

Results and opportunities in pion and muon decays

Dinko Počanić

University of Virginia

PSI 2010 Workshop,
Paul Scherrer Insitute, Switzerland
11-15 October 2010

Outline

Overview and status of allowed π and μ decays

Pion beta decay: $\pi^+ \rightarrow \pi^0 e^+ \nu$

Radiative pion decay: $\pi^+ \rightarrow e^+ \nu \gamma$

Allowed muon decays: ordinary and radiative

The π_{e2} decay: $\pi^+ \rightarrow e^+ \nu$

Summary

Known and measured pion and muon decays

Decay	BR		
$\pi^+ \rightarrow \mu^+ \nu$	0.9998770 (4)	$(\pi_{\mu 2})$	
$\mu^+ \nu \gamma$	$2.00 (25) \times 10^{-4}$	$(\pi_{\mu 2 \gamma})$	
$e^+ \nu$	$1.230 (4) \times 10^{-4}$	$(\pi_{e 2})$	✓
$e^+ \nu \gamma$	$1.61 (23) \times 10^{-7}$	$(\pi_{e 2 \gamma})$	✓
$\pi^0 e^+ \nu$	$1.025 (34) \times 10^{-8}$	$(\pi_{e 3}, \pi_{\beta})$	✓
$e^+ \nu e^+ e^-$	$3.2 (5) \times 10^{-9}$	$(\pi_{e 2 ee})$	
$\pi^0 \rightarrow \gamma \gamma$	0.98798 (32)	✓	
$e^+ e^- \gamma$	$1.198 (32) \times 10^{-2}$	(Dalitz)	
$e^+ e^- e^+ e^-$	$3.14 (30) \times 10^{-5}$		
$e^+ e^-$	$6.2 (5) \times 10^{-8}$		
$\mu^+ \rightarrow e^+ \nu \bar{\nu}$	~ 1.0	✓	
$e^+ \nu \bar{\nu} \gamma$	0.014 (4)	✓	
$e^+ \nu \bar{\nu} e^+ e^-$	$3.4 (4) \times 10^{-5}$		

Pions, muons, fundamental interactions & symmetries

- ▶ Why isn't $\pi \rightarrow e$ the dominant decay mode?
Deep link to **V – A** nature of the **weak interaction** $\Longleftrightarrow$ **PV**;
- ▶ Pion triplet (π^+ , π^0 , π^-), are the **Goldstone bosons** in the spontaneous breaking of **Chiral Symmetry**;
- ▶ Explicit breaking of χS : $m_\pi^2 \propto m_q$ (Gell-Mann–Oakes–Renner rel.);
- ▶ **Conserved Vector Current**: $\Longleftrightarrow$ **SU(2)_V**;
- ▶ Why is the beta energy spectrum in $\mu \rightarrow e$ decay continuous (3-body decay, **NO** $\mu \rightarrow e\gamma$)? $\Rightarrow$ **Lepton Flavor Conservation**.

Today there are **many** excellent precise measurements exploring these topics: **FAST**, **MEG**, **MULAN**, **Muon(g-2)**, **TWIST**,...

Recent π , μ allowed decay measurements

- ▶ $\pi^+ \rightarrow \pi^0 e^+ \nu_e$ PIBETA ('99-'01)
 - SM checks related to CKM unitarity
- ▶ $\pi^+ \rightarrow e^+ \nu_e \gamma$ (or $e^+ e^-$) PIBETA ('99-'04), PEN ('06-)
 - F_A/F_V , π polarizability (χ PT calibration)
 - tensor coupling besides $V - A$ (?)
- ▶ $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$ TWIST (2003-04)
 - departures from $V - A$ in $\mathcal{L}_{\text{weak}}$
- ▶ $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$ (or $e^+ e^-$) PIBETA ('04), PEN ('06-)
 - departures from $V - A$ in $\mathcal{L}_{\text{weak}}$
- ▶ $\pi^+ \rightarrow e^+ \nu_e$ $\left\{ \begin{array}{l} \text{PEN (2006-)} \\ \text{PiENU ('06-)} \end{array} \right.$
 - e - μ universality
 - pseudoscalar coupling besides $V - A$
 - ν sector anomalies, Majoron searches, $\mathbf{m}_{h^+}$, PS I - $\mathbf{q}$'s, V I - $\mathbf{q}$'s, ...
 - search for signs of SUSY (MSSM)

Pion beta decay:

$$\pi^+ \rightarrow \pi^0 e^+ \nu$$

(PIBETA: 1999–2001 runs)

Quark-Lepton (Cabibbo) Universality

The basic weak-interaction **V-A** form (e.g., μ decay):

$$\mathcal{M} \propto \langle e | l^\alpha | \nu_e \rangle \rightarrow \bar{u}_e \gamma^\alpha (1 - \gamma_5) u_\nu$$

is replicated in hadronic weak decays

$$\mathcal{M} \propto \langle p | h^\alpha | n \rangle \rightarrow \bar{u}_p \gamma^\alpha (\mathbf{G}_V - \mathbf{G}_A \gamma_5) u_n \quad \text{with} \quad \mathbf{G}_{V,A} \simeq \mathbf{1}.$$

Departure from $\mathbf{G}_V = \mathbf{1}$ (**CVC**) comes from **weak quark (Cabibbo) mixing**: $\mathbf{G}_V = \mathbf{G}_\mu \cos \theta_C (= \mathbf{G}_\mu \mathbf{V}_{ud}) \quad \cos \theta_C \simeq 0.97$

3 **q** generations lead to the Cabibbo-Kobayashi-Maskawa (CKM) matrix (1973):

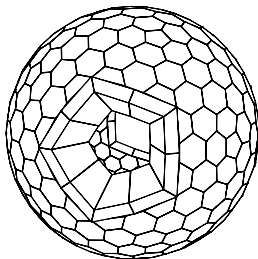
$$\begin{pmatrix} \mathbf{V}_{ud} & \mathbf{V}_{us} & \mathbf{V}_{ub} \\ \mathbf{V}_{cd} & \mathbf{V}_{cs} & \mathbf{V}_{cb} \\ \mathbf{V}_{td} & \mathbf{V}_{ts} & \mathbf{V}_{tb} \end{pmatrix}$$

CKM unitarity cond.: $\Delta \mathbf{V}^2 = 1 - (|\mathbf{V}_{ud}|^2 + |\mathbf{V}_{us}|^2 + |\mathbf{V}_{ub}|^2) \stackrel{?}{=} 0$, stringently tests the SM.

