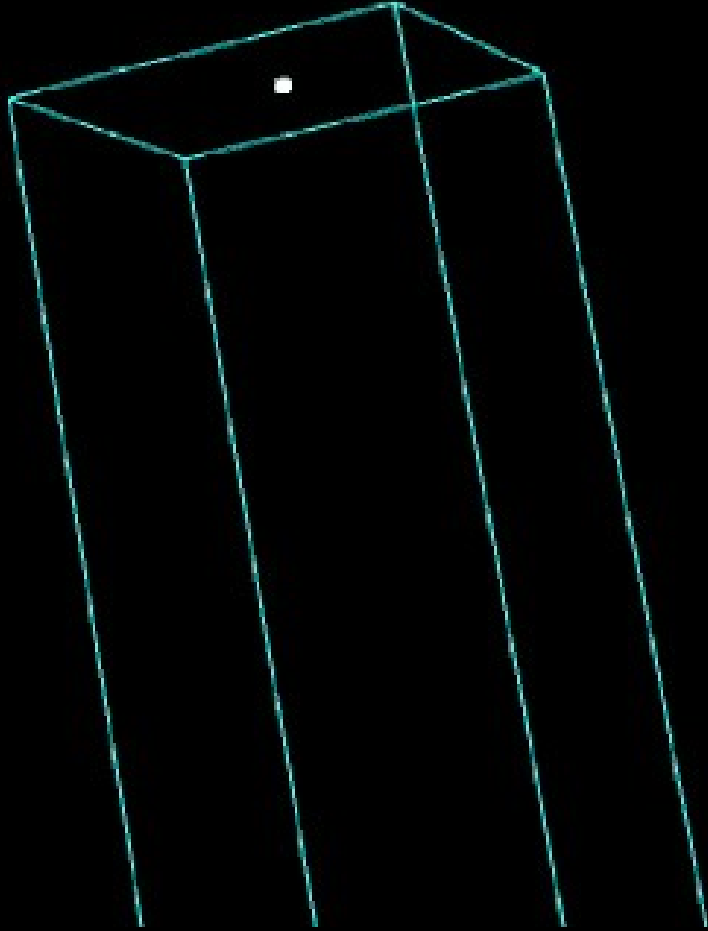


2) The UHECR sources:
Close-by astrophysical accelerators?
<100 Mpc due to GZK.
New Physics?

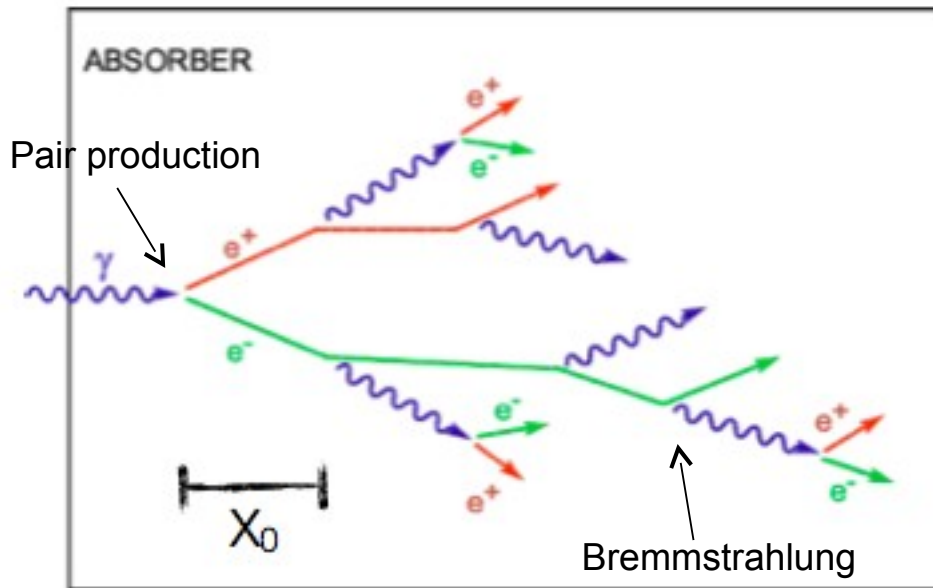


3) The UHECR composition:
protons? Heavier nuclei
(deviation in magnetic fields)