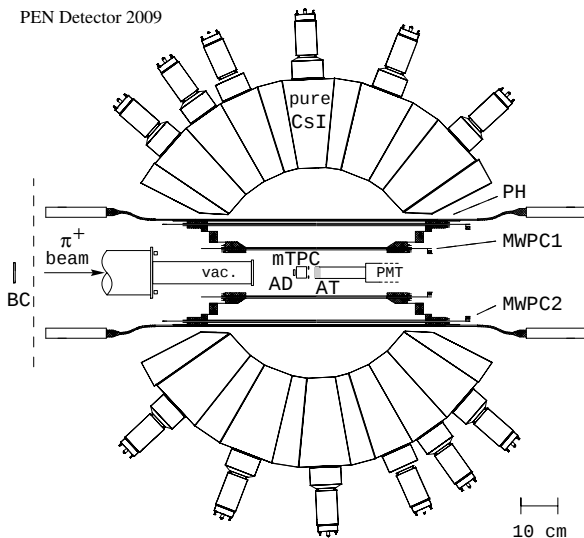
Prior to 2004 there was a **persistent $\sim 2.5\sigma$ shortfall** in $\Delta \mathbf{V}^2$, motivating many experiments to determine CKM m.e.'s, esp. $\mathbf{V}_{ud}$ and $\mathbf{V}_{us}$.

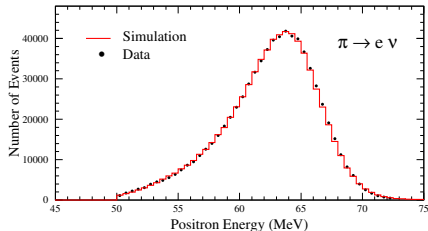
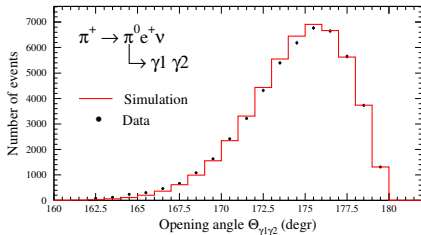
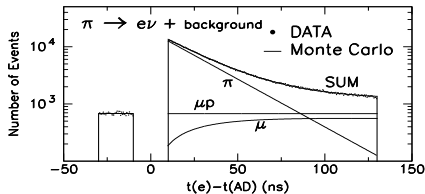
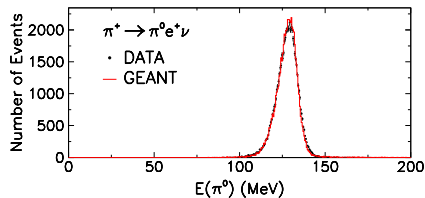
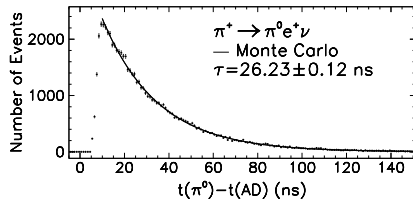
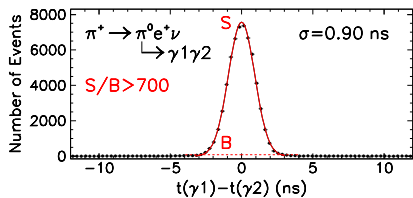
The PIBETA/PEN apparatus

stopped π^+ beam
 active target counter
 240-det. CsI calorimeter
 central tracking
 digitized waveforms
 stable temp./humidity



PEN Detector 2009





PIBETA result for π_β decay [PRL **93**, 181803 (2004)]

$$B_{\pi\beta}^{\text{exp-t}} = [1.040 \pm 0.004 (\text{stat}) \pm 0.004 (\text{syst})] \times 10^{-8},$$

$$B_{\pi\beta}^{\text{exp-e}} = [1.036 \pm 0.004 (\text{stat}) \pm 0.004 (\text{syst}) \pm 0.003 (\pi_{e2})] \times 10^{-8},$$

McFarlane et al. [PRD 1985]: $B = (1.026 \pm 0.039) \times 10^{-8}$

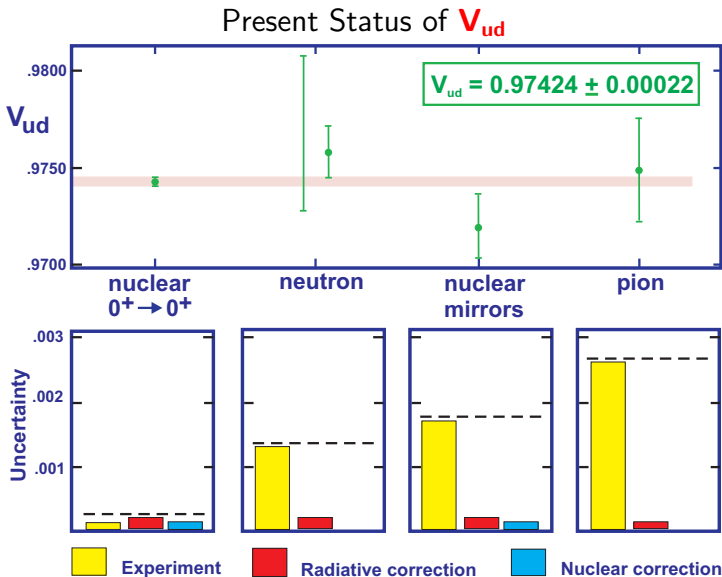
SM Prediction (PDG):

$$B = 1.038 - 1.041 \times 10^{-8} \quad (90\% \text{ C.L.})$$

$$(1.005 - 1.007 \times 10^{-8} \quad \text{excl. rad. corr.})$$

PDG 2008: $V_{ud} = 0.9742(3)$

PIBETA: $V_{ud} = 0.9748(25)$ or $V_{ud} = 0.9728(30)$.



(Courtesy of John Hardy, May 2009)

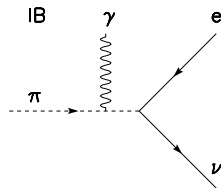
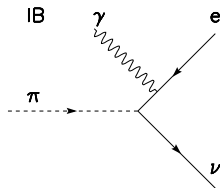
Radiative pion decay:

$$\pi^+ \rightarrow e^+ \nu \gamma$$

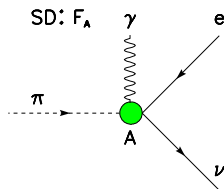
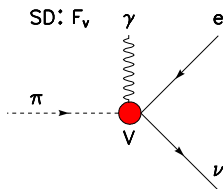
PIBETA: 1999-2001 & 2004 runs
(PEN: 2008–2010 runs)

$$\pi^+ \rightarrow e^+ \nu \gamma$$

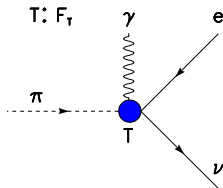
Standard **IB** and
V – A terms



SM



*A tensor
interaction, too?*



Exchange of $S=0$ leptoquarks

P Herczeg, PRD 49 (1994) 247

The $\pi \rightarrow e\nu\gamma$ amplitude and FF's

The IB amplitude (QED):

$$M_{IB} = -i \frac{e G_F V_{ud}}{\sqrt{2}} f_\pi m_e \epsilon^{\mu*} \bar{e} \left(\frac{k_\mu}{kq} - \frac{p_\mu}{pq} + \frac{\sigma_{\mu\nu} q^\nu}{2kq} \right) \times (1 - \gamma_5) \nu.$$

The structure-dependent amplitude:

$$M_{SD} = \frac{e G_F V_{ud}}{m_\pi \sqrt{2}} \epsilon^{\nu*} \bar{e} \gamma^\mu (1 - \gamma_5) \nu \times [F_V \epsilon_{\mu\nu\sigma\tau} p^\sigma q^\tau + i F_A (g_{\mu\nu} pq - p_\nu q_\mu)].$$

The SM branching ratio ($\gamma \equiv F_A/F_V$; $x = 2E_\gamma/m_\pi$; $y = 2E_e/m_\pi$),

$$\begin{aligned} \frac{d\Gamma_{\pi e 2\gamma}}{dx dy} = & \frac{\alpha}{2\pi} \Gamma_{\pi e 2} \left\{ IB(x, y) + \left(\frac{F_V m_\pi^2}{2f_\pi m_e} \right)^2 \right. \\ & \times [(1 + \gamma)^2 SD^+(x, y) + (1 - \gamma)^2 SD^-(x, y)] \\ & \left. + \left(\frac{F_V m_\pi}{f_\pi} \right) [(1 + \gamma) S_{\text{int}}^+(x, y) + (1 - \gamma) S_{\text{int}}^-(x, y)] \right\}. \end{aligned}$$

Available data on pion form factors

$$|F_V| \stackrel{\text{CVC}}{=} \frac{1}{\alpha} \sqrt{\frac{2\Gamma(\pi^0 \rightarrow \gamma\gamma)}{\pi m_{\pi^0}}} = 0.0259(9) .$$

$F_A \times 10^4$	reference	note
106 ± 60	Bolotov et al. (1990)	$(F_T = -56 \pm 17)$
135 ± 16	Bay et al. (1986)	
60 ± 30	Piilonen et al. (1986)	
110 ± 30	Stetz et al. (1979)	
116 ± 16	world average (PDG 2004)	

Available data on pion form factors

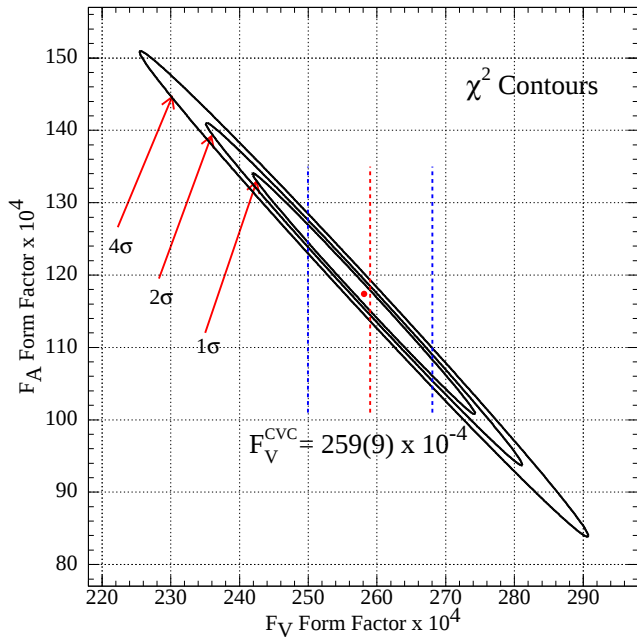
$$|F_V| \stackrel{\text{CVC}}{=} \frac{1}{\alpha} \sqrt{\frac{2\Gamma(\pi^0 \rightarrow \gamma\gamma)}{\pi m_{\pi^0}}} = 0.0259(9) .$$

$F_A \times 10^4$	reference	note
106 ± 60	Bolotov et al. (1990)	$(F_T = -56 \pm 17)$
135 ± 16	Bay et al. (1986)	
60 ± 30	Piilonen et al. (1986)	
110 ± 30	Stetz et al. (1979)	
116 ± 16	world average (PDG 2004)	

Available data on pion form factors

$$|F_V| \stackrel{\text{CVC}}{=} \frac{1}{\alpha} \sqrt{\frac{2\Gamma(\pi^0 \rightarrow \gamma\gamma)}{\pi m_{\pi^0}}} = 0.0259(9) .$$

$F_A \times 10^4$	reference	note
106 ± 60	Bolotov et al. (1990)	$(F_T = -56 \pm 17)$
135 ± 16	Bay et al. (1986)	
60 ± 30	Piilonen et al. (1986)	
110 ± 30	Stetz et al. (1979)	
116 ± 16	world average (PDG 2004)	