Only by understanding all of
the three pieces we will unveil
the true nature of UHECRs



Electromagnetic Showers



After \approx one X_0 (radiation length) the electromagnetic particle (photon or e^\pm) interacts

X_0 in cm or (multiplying length by density of absorber) in g/cm^2

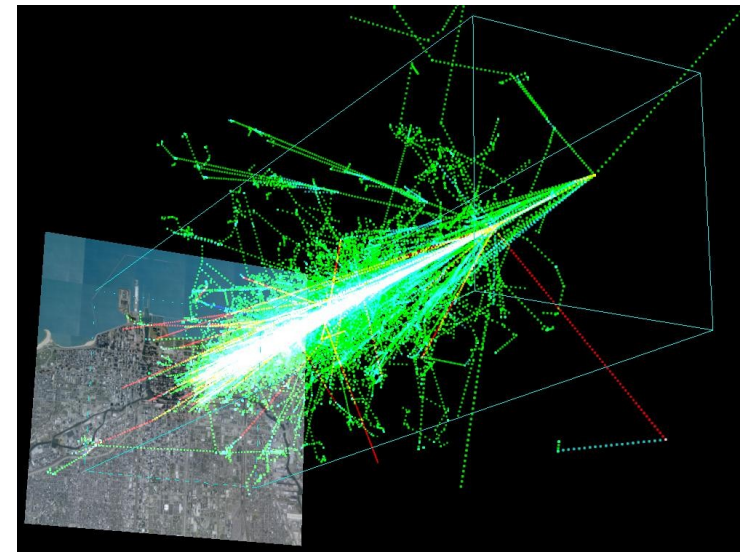
Examples:

$$X_0(\text{Pb}) = 6.4 \text{ g}/\text{cm}^2 = 0.56 \text{ cm}$$

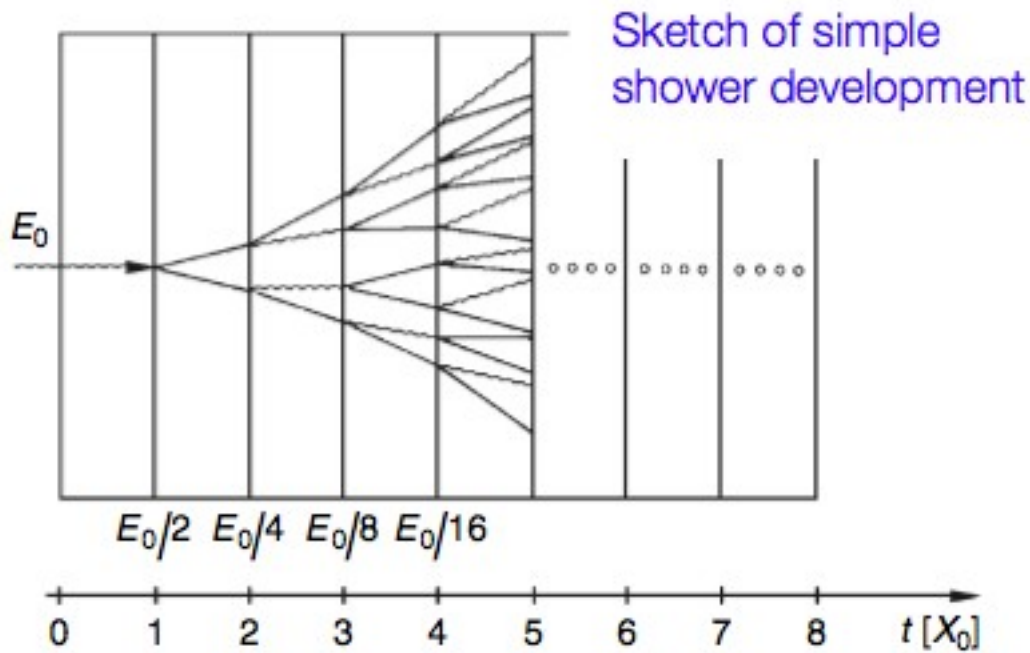
$$X_0(\text{air}) = 37 \text{ g}/\text{cm}^2 = 300 \text{ m} !$$

$$X_0(\text{air}) = 37 \text{ g}/\text{cm}^2 = 300 \text{ m} !$$

$$X_0(\text{Pb}) = 6.4 \text{ g}/\text{cm}^2 = 0.56 \text{ cm}$$



Heitler model of shower development



Assume that each time energy is divided equally between the two particles produced in the interaction