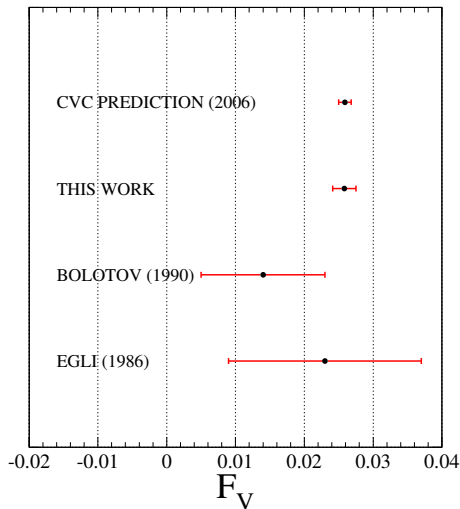
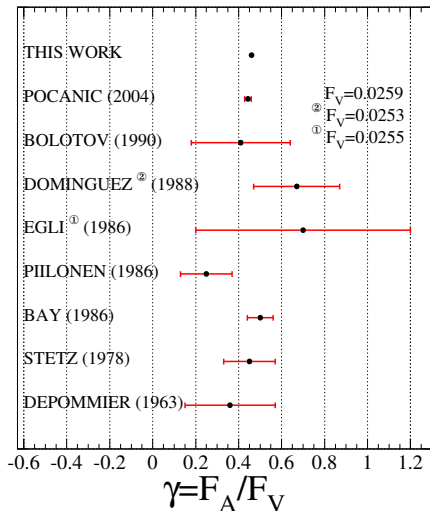


Best values of pion
form factor
parameters:

Combined analysis
of 1999-2001 and
2004 data sets

M. Bychkov, et al.,
PRL **103** (2009)
051802.

Experimental history of pion F_A and F_V



Summary of pion form factor and B.R. results

$$F_V = 0.0258 \pm 0.0017 \quad (14\times)$$

$$F_A = 0.0119 \pm 0.0001^{\text{exp}}_{(F_V^{\text{CVC}})} \quad (16\times)$$

$$a = 0.10 \pm 0.06 \quad (\infty)$$

$$-5.2 \times 10^{-4} < F_T < 4.0 \times 10^{-4} \quad 90\% \text{ C.L.}$$

Derived pion polarizability and π^0 lifetime (at L.O.):

$$\alpha_E = -\beta_M = (2.783 \pm 0.023_{\text{exp}}) \times 10^{-4} \text{ fm}^3$$

$$\tau_{\pi^0} = (8.5 \pm 1.1) \times 10^{-17} \text{ s} \quad \left\{ \begin{array}{l} \text{current PDG avg: } 8.4(5) \\ \text{PrimEx p'print: } 8.32(23) \end{array} \right.$$

$$B_{\pi_{e2\gamma}}(E_\gamma > 10 \text{ MeV}, \theta_{e\gamma} > 40^\circ) = 73.86(54) \times 10^{-8} \quad (17\times)$$

Above results will be improved with new PEN data and analysis.

Allowed muon decays:

$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \quad (\text{TWIST 2003–05})$$

$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma \quad (\text{PIBETA 2004, PEN 2008–10})$$

Michel parameters of muon decay: $\mu \rightarrow e \nu_\mu \bar{\nu}_e$

$$\frac{d^2\Gamma}{dx d(\cos\theta)} = \frac{m_\mu}{4\pi^3} W_{e\mu}^4 G_F^2 \sqrt{x^2 - x_0^2} \times \\ \times [\mathbf{F}_{\text{IS}}(x) + P_{\mu^+} \cos\theta \mathbf{F}_{\text{AS}}(x)] [1 + \vec{P}_{e^+}(x, \theta) \cdot \hat{\zeta}]$$

Isotropic part:

$$\mathbf{F}_{\text{IS}}(x) = x(1-x) + \frac{2}{9} \rho (4x^2 - 3x - x_0^2) + \eta x_0(1-x)$$

Anisotropic part:

$$\mathbf{F}_{\text{AS}}(x) = \frac{1}{3} \xi \sqrt{x^2 - x_0^2} \left(1 - x + \frac{2}{3} \delta \left[4x - 3 + \left(\sqrt{1 - x_0^2} - 1 \right) \right] \right)$$

Michel parameters of radiative muon decay: $\mu \rightarrow e \nu_\mu \bar{\nu}_e \gamma$

$$\frac{d^3 B(x, y, \theta)}{dx dy 2\pi d(\cos \theta)} = f_1(x, y, \theta) + \bar{\eta} f_2(x, y, \theta) + \left(1 - \frac{4}{3} \rho\right) f_3(x, y, \theta)$$

$$\rho = \frac{3}{4} - \frac{3}{4} \left[|g_{LR}^V|^2 + |g_{RL}^V|^2 + 2|g_{LR}^T|^2 + 2|g_{RL}^T|^2 + \Re(g_{RL}^S g_{RL}^{T*} + g_{LR}^S g_{LR}^{T*}) \right] \stackrel{\text{SM}}{=} \frac{3}{4},$$

$$\bar{\eta} = \left(|g_{RL}^V|^2 + |g_{LR}^V|^2 \right) + \frac{1}{8} \left(|g_{LR}^S + 2g_{LR}^T|^2 + |g_{RL}^S + 2g_{RL}^T|^2 + 2 \left(|g_{LR}^T|^2 + |g_{RL}^T|^2 \right) \right) \stackrel{\text{SM}}{=} 0.$$

Experimental Limits (90 % C.L.) on $g_{\alpha\beta}^{\gamma}$

$ g_{\alpha\beta}^{\gamma} $	S	V	T
LL	0.550	>0.960	$\equiv 0$
LR	0.088	0.036	0.025
RL	0.417	0.104	0.104
RR	0.067	0.034	$\equiv 0$
max. values:	$ g_{\alpha\beta}^S $ ≤ 2	$ g_{\alpha\beta}^V $ ≤ 1	$ g_{\alpha\beta}^T $ $\leq \frac{1}{\sqrt{3}} \approx 0.58$