The shower will stop growing when the particle energy goes below a critical energy E_c (when energy loss by ionization overcome photon production by Bremsstrahlung)

$$N(t) \quad 2 \quad 4 \quad 8 \quad 16 \quad \dots \quad 2^t$$

The energy per particle after t radiation length is $E = E_0/2^t$

The maximum of the shower t_{\max} is reached when the particles' energy is = to E_c

$$E_c = E_0/2^{t_{\max}}$$

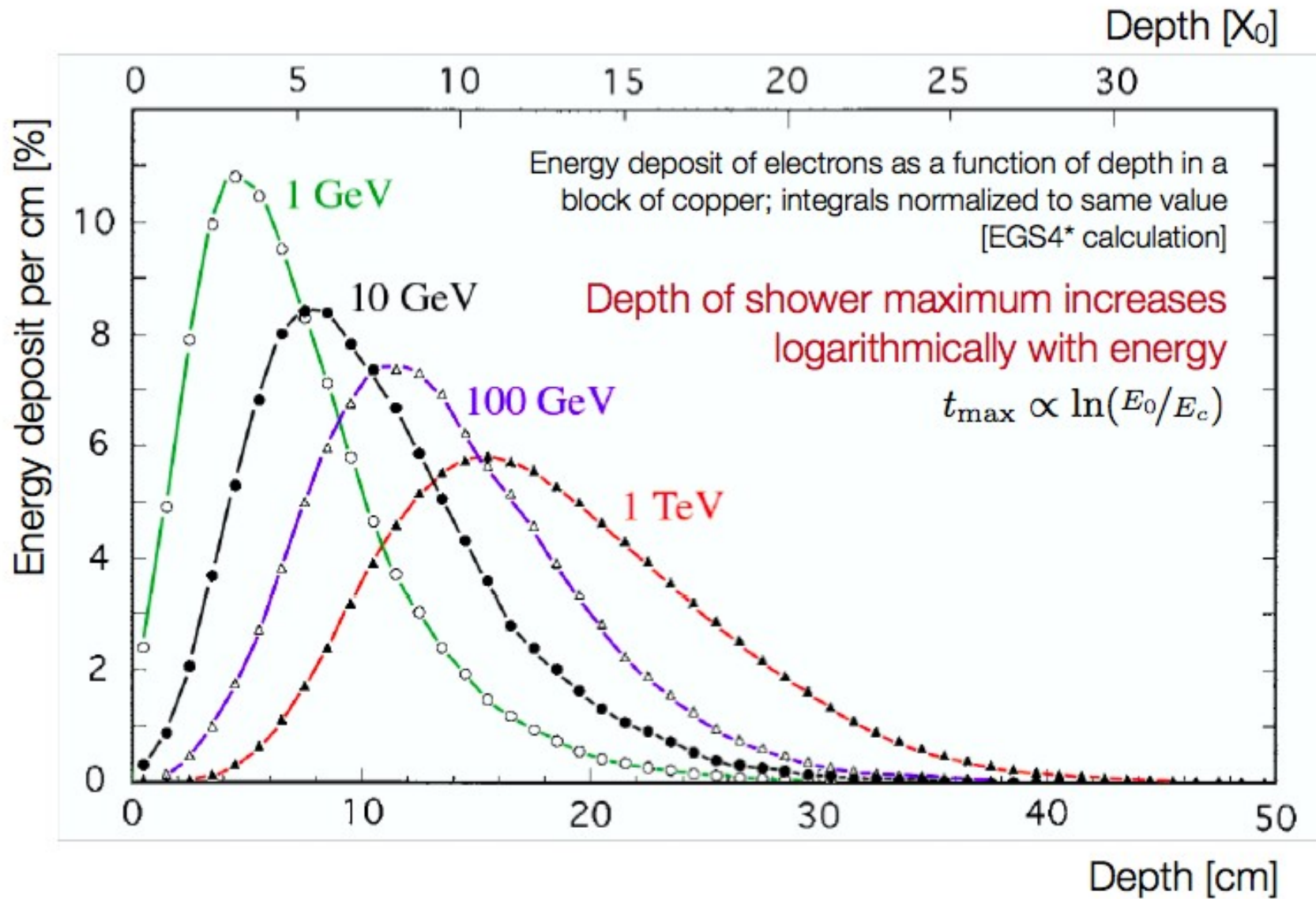
$$t_{\max} = \log_2 (E_0/E_c)$$

$$N_{\max} = 2^{t_{\max}} = E_0/E_c$$

shower max increases logarithmically with E

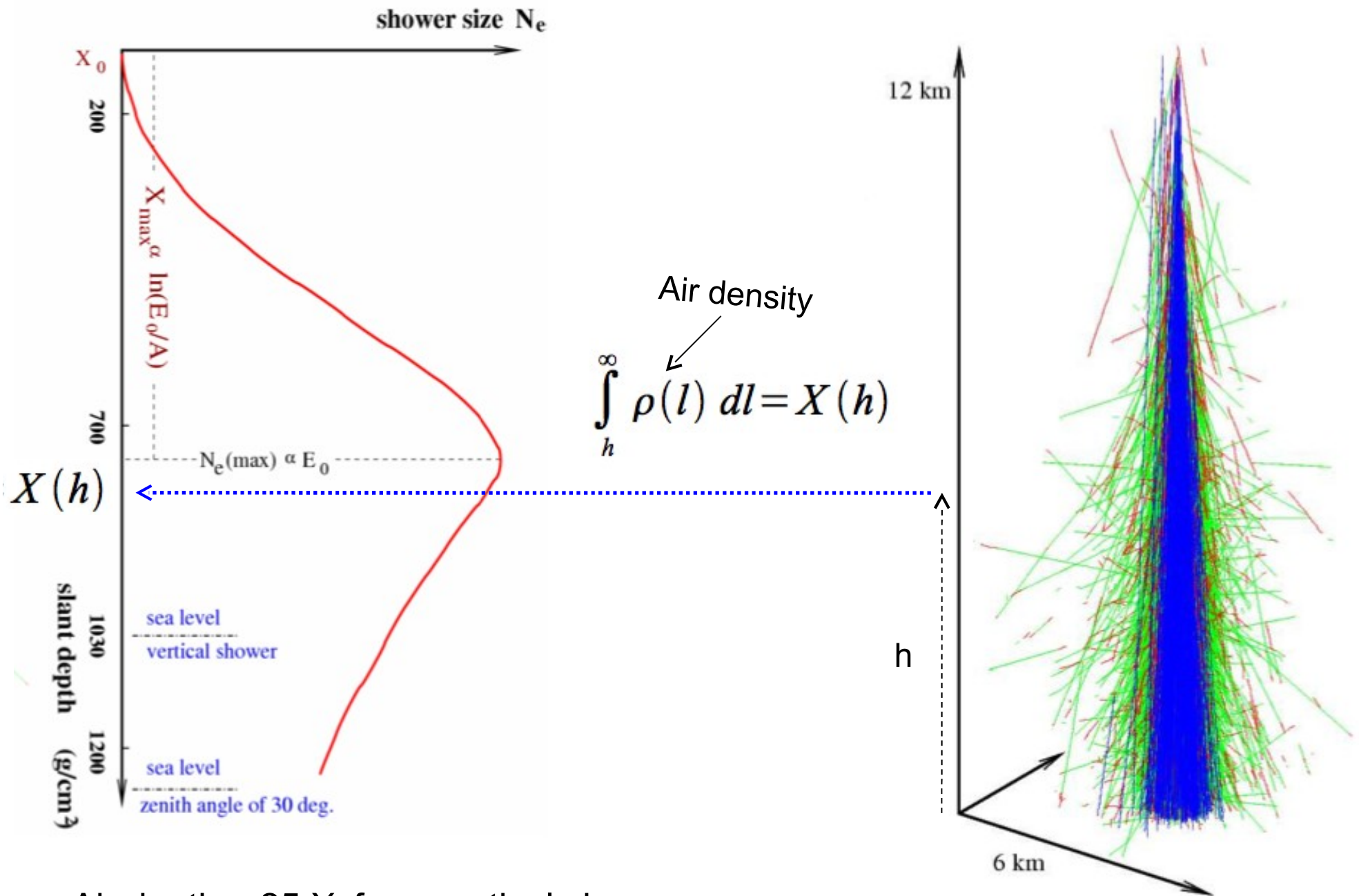
n. of particles at the max is proportional to E