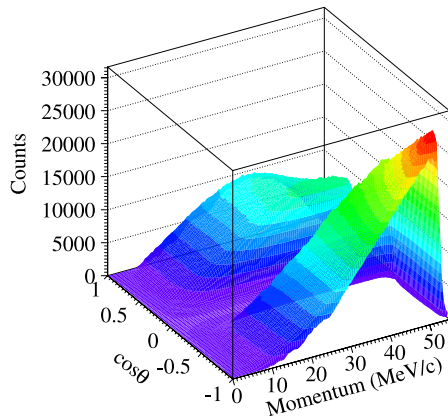
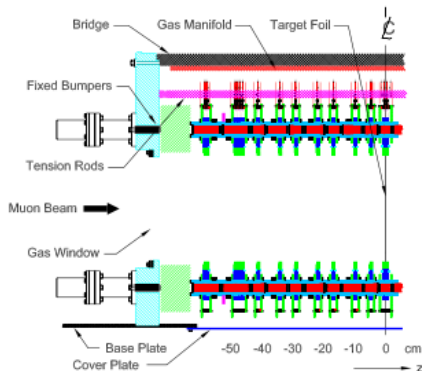
[Most recent global fit by C.A Gagliardi et al., PR D **72** (2005) 073002]

Experimental Limits (90 % C.L.) on $g_{\alpha\beta}^{\gamma}$

$ g_{\alpha\beta}^{\gamma} $	S	V	T
LL	0.550	>0.960	$\equiv 0$
LR	0.088	0.036	0.025
RL	0.417	0.104	0.104
RR	0.067	0.034	$\equiv 0$
max. values:	$ g_{\alpha\beta}^S $ ≤ 2	$ g_{\alpha\beta}^V $ ≤ 1	$ g_{\alpha\beta}^T $ $\leq \frac{1}{\sqrt{3}} \approx 0.58$

[Most recent global fit by C.A Gagliardi et al., PR D **72** (2005) 073002]

OMD study: TWIST experiment (TRIUMF)

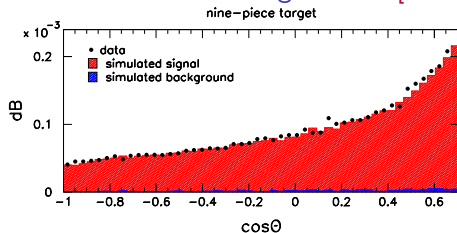


Main results:

$$\rho = 0.7501(5) \quad \text{and} \quad \delta = 0.7507(7),$$

MacDonald, et al., Phys. Rev. D **78** (2008) 032010.

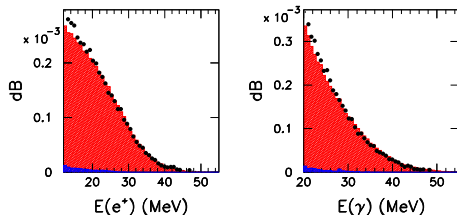
RMD differential branching ratio [B. VanDevender, PhD thesis]



PRELIMINARY

(new analysis+data)

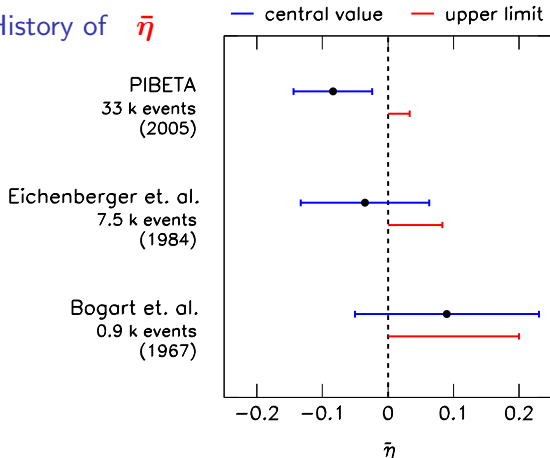
due to small-angle
bremsstrahlung
uncertainties in GEANT



$$B^{\text{exp}} = [4.40 \pm 0.02 \text{ (stat.)} \pm 0.09 \text{ (syst.)}] \times 10^{-3}$$

14x!

$$B^{\text{theo}} = 4.30 \times 10^{-3} \quad (E_{\gamma} > 10 \text{ MeV}, \theta > 30^{\circ})$$

Experimental History of $\bar{\eta}$ 

PIBETA preliminary (B. VanDevender, PhD thesis; 2004 data set):

$$\bar{\eta} = -0.084 \pm 0.050(\text{stat.}) \pm 0.034(\text{syst.})$$

$\Rightarrow \bar{\eta} \leq 0.033$; new world average: $\bar{\eta} \leq 0.028$ (68 % c.l.)

reduced by a factor of 2.5.

The π_{e2} decay:

$$\pi^+ \rightarrow e^+ \nu$$

PEN and PiENu experiments (2006–)

$\pi \rightarrow e \nu$ decay: SM calculations; measurements

Modern theoretical calculations: $B_{\text{calc}} = \frac{\Gamma(\pi \rightarrow e \bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}(\gamma))_{\text{calc}}} =$

$$\begin{cases} 1.2352(5) \times 10^{-4} & \text{Marciano and Sirlin, [PRL **71** (1993) 3629]} \\ 1.2354(2) \times 10^{-4} & \text{Finkemeier, [PL B **387** (1996) 391]} \\ 1.2352(1) \times 10^{-4} & \text{Cirigliano and Rosell, [PRL **99**, 231801 (2007)]} \end{cases}$$

Experiment, world average [current PDG]:

$$\frac{\Gamma(\pi \rightarrow e \bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}(\gamma))_{\text{exp}}} = (1.230 \pm 0.004) \times 10^{-4}$$

N.B.:

PEN, PiENu aim at: $\frac{\delta B}{B} \simeq 5 \times 10^{-4}$

$\pi \rightarrow e \nu$ decay: SM calculations; measurements

Modern theoretical calculations: $B_{\text{calc}} = \frac{\Gamma(\pi \rightarrow e \bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}(\gamma))_{\text{calc}}} =$

$$\begin{cases} 1.2352(5) \times 10^{-4} & \text{Marciano and Sirlin, [PRL **71** (1993) 3629]} \\ 1.2354(2) \times 10^{-4} & \text{Finkemeier, [PL B **387** (1996) 391]} \\ 1.2352(1) \times 10^{-4} & \text{Cirigliano and Rosell, [PRL **99**, 231801 (2007)]} \end{cases}$$

Experiment, world average [current PDG]:

$$\frac{\Gamma(\pi \rightarrow e \bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}(\gamma))_{\text{exp}}} = (1.230 \pm 0.004) \times 10^{-4}$$

N.B.:

PEN, PiENu aim at: $\frac{\delta B}{B} \simeq 5 \times 10^{-4}$

$\pi \rightarrow e \nu$ decay: SM calculations; measurements

Modern theoretical calculations: $B_{\text{calc}} = \frac{\Gamma(\pi \rightarrow e \bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}(\gamma))_{\text{calc}}} =$

$$\left\{ \begin{array}{ll} 1.2352(5) \times 10^{-4} & \text{Marciano and Sirlin, [PRL 71 (1993) 3629]} \\ 1.2354(2) \times 10^{-4} & \text{Finkemeier, [PL B 387 (1996) 391]} \\ 1.2352(1) \times 10^{-4} & \text{Cirigliano and Rosell, [PRL 99, 231801 (2007)]} \end{array} \right.$$

Experiment, world average [current PDG]:

$$\frac{\Gamma(\pi \rightarrow e \bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}(\gamma))_{\text{exp}}} = (1.230 \pm 0.004) \times 10^{-4}$$

N.B.:

PEN, PiENu aim at: $\frac{\delta B}{B} \simeq 5 \times 10^{-4}$

π_{e2} Decay and the SM

$B(\pi_{e2})$ in SM dominated by ($V - A$) helicity suppression. Deviations primarily due to PS int. terms. Most general 4-fermion π_{e2} amplitude:

$$\frac{G_F}{\sqrt{2}} \left[(\bar{d}\gamma_\mu\gamma^5 u) (\bar{\nu}_e\gamma^\mu\gamma^5(1 - \gamma^5)e) f_{AL}^e + f_{PL}^e (\bar{d}\gamma^5 u) (\bar{\nu}_e\gamma^5(1 - \gamma^5)e) \right] + \text{r.h. } \nu \text{ term}$$

In the SM: $f_{AL}^\ell = 1$, while $f_{xR}^\ell = f_{Px}^\ell = 0$, with $\ell = e, \mu$.

Strong helicity suppression amplifies sensitivity to f_{PL}^e :

$$\frac{B_{\pi e2}^{\text{obs}} - B_{\pi e2}^{\text{SM}}}{B_{\pi e2}^{\text{SM}}} = \frac{\Delta B}{B^{\text{SM}}} = \dots \simeq \frac{2m_\pi^2}{m_e(m_u + m_d)} f_{PL}^e \simeq \boxed{7700 f_{PL}^e} !$$

Tgt accuracy of the PEN experiment, $\Delta B/B \simeq 5 \times 10^{-4}$, translates into attractive mass limits:

Example mass bounds from PEN goal accuracy

- (a) Charged Higgs, m_{H^+} [Shanker, NP B204 (82) 375]

Given a mixing angle suppression $S \approx 10^{-2}$, we get

$$f_{\text{PL}}^e \approx S \frac{m_t m_\tau}{m_{H^+}^2} \quad \text{yielding} \quad m_{H^+} > 6.9 \text{ TeV}.$$

- (b) Pseudoscalar leptoquarks, m_P

Given an estimated effective Yukawa coupling of $y \simeq 1/250$, we can find m_P , mass of the color-triplet PS l - q :

$$f_{\text{PL}}^e \approx \frac{\sqrt{2}}{G_F} \frac{y^2}{2m_P^2} \quad \text{yielding} \quad m_P > 3.8 \text{ TeV}.$$

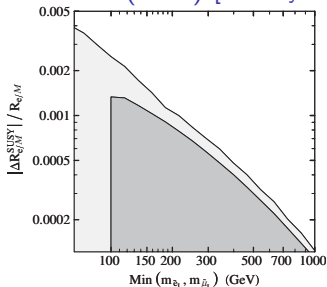
- (c) Vector leptoquarks, M_G

Following Shanker who assumes gauge coupling $g \simeq g_{\text{SU}(2)}$, we get:

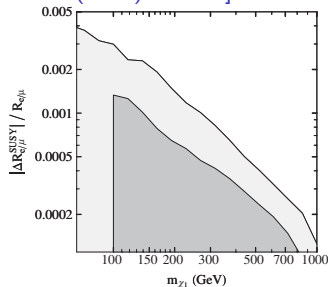
$$f_{\text{PL}}^e \approx \frac{4M_W^2}{M_G^2} \quad \text{yielding} \quad M_G > 630 \text{ TeV}.$$

MSSM calculations (RPC) [Ramsey-Musolf et al., PR D76 (2007) 095017]

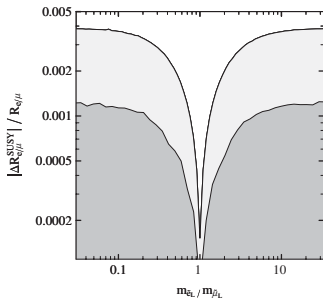
minimal
selectron,
smuon
masses:



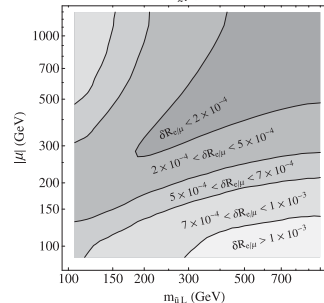
lowest
mass
chargino:



slepton
mass de-
generacy:



Higgsino
mass
param. μ
and $m_{\tilde{U}_L}$:



RPV scenario constraints also discussed.

Lepton universality (and neutrinos)

From

$$R_{e/\mu} = \frac{\Gamma(\pi \rightarrow e \bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}(\gamma))} = \frac{g_e^2}{g_\mu^2} \frac{m_e^2}{m_\mu^2} \frac{(1 - m_e^2/m_\mu^2)^2}{(1 - m_\mu^2/m_\pi^2)^2} (1 + \delta R_{e/\mu})$$

$$R_{\tau/\pi} = \frac{\Gamma(\tau \rightarrow e \bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu \bar{\nu}(\gamma))} = \frac{g_\tau^2}{g_\mu^2} \frac{m_\tau^3}{2m_\mu^2 m_\pi} \frac{(1 - m_\pi^2/m_\tau^2)^2}{(1 - m_\mu^2/m_\pi^2)^2} (1 + \delta R_{\tau/\pi})$$