Shower development



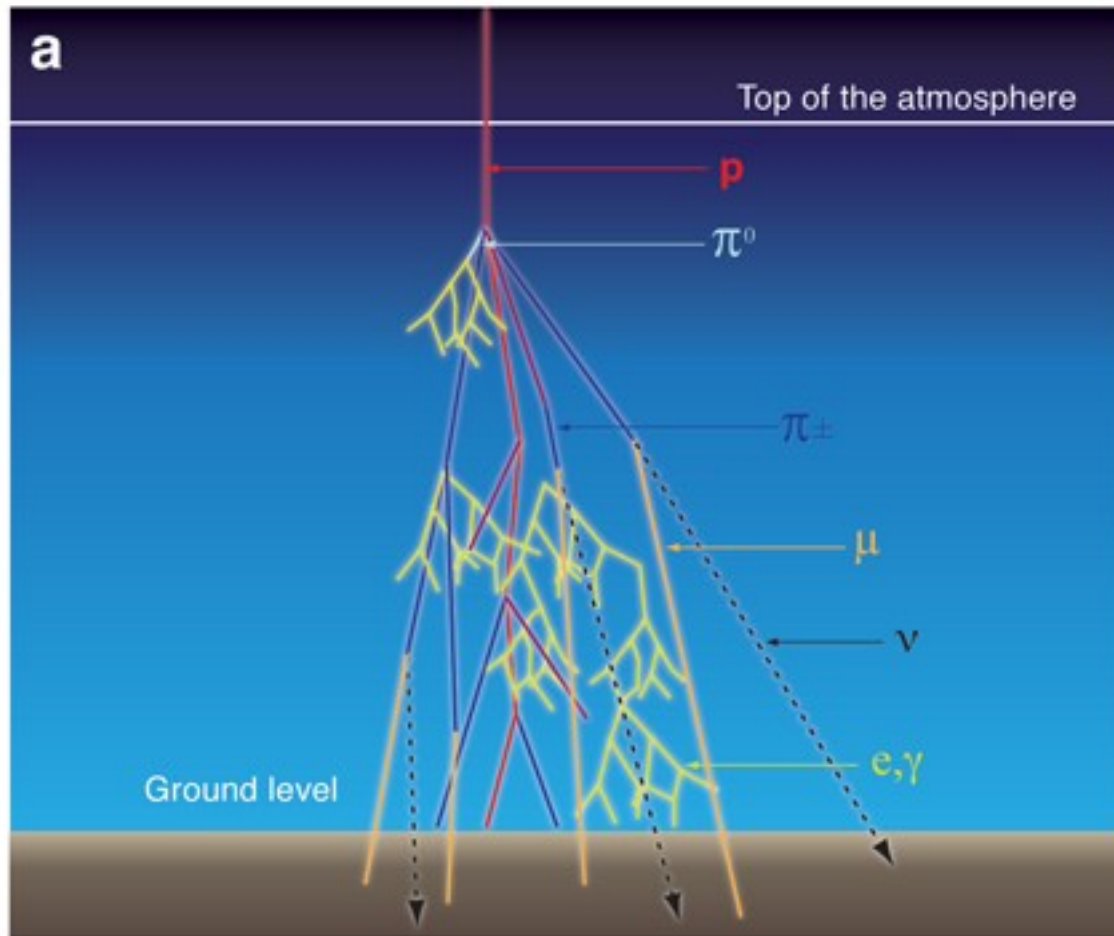
Fundamental for particle physics calorimetry: imagine if t_{\max} would increase linearly with energy

Atmosphere as a “calorimeter”



Air depth $\approx 25 X_0$ for a vertical shower

Hadronic Showers



- Shower particles mainly e^\pm and photons

(π^\pm interacts or decay, $\pi^0 \rightarrow \gamma\gamma$)

- $\approx 90\%$ of the primary cosmic ray energy is converted to ionization energy

- $\approx 10^{11}$ particles in a 10^{19} eV shower!

**Let's detect
UHECR
showers!**

At ground mainly e^\pm and photons, muons, neutrinos