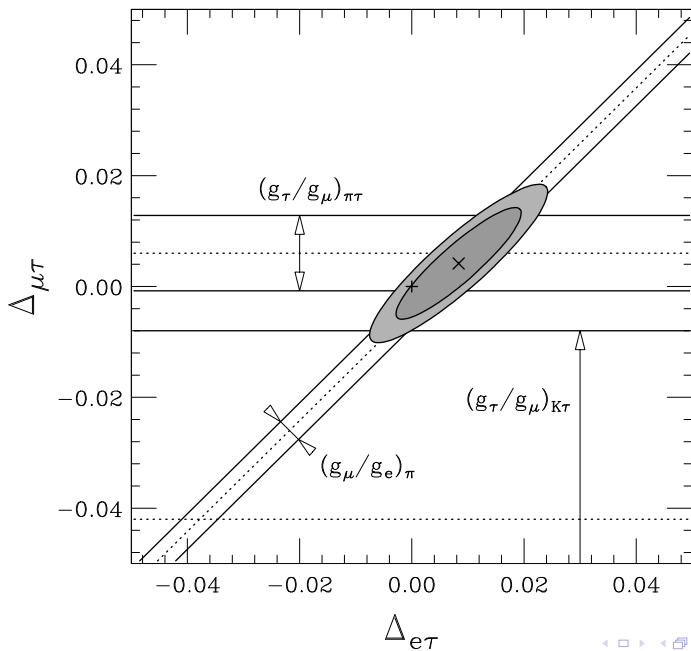
one can evaluate

$$\left(\frac{g_e}{g_\mu} \right)_\pi = 1.0021 \pm 0.0016 \quad \text{and} \quad \left(\frac{g_\tau}{g_\mu} \right)_{\pi\tau} = 1.0030 \pm 0.0034.$$

For comparison

$$\left(\frac{g_e}{g_\mu} \right)_W = 0.999 \pm 0.011 \quad \text{and} \quad \left(\frac{g_\tau}{g_e} \right)_W = 1.029 \pm 0.014.$$

[Presently allowed level of LUV could account for “NuTeV anomaly.”]



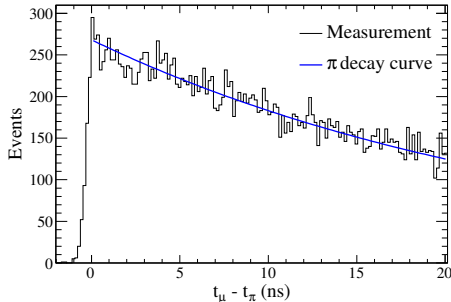
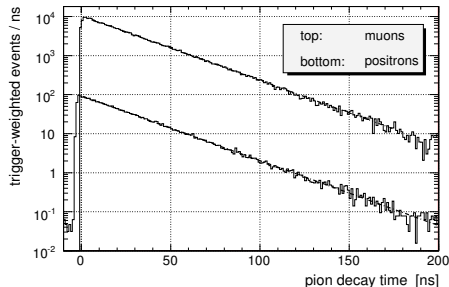
Loinaz et al.,
PRD **70** (2004)
113004

$$\Delta_{\ell\ell'} = 2 \left(\frac{g_\ell}{g_{\ell'}} - 1 \right)$$

PEN experiment: status and plans

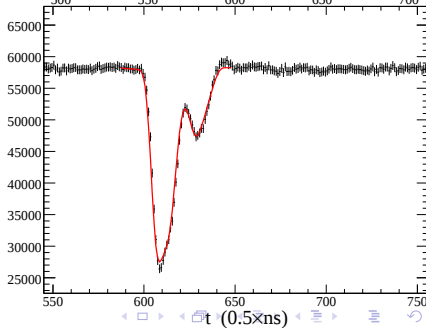
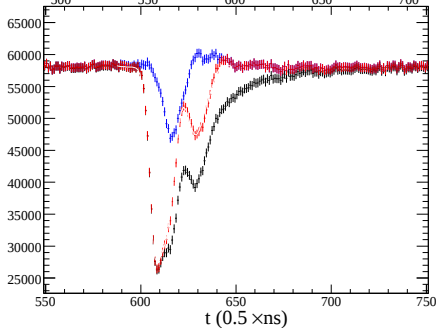
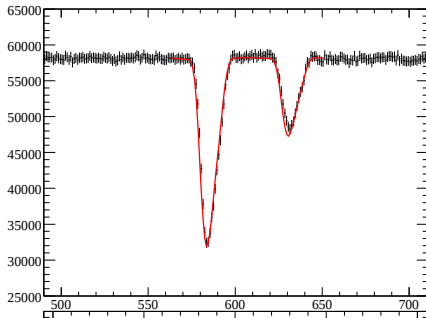
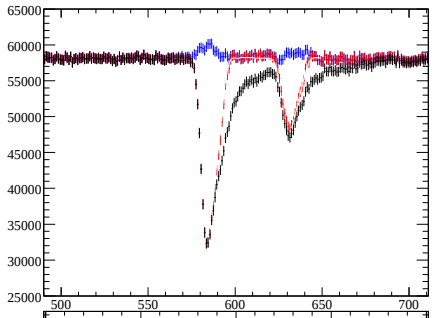
- ▶ Approved in 2006; development runs: 2007, '08; data runs '09, '10.
- ▶ Improved beam tracking (**miniTPC**) implemented in '09, '10 runs.
- ▶ $> 20 \text{ M } \pi_{e2}$'s recorded $\Rightarrow (\delta B/B)_{\text{stat}} \simeq 2 \times 10^{-4}$.

Illustration: decays in the target detector (2008 run):



Waveform fitting in PEN

[Anthony Palladino]



D. Počanić (UVa)

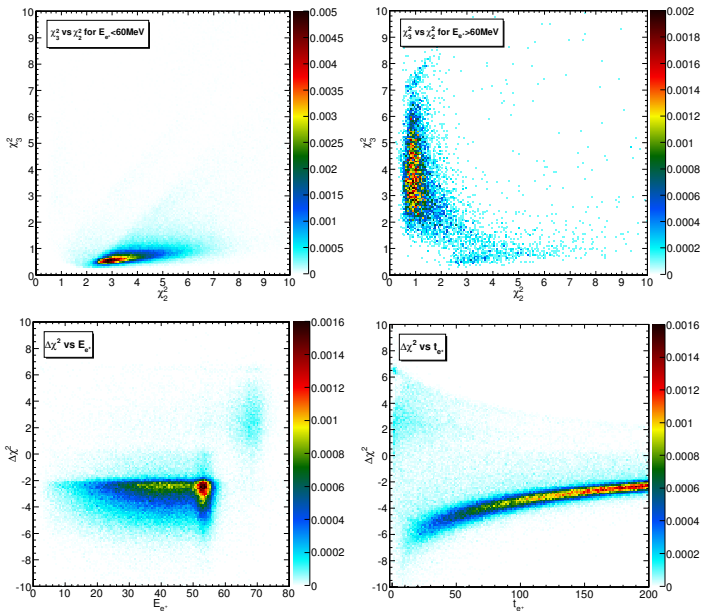
 π, μ decays

PSI2010, 12 Oct '10

34 / 39

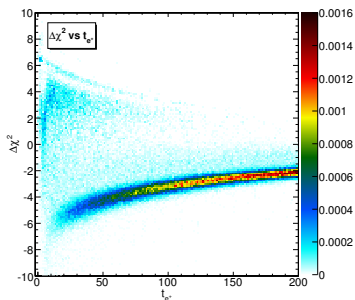
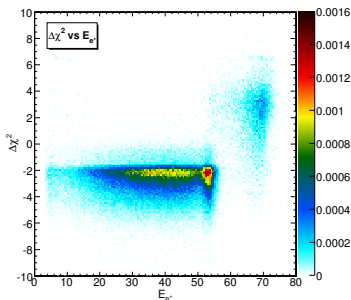
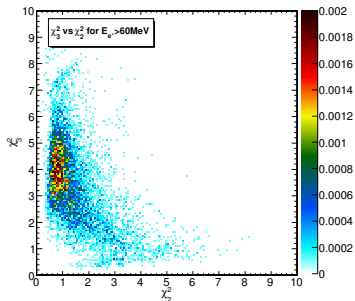
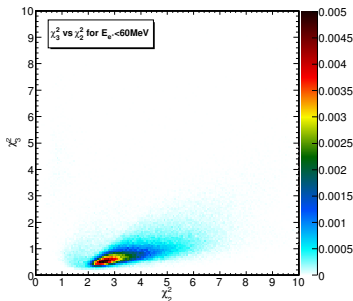
PEN: distinguishing $\pi \rightarrow e$ and $\pi \rightarrow \mu \rightarrow e$ decays (measurement)

[A. Palladino & L.P. Alonzi]

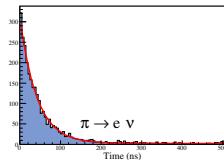
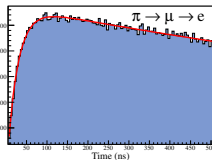
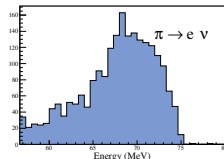
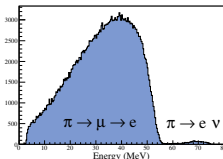
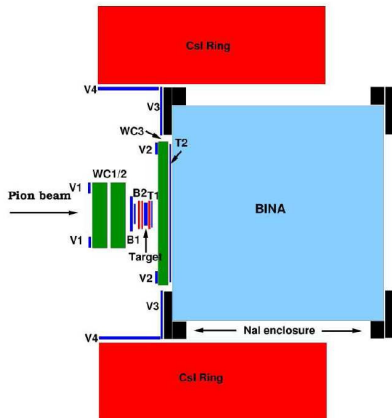


PEN: distinguishing $\pi \rightarrow e$ and $\pi \rightarrow \mu \rightarrow e$ decays (simulation)

[A. Palladino & L.P. Alonzi]



PiENu experiment (TRIUMF)



Acceptance: $\Delta\Omega \simeq 0.2 \times 4\pi \text{ sr}$
Excellent energy resolution.

Project started in 2006. Data taking currently under way.

Status of allowed π and μ decays

- ▶ A *significant experimental effort* is under way to make use of the *unparalleled theoretical precision* in the weak interactions of the lightest particles.
- ▶ Information obtained is *complementary to* expected *collider results*, and necessary for their proper interpretation.
- ▶ *Orders of magnitude* improvement in precision has been achieved; more lie in store.
- ▶ These projects are *ideally suited to PSI* (and *TRIUMF*).
- ▶ *Modest scale* of investment of resources required.
- ▶ *Unique opportunity* for scientific advancement.
- ▶ Great projects for *graduate students and postdocs*—full range of *professional training*.

Current and former PIBETA and PEN collaborators

L. P. Alonzi^a, K. Assamagan^a, V. A. Baranov^b, W. Bertl^c, C. Broennimann^c,
 S. Bruch^a, M. Bychkov^a, Yu.M. Bystritsky^b, M. Daum^c, T. Flügel^c, E. Frlež^a,
 R. Frosch^c, K. Keeter^a, V.A. Kalinnikov^b, N.V. Khomutov^b, J. Koglin^a,
 A.S. Korenchenko^b, S.M. Korenchenko^b, M. Korolija^d, T. Kozlowski^e,
 N.P. Kravchuk^b, N.A. Kuchinsky^b, D. Lawrence^h, W. Li^a, J. S. McCarthy^a,
 R. C. Minehart^a, D. Mzhavia^{b,f}, A. Palladino^{a,c}, D. Počanić^{a*}, B. Ritchie^h,
 S. Ritt^{a,c}, P. Robmann^g, O.A. Rondon-Aramayo^a, A.M. Rozhdestvensky^b,
 T. Sakhelashvili^f, S.N. Shkarovskiy^b, P. L. Slocum^a, L. C. Smith^a, N. Soić^d,
 U. Straumann^g, I. Supek^d, P. Truöl^g, Z. Tsamalaidze^f, A. van der Schaaf^{g*},
 E.P. Velicheva^b, V.P. Volnykh^b, Y. Wang^a, C. Wigger^c, H.-P. Wirtz^c, K. Ziock^a.

^aUniv. of *Virginia*, USA

^c*PSI*, Switzerland

^e*Swierk*, Poland

^gUniv. *Zürich*, Switzerland

^b*JINR, Dubna*, Russia

^d*IRB, Zagreb*, Croatia

^f*IHEP, Tbilisi*, Georgia

^h*Arizona State Univ.*, USA

Home pages: <http://pibeta.phys.virginia.edu>
<http://pen.phys.virginia.edu>